

Experimental Results on CP Violation

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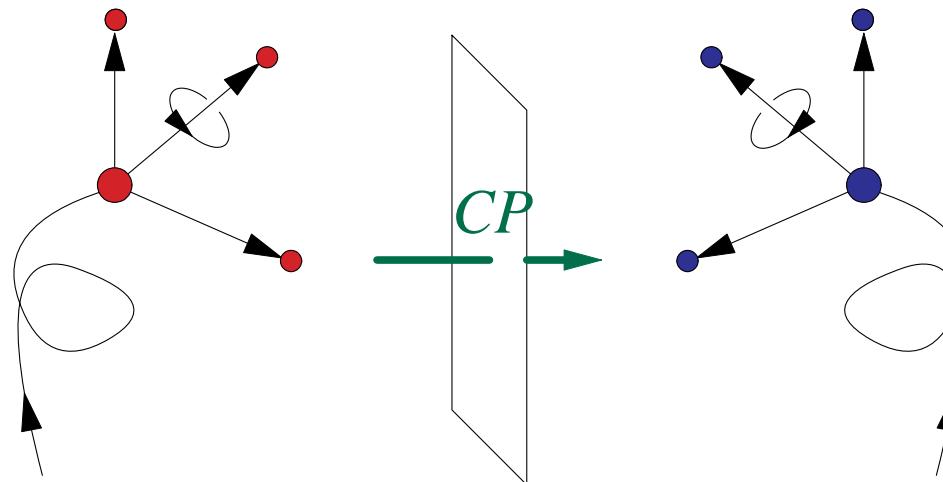


$\leftarrow CP \rightarrow$



CP Violation

C : particle \leftrightarrow antiparticle,
P : $\vec{x} \leftrightarrow -\vec{x}$ (\equiv mirror inversion)



Both satisfy the same law \rightarrow the law is CP symmetric.
If any phenomena do not \rightarrow CP violation.

CP Symmetry in Quantum Mechanics

Transition probability: $|\langle f|S|i\rangle|^2 = |\langle CPf|S|CPI\rangle|^2$
 $(CP: n \leftrightarrow \bar{n}, \vec{p} \leftrightarrow -\vec{p}, \vec{s}, \vec{L} \text{ unchanged})$

Suppose $(CP)S(CP)^\dagger = S$
or equivalently $(CP)H(CP)^\dagger = H$ or $[CP, H] = 0$

1. CP symmetry:

$$\langle f|S|i\rangle = \langle f|(\underbrace{CP)S(CP)^\dagger}_{S}(CP)|i\rangle = \langle CPf|S|CPI\rangle$$

2. Conservation of CP eigenvalues:

If $CP|i\rangle = \xi_i|i\rangle$, $CP|f\rangle = \xi_f|f\rangle$,

$$\langle f|S|i\rangle = \underbrace{\langle f|(\underbrace{CP)S(CP)^\dagger}_{S}(CP)|i\rangle}_{\xi_f^* \langle f| \xi_i | i \rangle} = \xi_f^* \xi_i \langle f|S|i\rangle$$

i.e. $\langle f|S|i\rangle = 0$ unless $\xi_f^* \xi_i = 1$ (namely $\xi_f = \xi_i$).

CP Violation (CPV) in K^0 - \bar{K}^0 System

If CP is conserved, i.e. $[CP, H] = 0$
 $\rightarrow K_{1,2}$: eigenstates of H (mass) and CP (*)

exp.: Mass eigenstates $K_{S,L}$ both decay to $\pi\pi(CP+)$

Two possibilities:

1. $K_{S,L}$ are CP eigenstates
 \rightarrow one is ($CP-$) decaying to $\pi\pi(CP+)$: CPV
CPV in decay (Direct CPV)
2. $K_{S,L}$ are not CP eigenstates.
Inverse of (*) ($K_{S,L}$ not degenerate) : CPV
CPV in mixing (Indirect CPV)

Either case, CP is violated.

(n.b.: 2. does not work for neutron system which is degenerate.)

Direct CP Violation in K^0 - \bar{K}^0 System

CPV in mixing (assuming CPT)

$$\begin{cases} K_S = K_1 + \epsilon K_2 \\ K_L = K_2 + \epsilon K_1 \end{cases} \quad (K_{1,2} : CP+, -)$$

If no CPV in decay, then for any CP eigenstate f

$$(CP_f = +) \quad \eta_f \equiv \frac{A(K_L \rightarrow f)}{A(K_S \rightarrow f)} = \epsilon$$

$$(CP_f = -) \quad \eta_f \equiv \frac{A(K_S \rightarrow f)}{A(K_L \rightarrow f)} = \epsilon$$

Any difference in η_f for different f
→ CPV in decay (direct CPV)

Direct CP Violation in $K_{S,L} \rightarrow \pi\pi$

Difference between $\pi^+\pi^-$ and $\pi^0\pi^0$ written as

$$\eta_{+-} \equiv \frac{A(K_L \rightarrow \pi^+\pi^-)}{A(K_S \rightarrow \pi^+\pi^-)} = \epsilon + \epsilon'$$

$$\eta_{00} \equiv \frac{A(K_L \rightarrow \pi^0\pi^0)}{A(K_S \rightarrow \pi^0\pi^0)} = \epsilon - 2\epsilon'$$

We measure the double ratio,

$$\frac{\Gamma(K_L \rightarrow \pi^+\pi^-)/\Gamma(K_S \rightarrow \pi^+\pi^-)}{\Gamma(K_L \rightarrow \pi^0\pi^0)/\Gamma(K_S \rightarrow \pi^0\pi^0)} = 1 + 6 \operatorname{Re} \frac{\epsilon'}{\epsilon}$$

Two experiments:

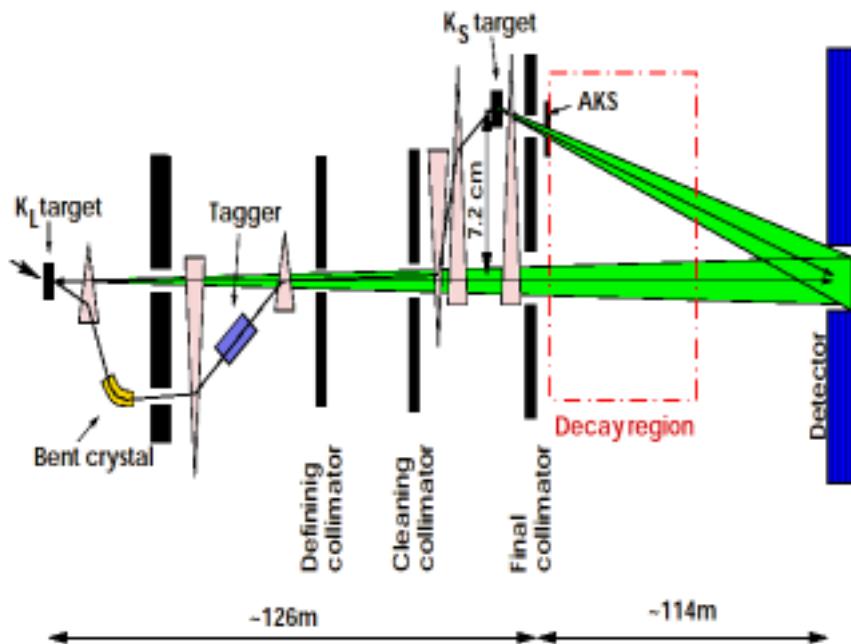
NA48 (CERN) and Fermilab E832 (KTeV)

Simultaneous logging of all 4 modes

(Makes insensitive to K_S/K_L beam ratio, deadtimes)

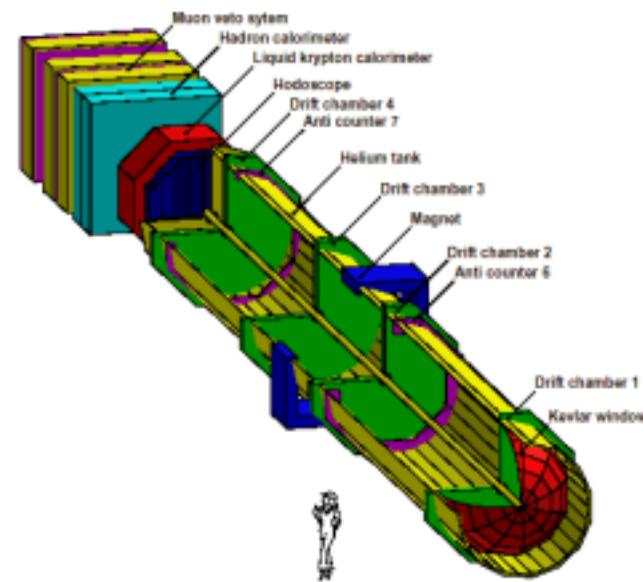
NA48 (CERN)

Beamline



- Use tagged p's for K_S .
- Liq. Kr calorimeter.
- $K_{S,L}$ separated by p-tag.

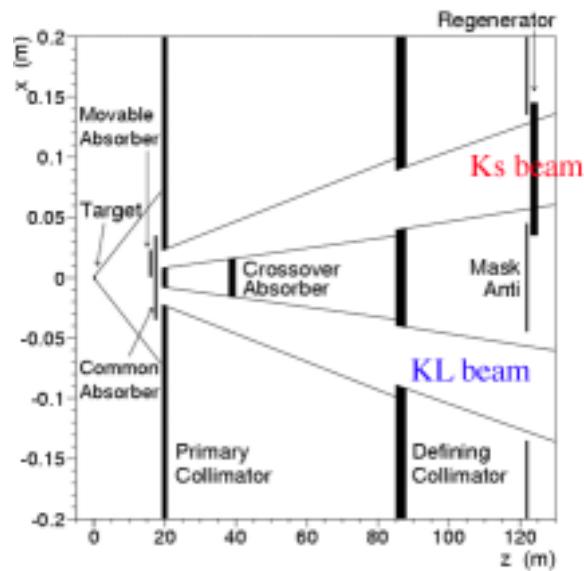
Detector



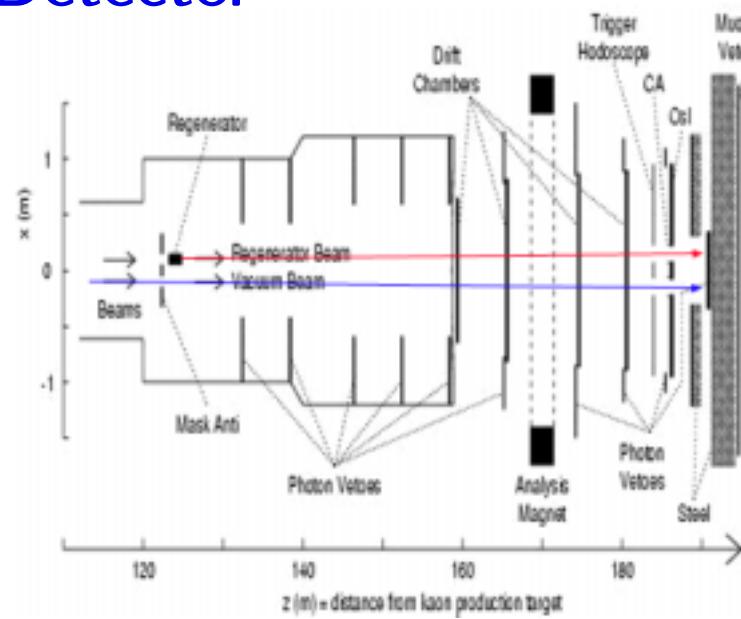
- $K_{S,L}$ beams converge.
Cancels transverse bias.
- Longitudinal effect:
re-weighting by z.

Fermilab E832 (KTeV)

Beamline

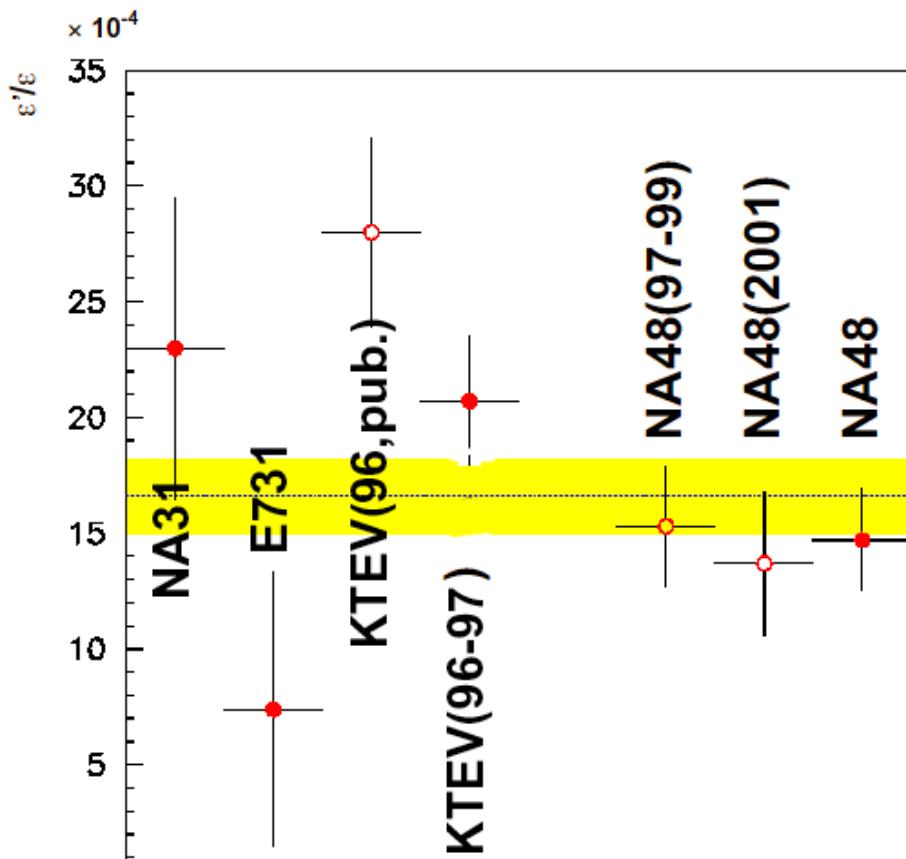


Detector



- Use regenerator for K_S .
- Pure CsI calorimeter.
- $K_{S,L}$ separated by CM.
- $K_{S,L}$ beams alternate.
Cancels transverse bias.
- Longitudinal effect: MC.

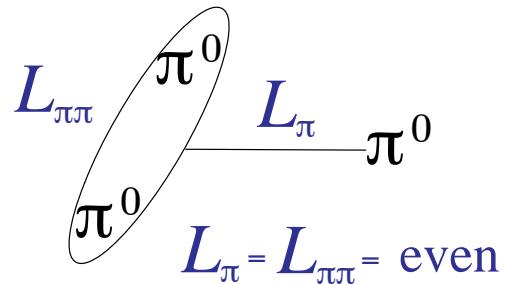
ϵ'/ϵ Results



$$\text{Re} \frac{\epsilon'}{\epsilon} = \begin{cases} (14.7 \pm 2.2) \times 10^{-4} & (\text{NA48: full data, } PL, 2002) \\ (20.7 \pm 2.8) \times 10^{-4} & (\text{E832: partial data, } PRD, 2003) \end{cases}$$

- Direct CPV in $K \rightarrow \pi\pi$ is firmly established.
- Theory: $(-10 \sim 40) \times 10^{-4}$ (hadronic uncertainty)
- → Cannot constrain CPV CKM phases.

Search for CPV in $K_{S,L} \rightarrow 3\pi^0(CP-) \quad (\text{NA48})$



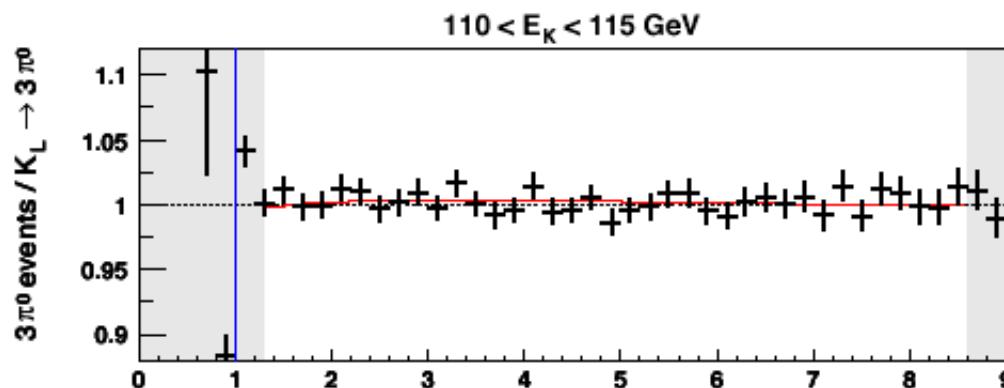
$$CP_{\pi\pi} = +, CP_{\pi^0} = -, \\ CP_{3\pi^0} = CP_{\pi\pi} \cdot CP_{\pi^0} \cdot (-)^{L_\pi} = -$$

IF no direct CPV, we expect

$$\eta_{000} \equiv \frac{A(K_S \rightarrow 3\pi^0)}{A(K_L \rightarrow 3\pi^0)} = \eta_{\pi\pi} \sim 2.3 \times 10^{-3} e^{i\frac{\pi}{4}}$$

Compare the K_S beam ('Near': $K_{S,L}$ 50/50 at $t = 0$)
with the K_L beam ('Far').

η_{000} Result (NA48)



$$\text{Re}\eta_{000} = -0.026 \pm 0.010$$

$$\text{Im}\eta_{000} = -0.034 \pm 0.010$$

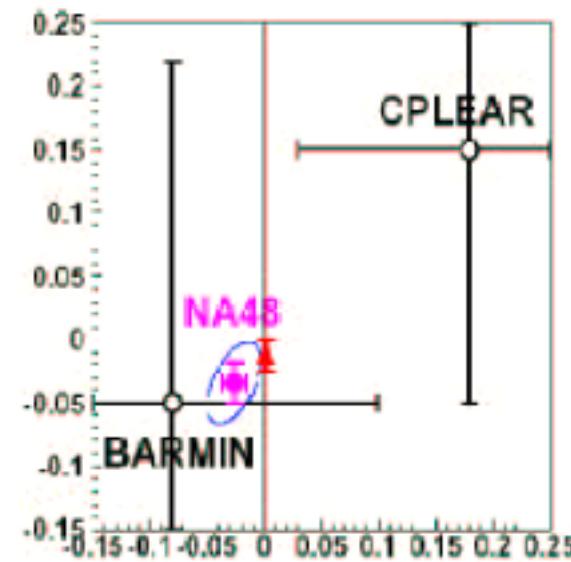
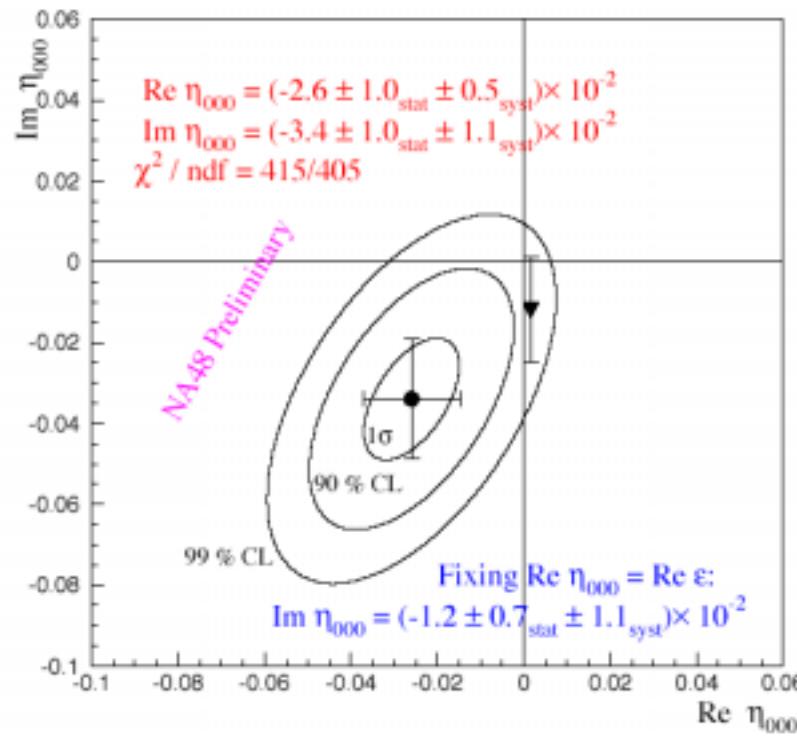
$$Br(K_S \rightarrow 3\pi^0) = 1.4 \times 10^{-6} \quad (90\% c.l.)$$

$$\text{Assume CPT } (\text{Re}\eta_{000} = \text{Re}\eta_{\pi\pi})$$

$$\text{Im}\eta_{000} = -0.012 \pm 0.007 \pm 0.011$$

$$Br(K_S \rightarrow 3\pi^0) < 3.0 \times 10^{-7} \quad (90\% c.l.)$$

Comparison with Other η_{000} Result



About factor of 10 improvement.
(note also: Novosibirsk $\text{Br}(K_S \rightarrow 3\pi^0) < 1.4 \times 10^{-5}$)

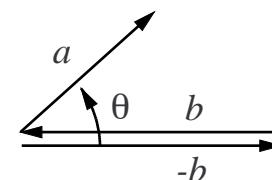
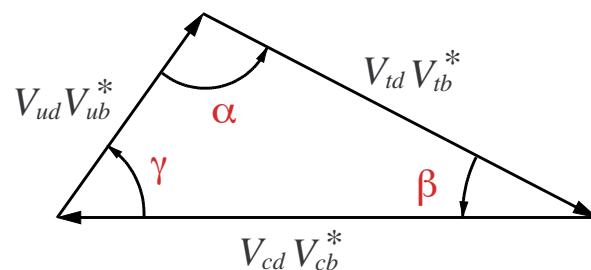
Another $\times 10$ improvement needed for CPV.

CPV in B Meson System

$$\mathcal{L}_{qW}(x) = \frac{g}{\sqrt{2}} \sum_{i,j=1,3} V_{ij} \bar{u}_{iL} \gamma_\mu d_{jL} W^\mu$$

$u_i = (u, c, t)$, $d_i = (d, s, b)$, and V =CKM matrix (unitary):
e.g: orthogonality of d -column and b -column:

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$



$$\theta = \arg \frac{a}{-b}$$

$$\alpha/\phi_2 \equiv \arg \left(\frac{V_{td}V_{tb}^*}{-V_{ud}V_{ub}^*} \right), \quad \beta/\phi_1 \equiv \arg \left(\frac{V_{cd}V_{cb}^*}{-V_{td}V_{tb}^*} \right), \quad \gamma/\phi_3 \equiv \arg \left(\frac{V_{ud}V_{ub}^*}{-V_{cd}V_{cb}^*} \right)$$

e^+e^- B-Factories

$$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B^0\bar{B}^0, B^+B^-$$

B 's nearly at rest in the $\Upsilon(4S)$ frame:

$$\beta_B \sim 0.06$$

	PEPII(BaBar)	KEKB(Belle)	CESR(CLEO2.x)
type	asymmetric	asymmetric	symmetric
#ring	double	double	single
E_{beam} (GeV)	$9(e^-)/3.1(e^+)$	$8(e^-)/3.5(e^+)$	$5.29(e^\pm)$
$\beta_{\Upsilon(4S)}$ in lab.	0.49	0.39	0
full xing angle	0 mrad	22 mrad	4.6 mrad
$\mathcal{L}_{\max} (\times 10^{33}/\text{cm}^2\text{s})$	6.6	10.6	1.25
$\int \mathcal{L} dt$ (recd. fb^{-1})	130.7	158.7	13.7
off resonance	9%	9%	1/3

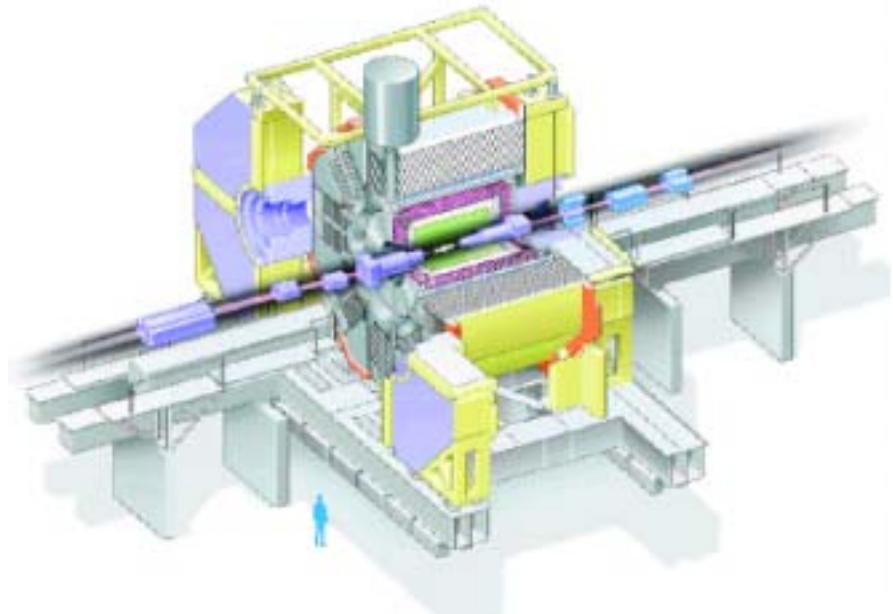
**Basic design: Vertexing(Si)-Central tracker(DC)-PID-SC coil
-EM calorimeter(CsI)-Muon system(RPC)**

BaBar detector



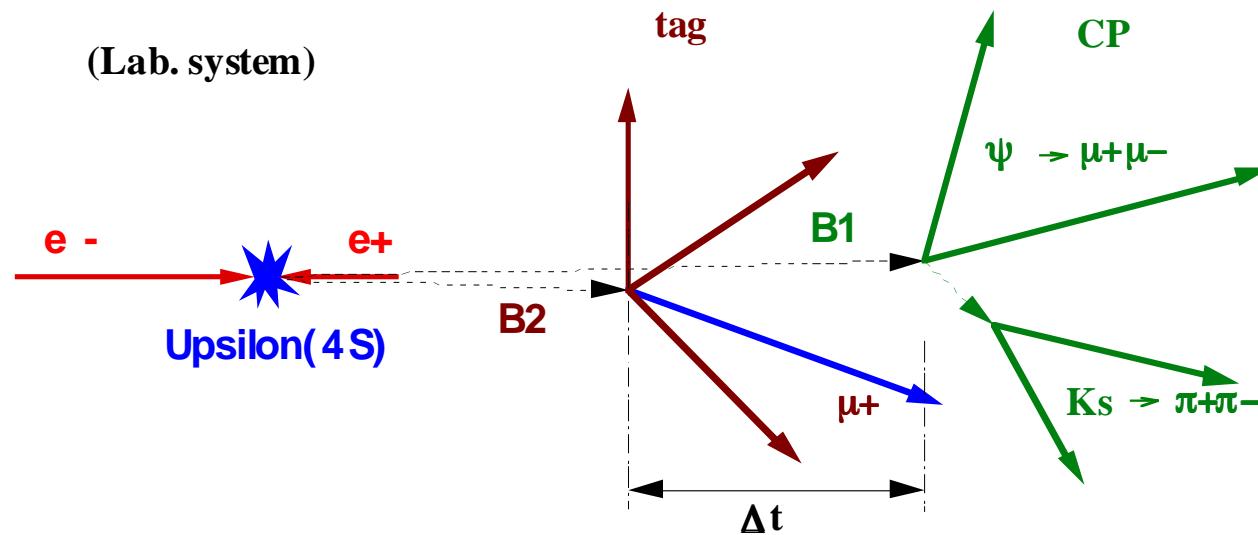
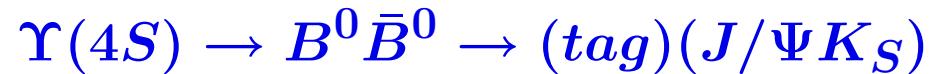
- PID=DIRC(Cerenkov)

Belle detector



- PID=Aerogel+TOF

Measurement of $\sin 2(\phi_1/\beta)$ at asym. B-factories



$$\Delta t \equiv t_{CP} - t_{tag} \sim \frac{\Delta z}{\beta \gamma c}$$

(t : decay time in the B rest frame)

CP-side Reconstruction and Flavor Tagging

Belle(78 fb⁻¹)/BaBar(82 fb⁻¹)

mode	<i>CP</i>	<i>N_{evt}</i>	purity
ΨK_S	–	1278/1144	0.96/0.96
$\Psi' K_S$	–	172/150	0.93/0.97
$\chi_{c1} K_S$	–	67/80	0.96/95
$\eta_c K_S$	–	122/132	0.71/0.73
<i>CP</i> – total		1639/1506	0.94/0.94
ΨK_L	+	1230/988	0.63/0.55
ΨK^{*0}	+/-	89/147	0.92/0.81

Flavor tagging:

lepton ($b \rightarrow \ell^- X$)

K^\pm ($b \rightarrow c \rightarrow s$)

Λ ($b \rightarrow c \rightarrow s$)

low-energy π^\pm (D^{*+})

high-energy tracks

Full B Reconstruction

(When all B decay products are detected)

$$B \rightarrow f_1 \cdots f_n$$

(In the $\Upsilon 4S$ frame)

$E_B = 5.28 \text{ GeV}$ and $|\vec{P}_B| = 0.35 \text{ GeV}/c$ are known.
Use energy-momentum conservation:

- $E_B = \sum_i^n E_i \rightarrow \Delta E \equiv E_B - E_{\text{beam}}$
- $\vec{P}_B = \sum_i^n \vec{P}_i \rightarrow M_{bc} \equiv \sqrt{E_{\text{beam}}^2 - P_B^2}$

(In the lab. frame: no need to boost)

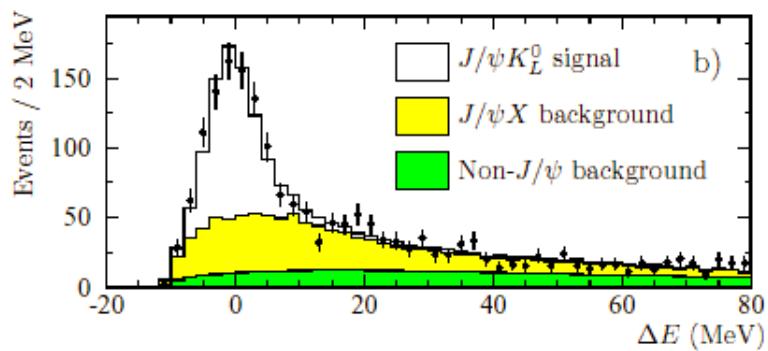
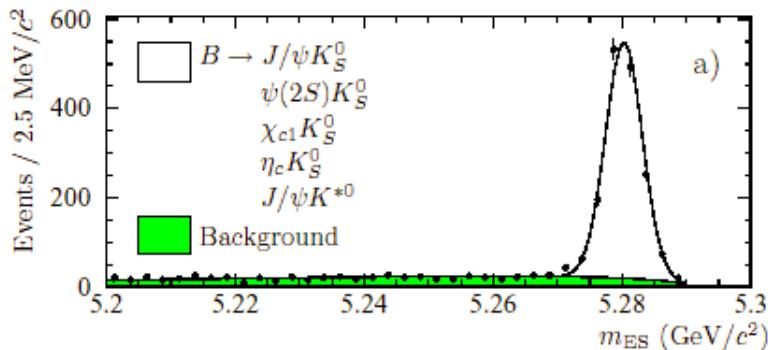
$$q_\Upsilon = (E_\Upsilon, \vec{P}_\Upsilon), \quad q_B = (E_B, \vec{P}_B)$$

- $M_{ES} = \sqrt{s/2 + \vec{P}_\Upsilon \cdot \vec{P}_B)^2/E_\Upsilon^2 - \vec{P}_B^2}$
- $\Delta E = (q_\Upsilon \cdot q_B)/\sqrt{s} - \sqrt{s}$

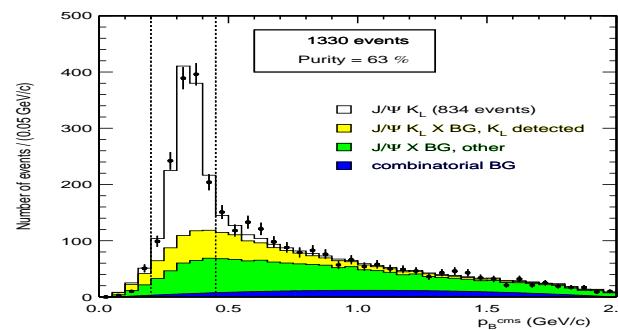
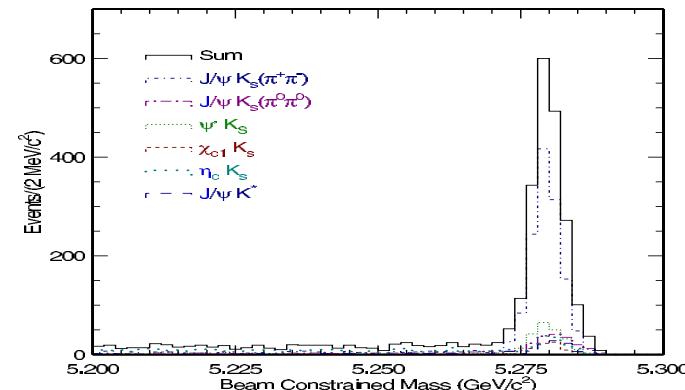
$M_{bc} = M_{ES}$ if masses are correct.

Charmonium $K_{S,L}$ Mode Reconstruction

BaBar



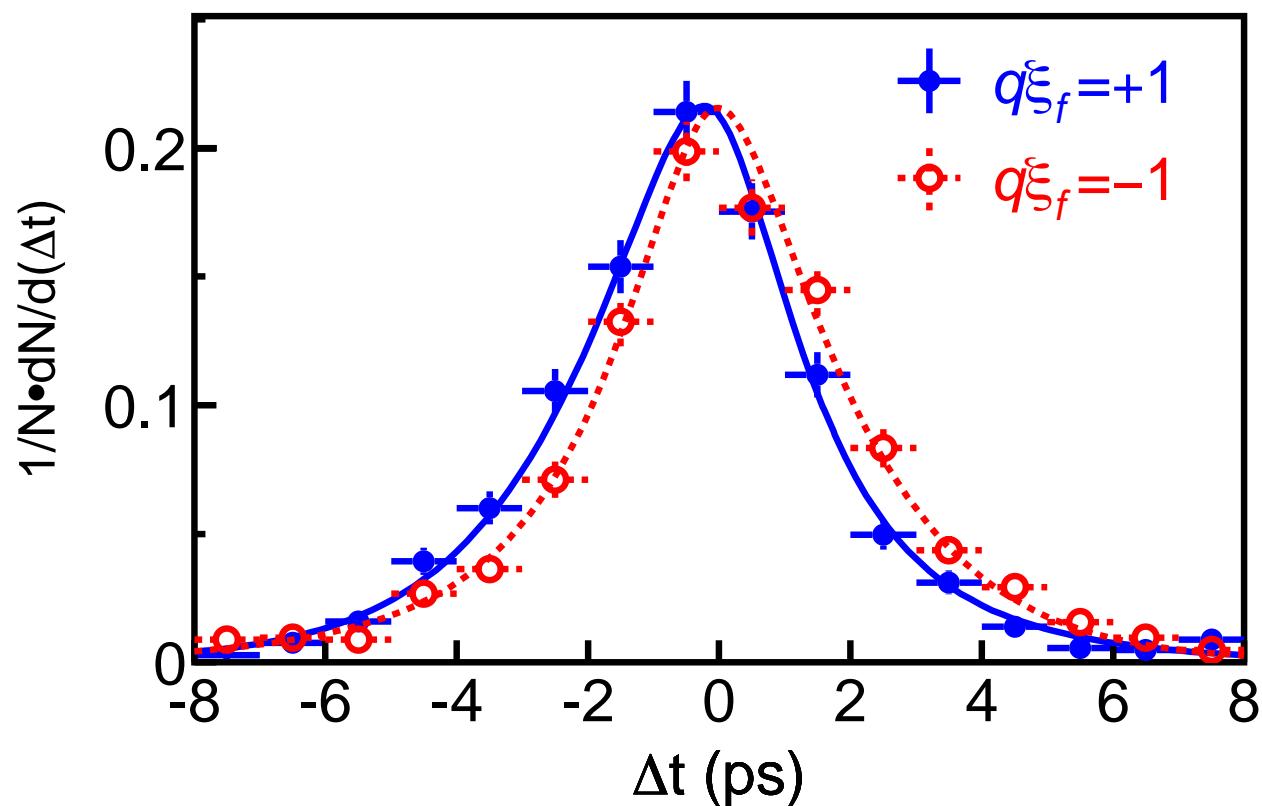
Belle



K_S modes: cut on ΔE , plot M .

K_L : only its direction measured \rightarrow either P_B or ΔE .

$q = +1$ Tag side is B^0 , ξ_f : CP eigenvalue. -1 for $J/\Psi K_S$
 $q = -1$ Tag side is \bar{B}^0 ,



We observed:

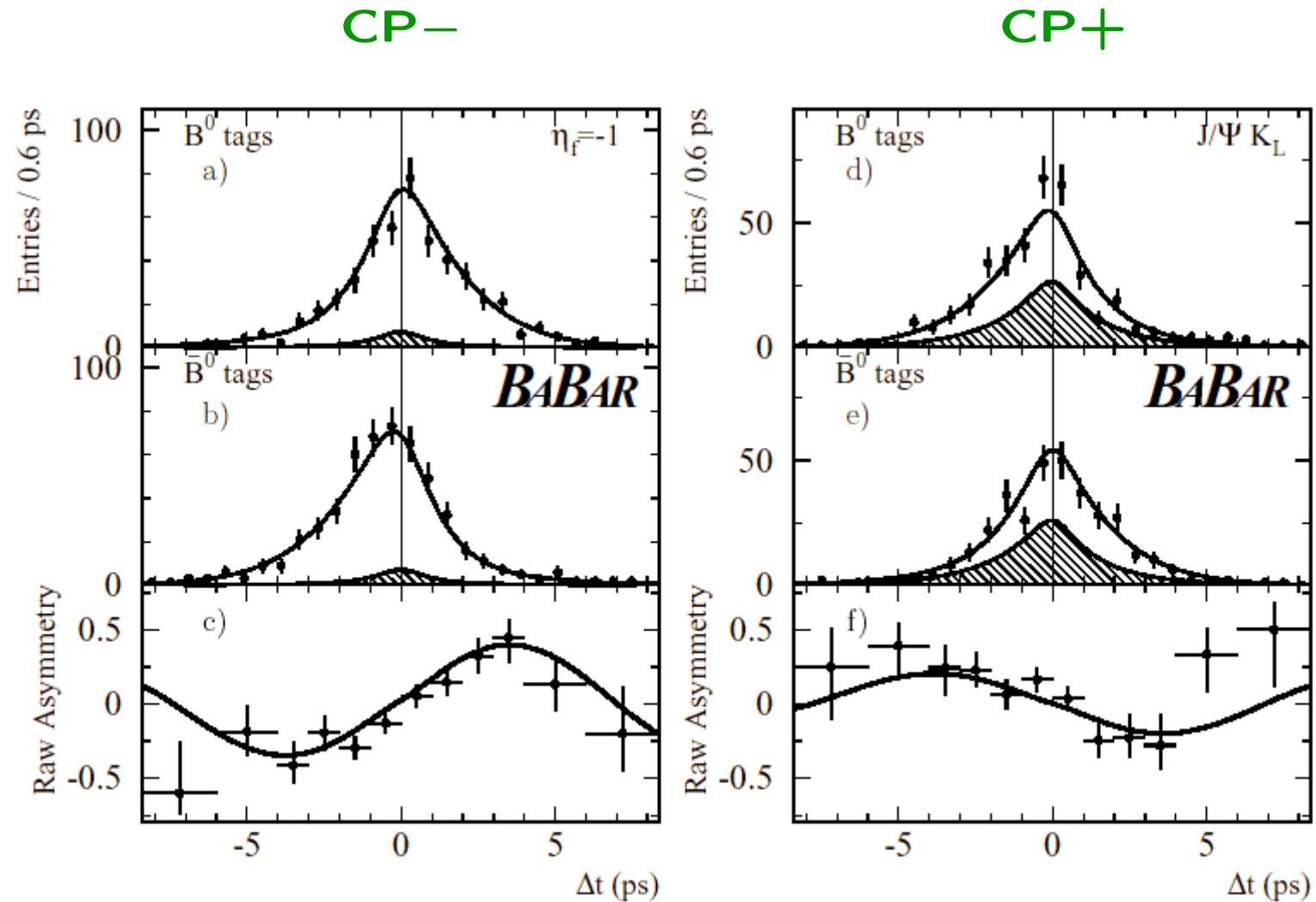
If the tagside is B^0 , the $J/\Psi K_S$ side tends to decay later than the tagside.

$CP \left\{ \begin{array}{l} \text{particle} \leftrightarrow \text{antiparticle} \\ \text{mirror inversion (no effect)} \end{array} \right.$

If the tagside is \bar{B}^0 , the $J/\Psi K_S$ side tends to decay later than the tagside.

:Inconsistent with observation.

→ CP violation



Asymmetry is opposite for CP + and -.

Single- B Evolution and Decay

Assuming CPT,

$$\begin{cases} B_H = pB^0 - q\bar{B}^0 \\ B_L = pB^0 + q\bar{B}^0 \end{cases}, \quad \begin{aligned} B_i(t) &= B_i e^{-i\omega_i t} \\ (\omega_i &= m_i + i\frac{\gamma_i}{2}) \end{aligned} \quad (i = H, L)$$

For $\gamma_H = \gamma_L \equiv \gamma$,

$$\begin{cases} B^0(t) = e^{-\frac{\gamma}{2}t} \left(B^0 \cos \frac{\delta m}{2}t + \frac{q}{p} \bar{B}^0 \sin \frac{\delta m}{2}t \right) \\ \bar{B}^0(t) = e^{-\frac{\gamma}{2}t} \left(\bar{B}^0 \cos \frac{\delta m}{2}t + \frac{p}{q} B^0 \sin \frac{\delta m}{2}t \right) \end{cases}$$

For final state f : $A \equiv A(B^0 \rightarrow f)$, $\bar{A} \equiv A(\bar{B}^0 \rightarrow f)$.

Decay distribution is given by $B^0 \rightarrow A$, $\bar{B}^0 \rightarrow \bar{A}$ and squaring:

$$\Gamma(t) \propto e^{-\gamma t} [1 + q(\textcolor{red}{A} \cos \delta m t + \textcolor{blue}{S} \sin \delta m t)]$$

$$(q = +, - \text{ for } \bar{B}^0, B^0 \text{ at } t = 0)$$

$$\textcolor{blue}{S} \equiv \frac{2 \operatorname{Im} \lambda}{|\lambda|^2 + 1}, \quad \textcolor{red}{A} \equiv \frac{|\lambda|^2 - 1}{|\lambda|^2 + 1}, \quad \lambda \equiv \frac{q \bar{A}}{p A}$$

Flavor-tagged $\Upsilon(4S) \rightarrow B^0 \bar{B}^0$

$\Upsilon(4S) \rightarrow B^0 \bar{B}^0$ is a **P-wave**. Using $B_{H.L}(t)$,

$$\Upsilon(4S) \rightarrow B^0 \bar{B}^0 - \bar{B}^0 B^0 \rightarrow e^{-i(\omega_H + \omega_L)t} (\bar{B}^0 B^0 - B^0 \bar{B}^0)$$

If tag side decays to B^0 at t_t , the other side is pure \bar{B}^0 at t_t which will then evolve/decay to f at t_s .

I.e., simply replace $t \rightarrow \Delta t \equiv t_s - t_t$ for $\Delta t > 0$:

$$\Gamma(\Delta t) \propto e^{-\gamma|\Delta t|} [1 + q(\mathbf{S} \sin \delta m \Delta t + \mathbf{A} \cos \delta m \Delta t)]$$

$$(q = +, - \text{ for } B^0, \bar{B}^0 \text{ tag })$$

If works fine for $\Delta t < 0$ by simply $\gamma \Delta t \rightarrow \gamma |\Delta t|$.

In Heisenberg picture, the state is $\Psi_{B^0} \Psi_{\bar{B}^0} - \Psi_{\bar{B}^0} \Psi_{B^0}$, where Ψ_{B^0} is a state which is purely B^0 at $t = 0$, but represents the entire evolution. Given that tagside was pure B^0 at t_t , the other side is a state which is a pure \bar{B}^0 at t_t but represents the entire evolution.

f : CP Eigenstate

In SM, we expect (phase convention: $CP|B^0\rangle = |\bar{B}^0\rangle$)

$$\frac{q}{p} = e^{-2i\phi_1} \quad \rightarrow \quad \left| \frac{q}{p} \right| = 1 \text{ (experimentally, later)}$$

$|\lambda| \neq 1$ ($A \neq 0$) means $|A(\bar{B}^0 \rightarrow f)| \neq |A(B^0 \rightarrow f)|$: (direct CPV)

If $CP|f\rangle = \xi_f|f\rangle$, and the decay is CP invariant
 $((CP)S(CP)^\dagger = S)$,

$$\lambda = \frac{\frac{q}{p}}{e^{-2i\phi_1}} \frac{\langle f | S | \bar{B}^0 \rangle}{\underbrace{\langle f | (CP)^\dagger}_{\xi_f^* \langle f |} \underbrace{(CP)S(CP)^\dagger}_{S} \underbrace{\langle CP | \bar{B}^0 \rangle}_{|\bar{B}^0\rangle}} = e^{-2i\phi_1} \xi_f$$

With $A = 0$,

$$\Gamma(\Delta t) \propto e^{-\gamma|\Delta t|} (1 + qS \sin \delta m \Delta t), \quad S = -\xi_f \sin 2\phi_1$$

Results on Charmonium X_s Analyses

S : $\Delta t \leftrightarrow -\Delta t$ asymmetry

A : $q+ \leftrightarrow q-$ area asymmetry

$$\sin 2(\phi_1/\beta) = \begin{cases} 0.719 \pm 0.074(\text{stat}) \pm 0.035(\text{sys}) & (\text{Belle}) \\ 0.741 \pm 0.067(\text{stat}) \pm 0.034(\text{sys}) & (\text{BaBar}) \end{cases}$$

(HFAG average) $\sin 2(\phi_1/\beta) = 0.734 \pm 0.055$

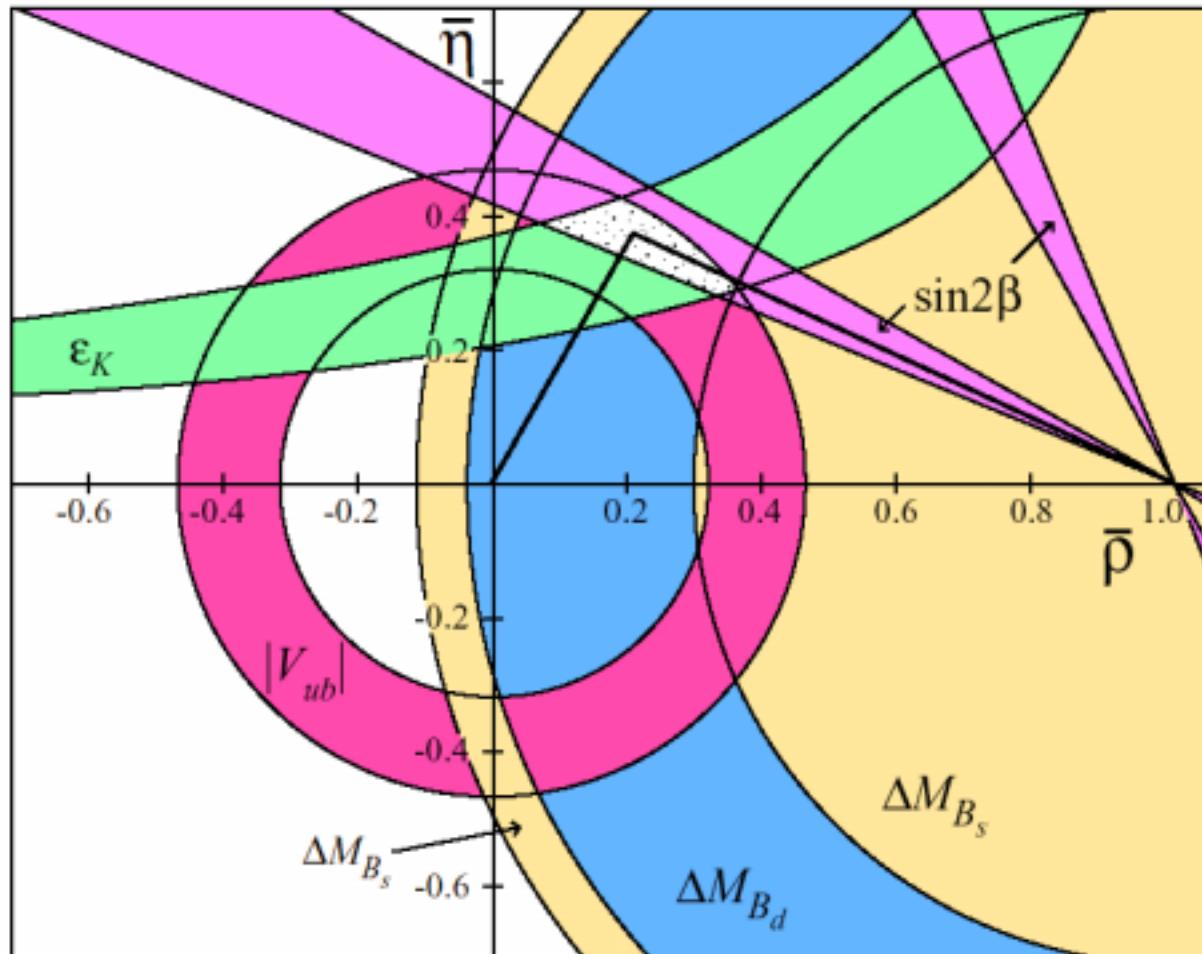
Direct CPV (Belle, BaBar combined)

$$A_{\text{Belle}} (\equiv -C_{\text{BaBar}}) = -0.052 \pm 0.047$$

No indication of direct CPV.

(Belle result to be updated for 140 fb^{-1} at LP03)

PDG2002 updated



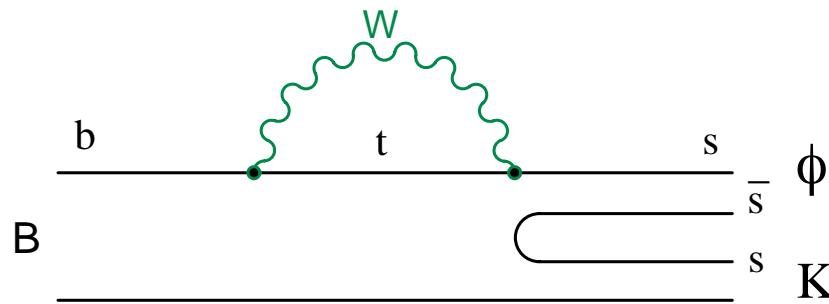
All regions cross at one point!

Time-dependent CPV of $b \rightarrow s$ penguin modes

$$\bar{B}^0 \rightarrow \begin{cases} \phi K_S \\ K^+ K^- K_S (\text{no } \phi, D0, \chi_{c0}) \\ \eta' K_s \end{cases}$$

In SM, expect $S \sim -\xi_f \sin 2\phi_1$, $A \sim 0$

Deviation therefrom \rightarrow new physics in $b \rightarrow s$
(e.g. the W-loop replaced by a charged Higgs loop)

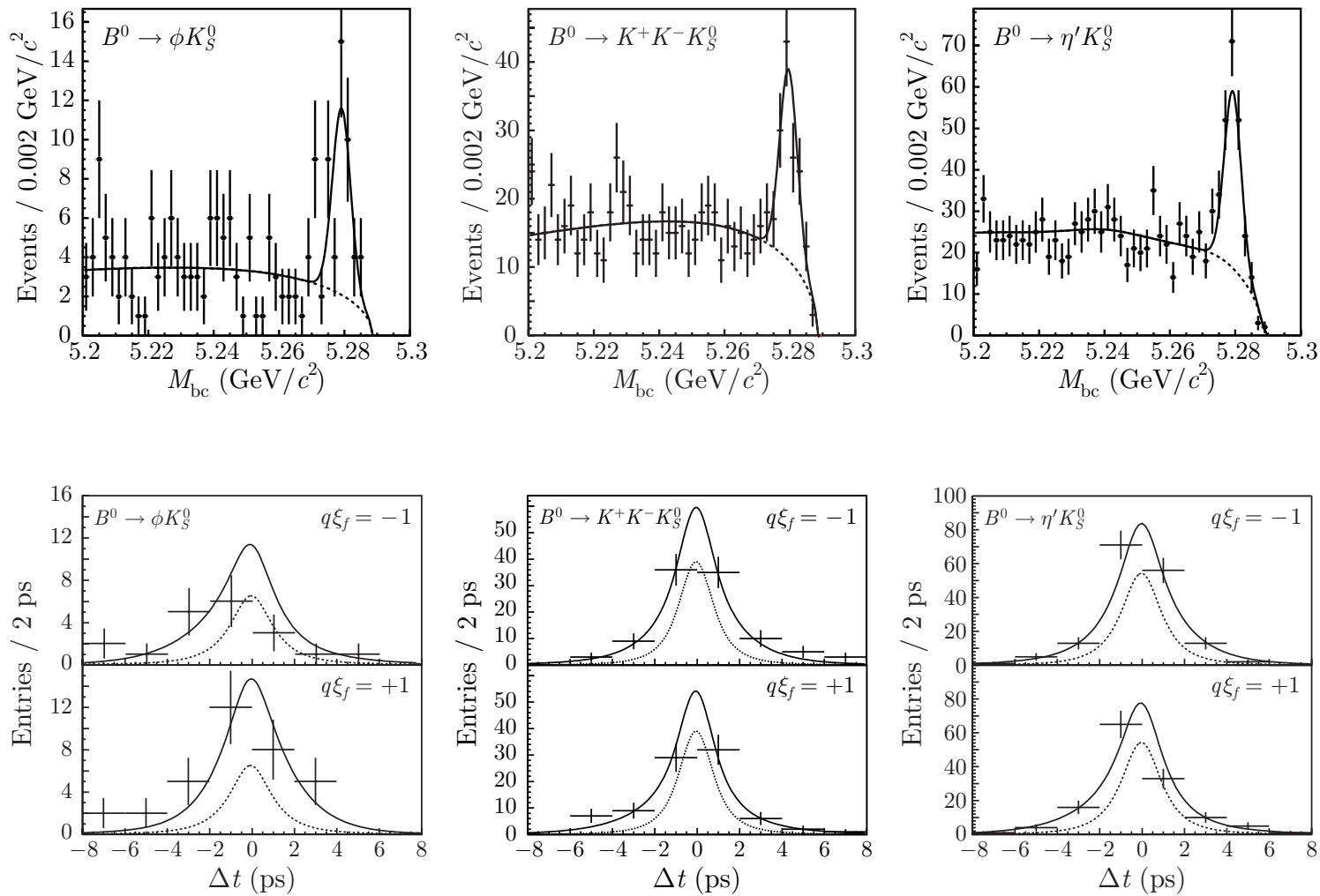


Continuum Suppression

Most rare modes: background is dominated by continuum $e^+e^- \rightarrow q\bar{q}$ 2-jet events.

- Event shape variables: Fox-Wolfram R_l , thrust, etc.
continuum: skinny, $B\bar{B}$: spherical.
- Angle(B candidate axis, axis of the rest)
continuum: aligned, $B\bar{B}$: uniform.
- Angle(B , beam)
continuum: $1 + \cos^2 \theta$, B : $\sin^2 \theta$.
- Fisher: $F = \sum_i c_i X_i$ (above+ X_i energy flow etc.)
Adjust c_i to maximize the separation.

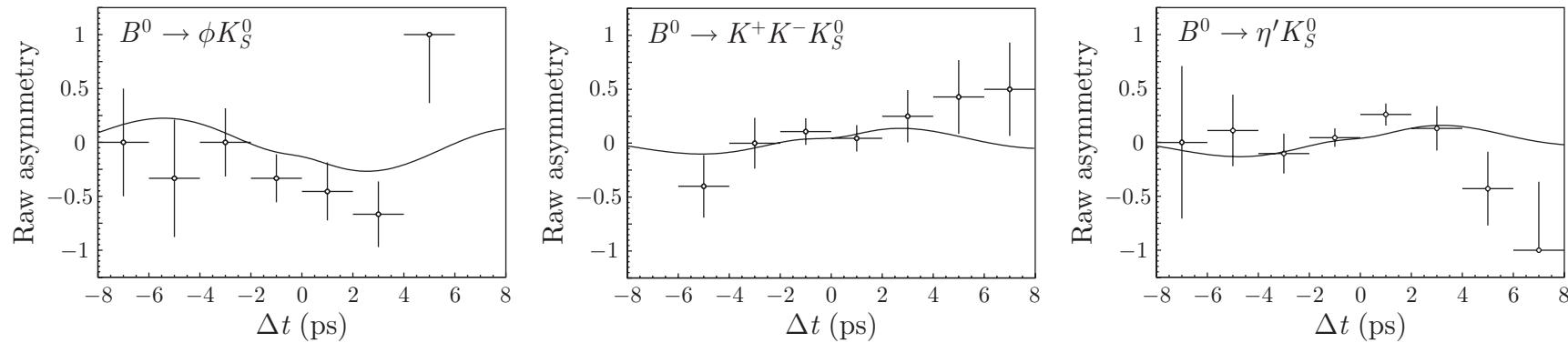
Belle (78 fb^{-1})



Belle $b \rightarrow s$ Penguins

$$A_{cp}(\Delta t) = d(S \sin \delta m \Delta t + A \cos \delta m \Delta t)$$

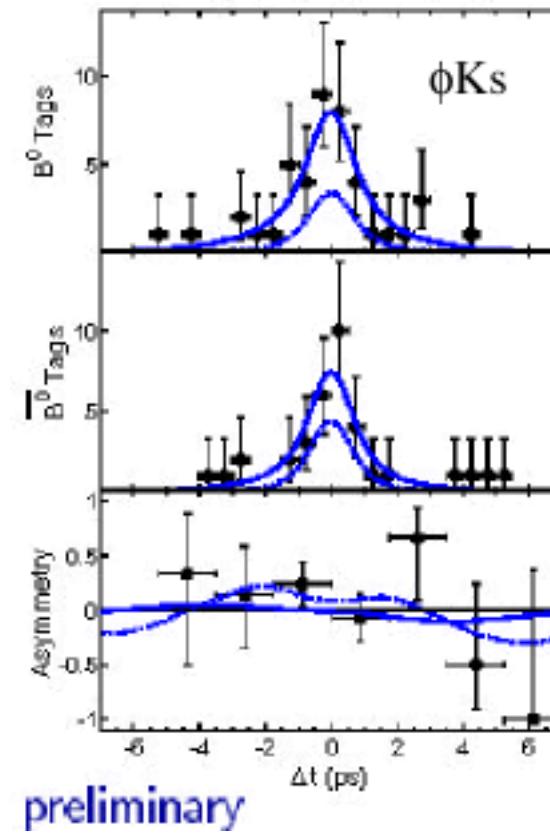
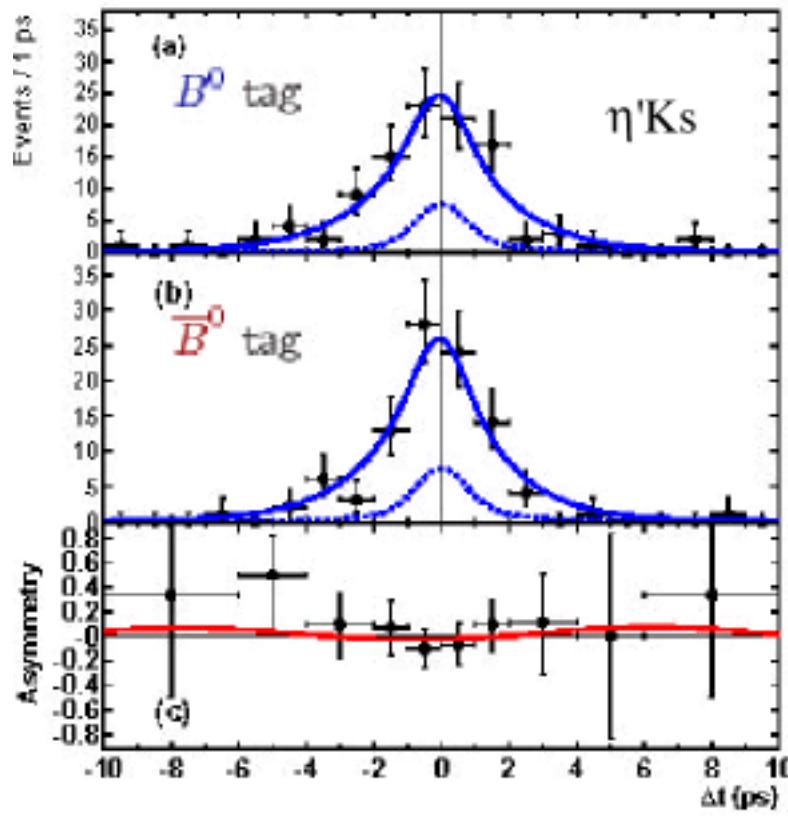
Plot $-\xi_f A_{cp}$:



(78fb^{-1})	"sin 2 ϕ_1 "($-\xi_f S$)	A
ϕK_S	$-0.73 \pm 0.64 \pm 0.22$	$-0.56 \pm 0.41 \pm 0.16$
$K^+ K^- K_S$ (non res.)	$+0.49 \pm 0.43 \pm 0.11^{+0.33}_{-0}$	$-0.40 \pm 0.33 \pm 0.10^{+0}_{-0.26}$
$\eta' K_S$	$+0.71 \pm 0.37^{+0.05}_{-0.06}$	$+0.26 \pm 0.22 \pm 0.03$
$J/\Psi K_{S/L}$ etc.	0.735 ± 0.055	-0.052 ± 0.047

$CP(K^+ K^- K_S) = +$ mostly (the last sys errors).

BaBar $b \rightarrow s$ Penguins



$$S_{\eta' K_S} = 0.02 \pm 0.34 \pm 0.03$$

$$C_{\eta' K_S} = 0.10 \pm 0.22 \pm 0.03$$

$$S_{\phi K_S} = -0.18 \pm 0.51 \pm 0.07$$

$$C_{\phi K_S} = -0.80 \pm 0.38 \pm 0.12$$

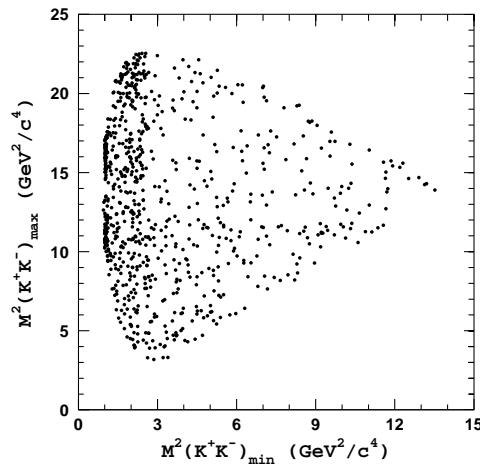
$S_{\eta' K_S} = S_{\phi K_S} = \text{"sin } 2\beta\text{"}$

CP content of $K^+K^-K_S$ (Belle)

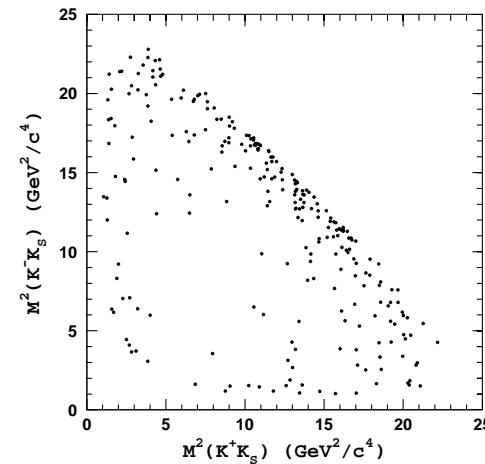
(Belle 79 fb^{-1})

	Signal yield (evts)	$\mathcal{B}(90\% \text{ U.L.})(\times 10^{-6})$
$K^+K^-K^+$	565 ± 30	$33.0 \pm 1.8 \pm 3.2$
$K^0K^+K^-$	149 ± 15	$29.0 \pm 3.4 \pm 4.1$
$K_SK_SK^+$	66.5 ± 9.3	$13.4 \pm 1.9 \pm 1.5$
$K_SK_SK_S$	$12.2^{+4.5}_{-3.8}$	$4.3^{+1.6}_{-1.4} \pm 0.75$
$K^+K^-\pi^+$	93.7 ± 23.2	$9.3 \pm 2.3 (< 13)$
$K^0K^-\pi^+$	26.8 ± 16.6	$8.4 \pm 5.2 (< 15)$

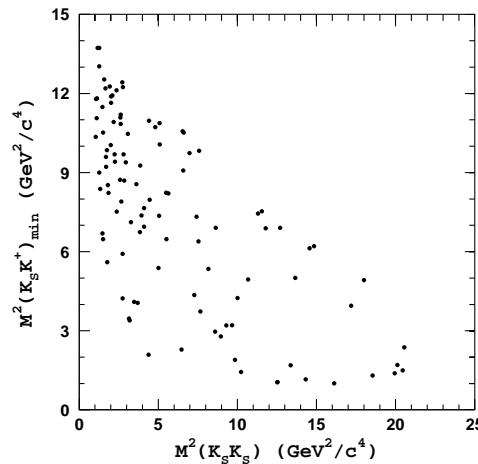
$K^+K^-K^+$



$K_SK^+K^-$



$K_SK_SK^+$



$(K^+K^-)K_S$ system:

- $L_{(K^+K^-)-K_S} = L_{K^+-K^-} \equiv L$ (B is spinless)
- $CP(K^+K^-) = +$ (any L , since $C = P$)
- $CP(K^+K^-K_S) = \underbrace{CP(K^+K^-)}_+ \underbrace{CP(K_S)(-)^L}_+ = (-)^L$

Even/odd $L_{K^+-K^-} \rightarrow$ even/odd $CP(K^+K^-K_S)$

On the other hand,

Expect $B \rightarrow K\bar{K}K$ to be dominated by $b \rightarrow s$ penguin. In fact:
since no $b \rightarrow s$ penguin (odd s/\bar{s}) in $K\bar{K}\pi$ (even s/\bar{s}),

$$F \equiv \frac{\Gamma_{b \rightarrow u}^{3K}}{\Gamma_{\text{total}}^{3K}} \sim \frac{\mathcal{B}(K^+K^-\pi^+)}{\mathcal{B}(K^+K^-K^+)} \left(\frac{f_K}{f_\pi} \right)^2 \tan^2 \theta_c = 0.022 \pm 0.005$$

($F = 0.023 \pm 0.013$ using $K_SK^-\pi^+$ and $K_SK^-K^+$)

We can assume $3K$ modes are 100% due to $b \rightarrow s$ penguin.

Then,

$$\bar{B}^0(b\bar{d}) \rightarrow \begin{pmatrix} s \\ \bar{d} \end{pmatrix} + \begin{pmatrix} s\bar{s} \\ u\bar{u} \end{pmatrix} \rightarrow \begin{matrix} K^-(s\bar{u}) & K^+(\bar{s}u) \\ \bar{K}^0(s\bar{d}) & \end{matrix}$$

$u \leftrightarrow d, \bar{u} \leftrightarrow \bar{d}$ everywhere
 ↓
 (isospin)

$$B^-(b\bar{u}) \rightarrow \begin{pmatrix} s \\ \bar{u} \end{pmatrix} + \begin{pmatrix} s\bar{s} \\ d\bar{d} \end{pmatrix} \rightarrow \begin{matrix} \bar{K}^0(s\bar{d}) & K^0(\bar{s}d) \\ K^-(s\bar{u}) & \end{matrix}$$

$\bar{B}^0 \rightarrow K^+ K^- \bar{K}^0$ and $B^- \rightarrow \bar{K}^0 K^0 K^-$ have the same rate and the same kinematic configuration.

also : $(\bar{K}^0 K^0)_{L\text{even}} \rightarrow K_S K_S, K_L K_L, \quad (\bar{K}^0 K^0)_{L\text{odd}} \rightarrow K_S K_L.$

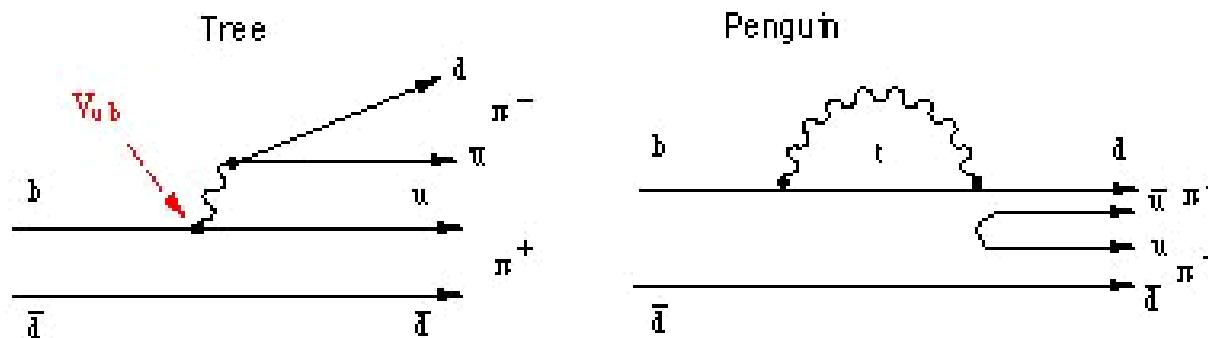
$$\begin{aligned}
 \frac{CP(K^+ K^- \bar{K}^0)_{+}}{CP(K^+ K^- \bar{K}^0)_{\text{any}}} &= \frac{K^+ K^- \bar{K}^0(L_{K^+ K^- \text{even}})}{K^+ K^- \bar{K}^0(L_{K^+ K^- \text{any}})} = \frac{\bar{K}^0 K^0 K^-(L_{\bar{K}^0 K^0 \text{even}})}{\bar{K}^0 K^0 K^-(L_{\bar{K}^0 K^0 \text{any}})} \\
 &= \frac{2(K_S K_S K^-)}{(K^+ K^- \bar{K}^0)} = \begin{cases} 0.86 \pm 0.15 \pm 0.05 & (\text{incl. } \phi K_S) \\ 1.04 \pm 0.19 \pm 0.06 & (\phi K_S \text{ removed}) \end{cases}
 \end{aligned}$$

Time-dependent CPV analysis of $\pi^+\pi^-$

$$\frac{d\Gamma}{d\Delta t} \propto e^{-\frac{|\Delta t|}{\tau_B}} [1 + q(S_{\pi\pi} \sin \delta m \Delta t + A_{\pi\pi} \cos \delta m \Delta t)]$$

$$S_{\pi\pi} = \frac{\text{Im}\lambda}{|\lambda|^2 + 1}, \quad A_{\pi\pi} = -C_{\pi\pi} = \frac{|\lambda|^2 - 1}{|\lambda|^2 + 1}.$$

$$|S_{\pi\pi}|^2 + |C_{\pi\pi}|^2 \leq 1$$

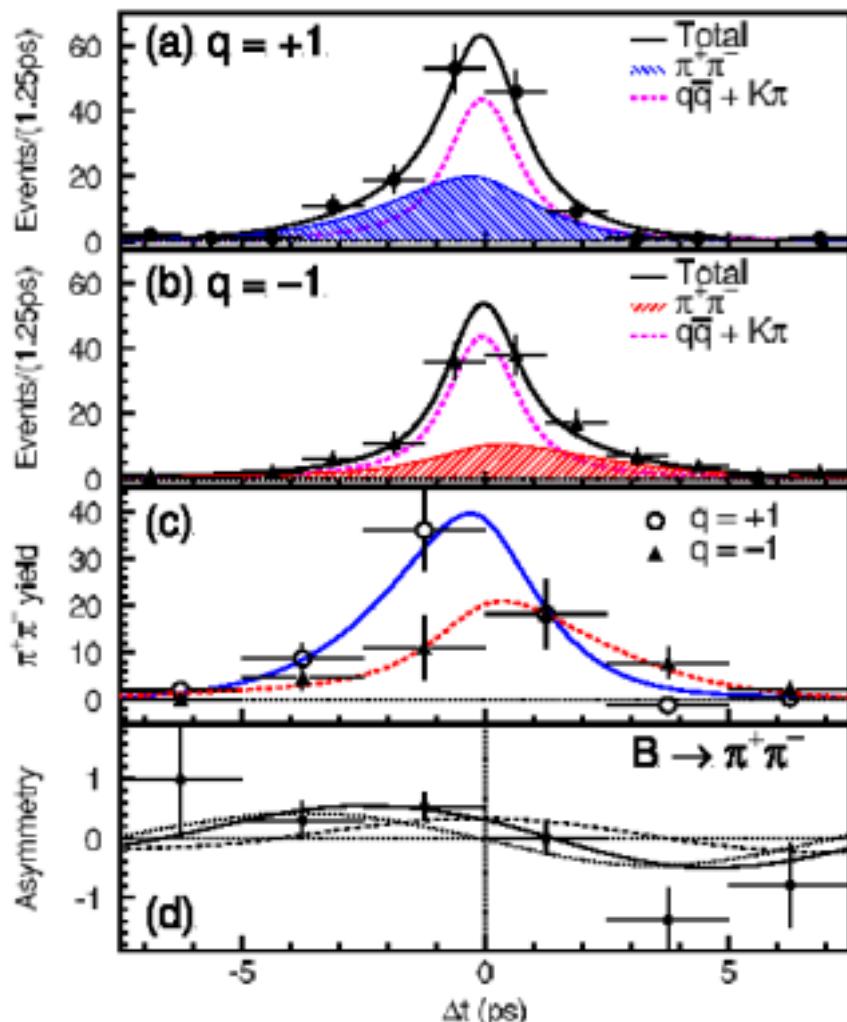


Expect:

$S_{\pi\pi} = \sin 2(\phi_2/\alpha)$ IF SM no penguin pollution
 $A_{\pi\pi} = 0$ IF no direct CPV

Belle $\pi^+\pi^- \Delta t$ Fit

Belle (78 fb^{-1})



- Use the same flavor tagging as the ϕ_1 analysis.
- Unbinned likelihood fit for Δt distribution.
- $K^-\pi^+$ asymmetry known (~ 0).
→ Its shape is known.
- $(q+ \text{area}) > (q- \text{area}) \rightarrow A_{\pi\pi} > 0$.
- Left-right asymmetry → $S_{\pi\pi}$.
(opposite signs for $q\pm$)

$$S_{\pi\pi} = -1.23 \pm 0.41^{+0.08}_{-0.07}$$

$$A_{\pi\pi} = +0.77 \pm 0.27 \pm 0.08$$

Statistical errors estimated by 'pseudo experiments' (Gives more conservative errors in general than the fit output.)

Belle $\pi^+\pi^-$ Result

CPV ($S_{\pi\pi}, A_{\pi\pi}$) at 3.4σ .
Direct CPV ($A_{\pi\pi}$) at 2.2σ .

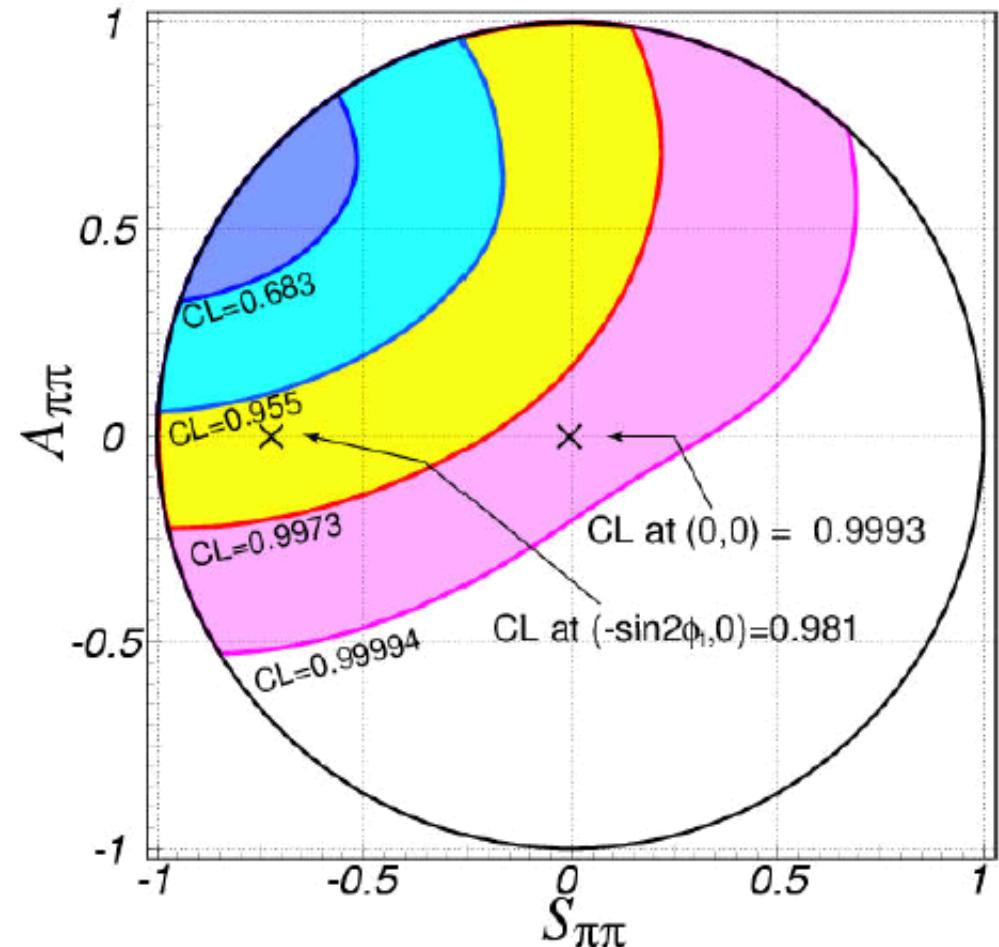
$$\lambda = e^{-2i\phi_2} \frac{1 + |P/T|e^{i(\delta + \phi_3)}}{1 + |P/T|e^{i(\delta - \phi_3)}}$$

Assuming, $\phi_3 = \pi - \phi_1 - \phi_2$,
 $\phi_1 = 23.5^\circ$ (Belle, BaBar), and
 $|P/T| = 0.15 \sim 0.45$ (th. av. ~ 0.3)
fit for ϕ_2 and δ :

$$\rightarrow 78 < \phi_2 < 152^\circ$$

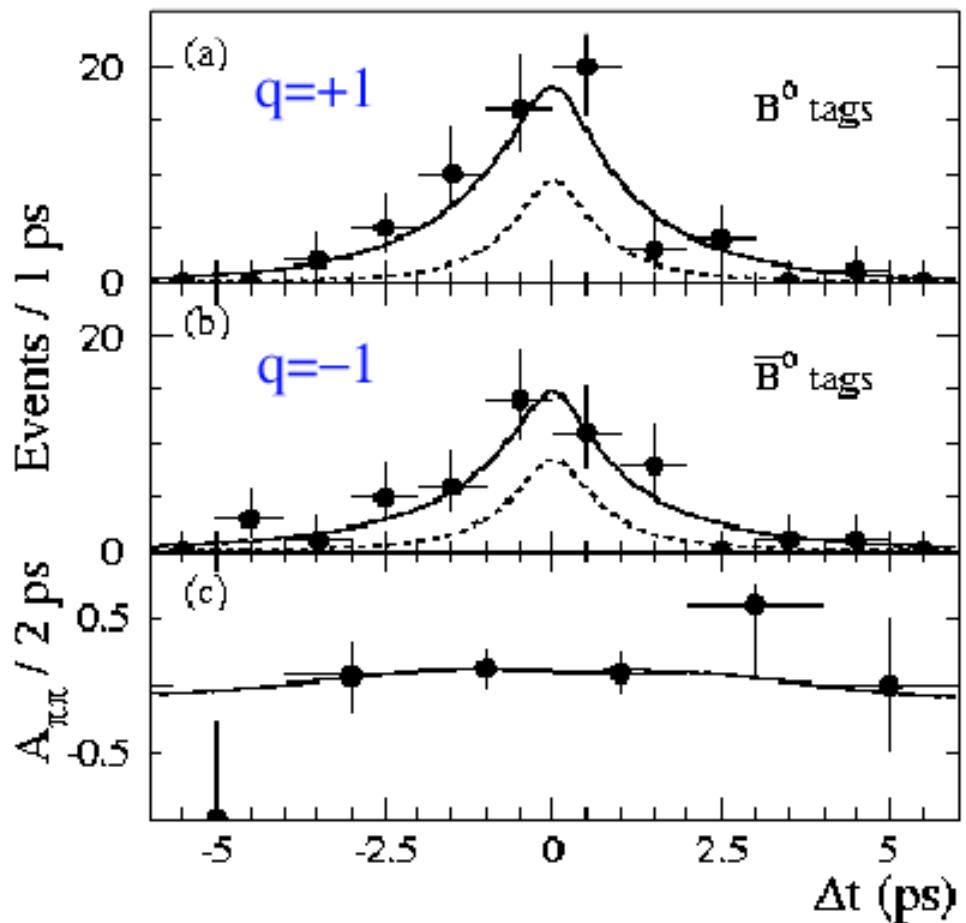
$\delta \sim -100^\circ$: large strong phase

Feldman-Cousin



BaBar $\pi^+\pi^- \Delta t$ Analysis

BaBar (81 fb^{-1})



$$S_{\pi\pi} = 0.02 \pm 0.34 \pm 0.05$$
$$C_{\pi\pi} = -0.30 \pm 0.25 \pm 0.04$$

No indication of CPV
(indirect or direct).

$\rho^\pm\pi^\mp$ Δt Analyses (BaBar)

Two final states :

$\rho^+\pi^-$ and $\rho^-\pi^+ \rightarrow (S, C)$ for each.

Total integrated yield asymmetry A :

$\rho^+\pi^- \leftrightarrow \rho^-\pi^+$ (regardless of tag)

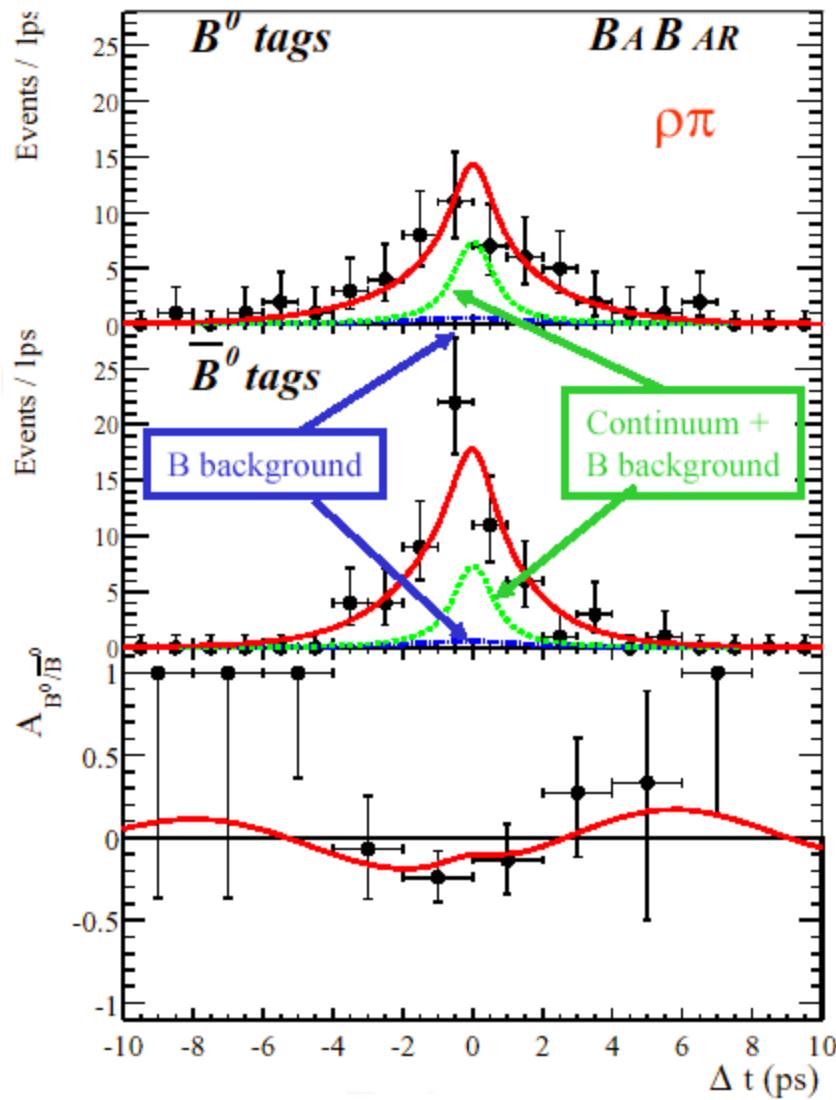
(different from A_{CP} or from $A(\text{Belle}) = -C(\text{BaBar})$)

Parametrize as

$$f_{\rho^\pm}(\Delta t) = (1 \pm \textcolor{magenta}{A}) e^{-\frac{\Delta t}{\tau_B}} [1 + q \{(S \pm \Delta S) \sin \delta m t - (\textcolor{red}{C} \pm \Delta C) \cos \delta m t\}]$$

$\rho^\pm\pi^\mp$ Results (BaBar)

BaBar (81 fb^{-1})



$$A_{\rho\pi} = -0.18 \pm 0.08 \pm 0.03$$

$$\begin{aligned} S_{\rho\pi} &= 0.19 \pm 0.24 \pm 0.03 \\ \Delta S_{\rho\pi} &= 0.15 \pm 0.25 \pm 0.03 \end{aligned}$$

$$\begin{aligned} C_{\rho\pi} &= 0.36 \pm 0.18 \pm 0.04 \\ \Delta C_{\rho\pi} &= 0.28 \pm 0.18 \pm 0.04 \end{aligned}$$

From all these, one can extract usual A_{CP} :

$$\begin{aligned} A_{CP}(\bar{B}^0 \rightarrow \rho^+ \pi^-) &= -0.62^{+0.24}_{-0.28} \pm 0.06 \\ A_{CP}(\bar{B}^0 \rightarrow \rho^- \pi^+) &= -0.11^{+0.16}_{-0.17} \pm 0.04 \end{aligned}$$

Slightly more than 2σ of DCPV.

$D^{(*)}\pi$, Δt Analyses ($2\beta + \gamma$, BaBar)

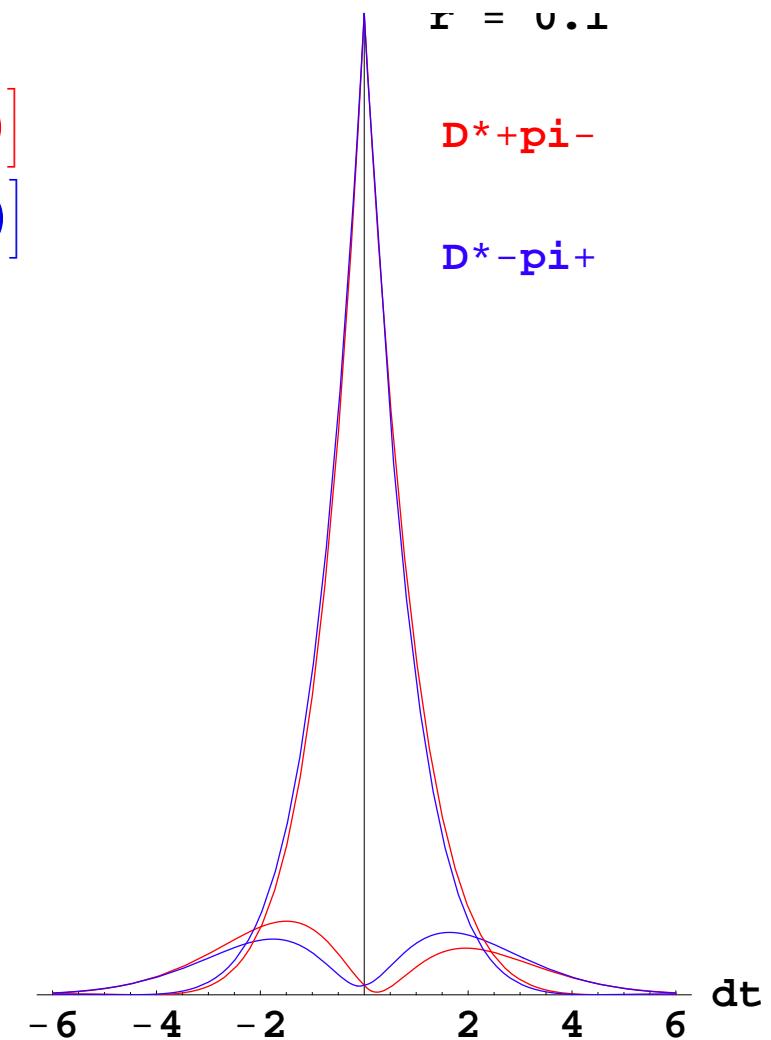
$$D^+\pi^- \propto e^{-\gamma\Delta t} [1 + q(C \cos \delta m t - S^+ \sin \delta m t)]$$

$$D^-\pi^+ \propto e^{-\gamma\Delta t} [1 - q(C \cos \delta m t - S^- \sin \delta m t)]$$

$$C \sim 1, \quad S^\pm \sim 2r \sin(2\beta + \gamma \pm \delta)$$

$$r = \frac{|A(B^0 \rightarrow D^+\pi^-)|}{|A(\bar{B}^0 \rightarrow D^+\pi^-)|} \quad (\text{expect } \sim 0.02)$$

- Most of the info on mixed modes.
Dip location + height asymmetry.
- Existense of negative Δt is advantageous (vs hadron machines)

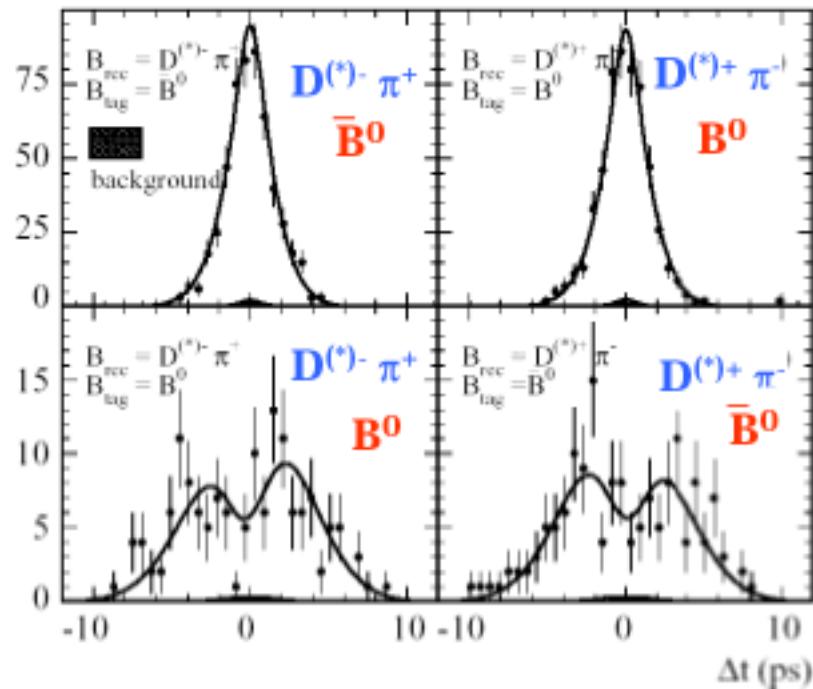


$D^{(*)}\pi$ Δt Distributions (BaBar)

Full reconstruction

$D^+\pi^-$ (5207 evs)

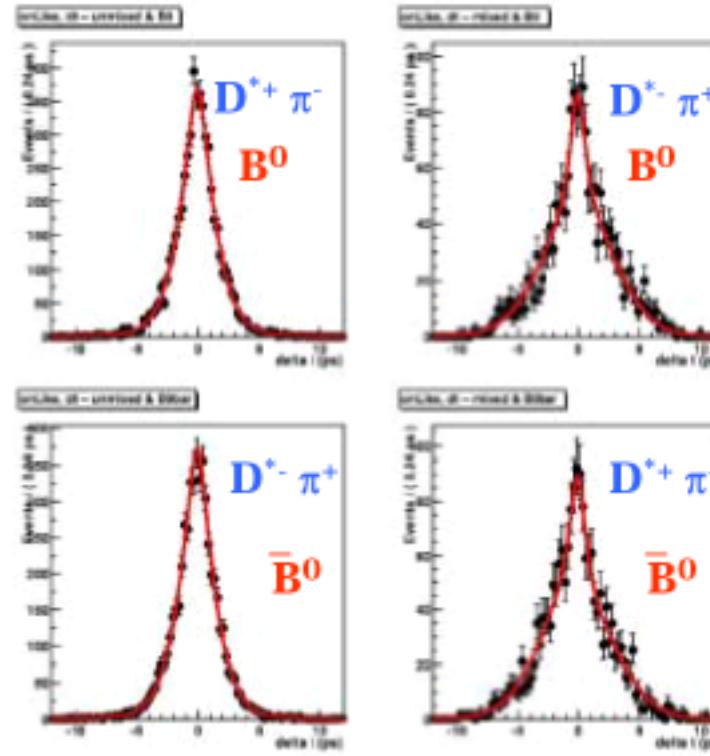
$D^{*+}\pi^-$ (4746 evs).



Partial reconstruction.

$D^{*+}\pi^-$,

$D^{*+} \rightarrow (D^0)\pi^+$.



Tag: lepton+K. lepton tags are shown.

$D^{(*)}\pi$ Results (BaBar)

Include tag-side $b \rightarrow u$ interference (K-tag only):

$$q2r \sin(2\beta + \gamma - \delta) + 2r' \sin(2\beta + \gamma + q\delta')$$

Same order as the original CPV effect.

Partial $D^*\pi$:

$$2r_* \sin(2\beta + \gamma) \cos \delta_* = -0.063 \pm 0.024 \pm 0.017$$

$$2r_* \cos(2\beta + \gamma) \sin \delta_* = -0.004 \pm 0.037 \pm 0.020$$

Full $D^{(*)}\pi$:

$$2r \sin(2\beta + \gamma) \cos \delta = -0.022 \pm 0.038 \pm 0.021$$

$$2r \cos(2\beta + \gamma) \sin \delta = 0.025 \pm 0.068 \pm 0.035$$

$$2r_* \sin(2\beta + \gamma) \cos \delta_* = -0.068 \pm 0.038 \pm 0.021$$

$$2r_* \cos(2\beta + \gamma) \sin \delta_* = 0.031 \pm 0.070 \pm 0.035$$

Implication of $D^{(*)}\pi$ Analysis on γ (BaBar)

BaBar result on $Br(D_s^{(*)+}\pi^-)$ + SU(3)

$$r = 0.021^{+0.004}_{-0.005}, \quad r_* = 0.017^{+0.005}_{-0.007}.$$

Fit $\sin(2\beta + \gamma)$ and δ, δ_* :

$$\sin(2\beta + \gamma) > 0.76 \quad (90\% \text{ C.L.})$$

Note: with $\sin 2\beta = 0.735$

$\sin(2\beta + \gamma) > 0.76$ means $-3^\circ < \gamma < 97^\circ$

$B \rightarrow DK$ for ϕ_3/γ

$B^- \rightarrow D_{CP} K^-$

Interference of

$B^- \rightarrow D^0 K^- / B^- \rightarrow \bar{D}^0 K^-$

$$r \equiv \frac{|B|}{|A|} = 0.1-0.2$$

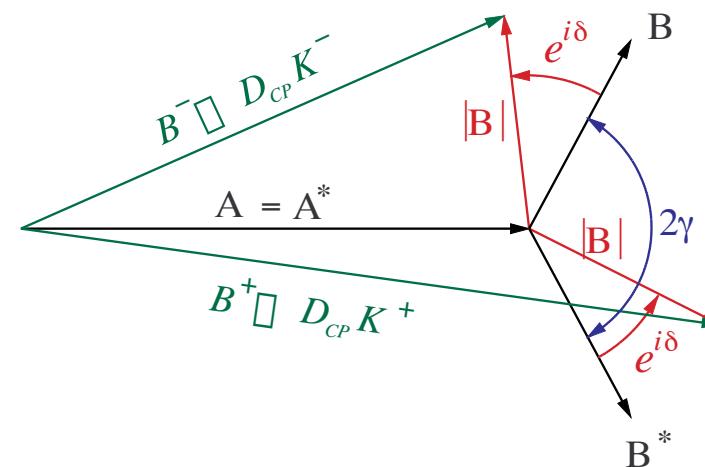
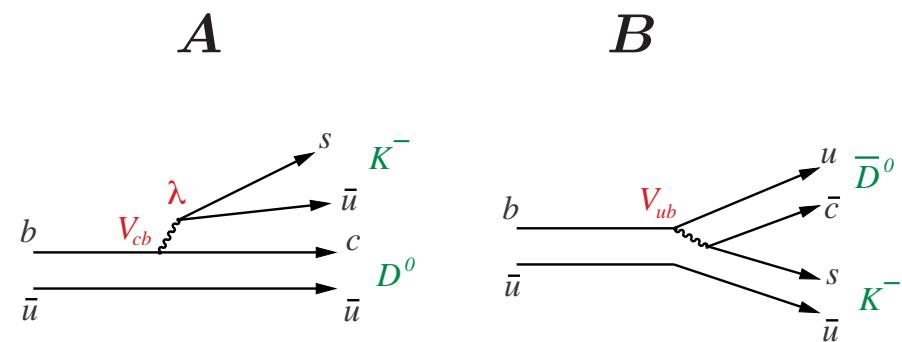
$\sim 10\%$ asymmetry expected.

Depends on strong phase δ .

$c = 1$ in final state

→ no penguin pollution.

Eventually extract γ .



$$B^\pm \rightarrow D_{CP} K^\pm \text{ (Belle 78 fb}^{-1}\text{)}$$

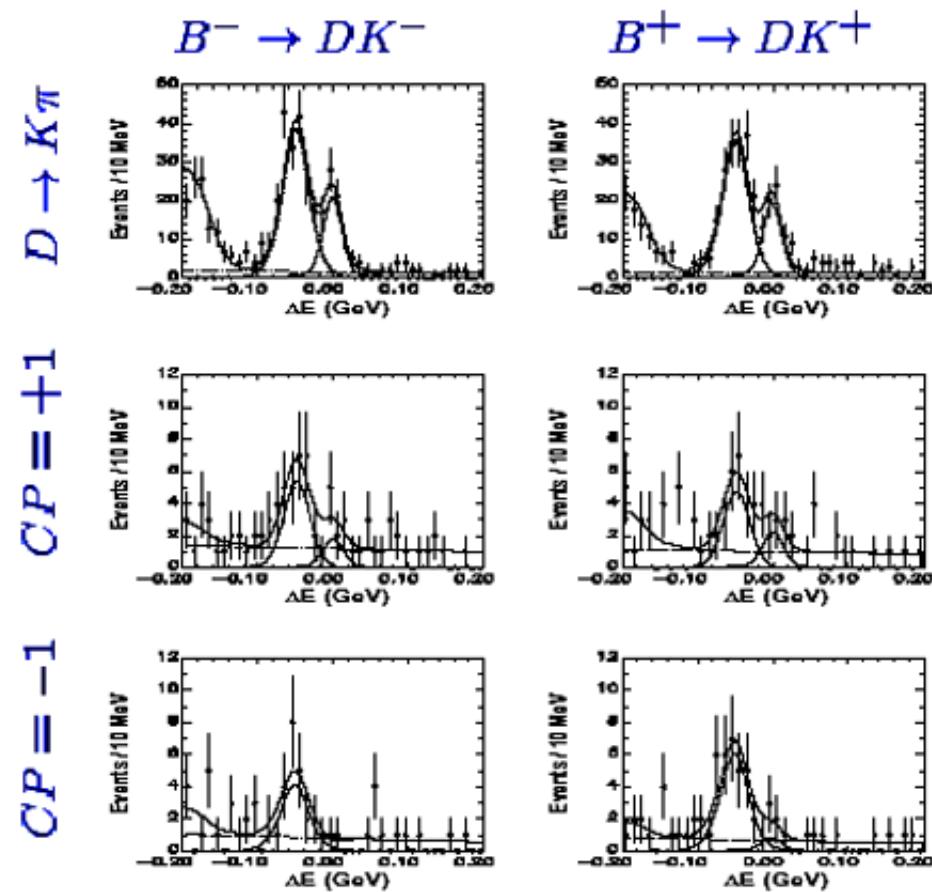
$D^0 h^-$: assign π mass to h^- .
Signal at $\Delta E = -49$ MeV.

$$D^0 : K^-\pi^+$$

$$\text{CP+ } (D_1) : \\ K^+K^-, \pi^+\pi^-$$

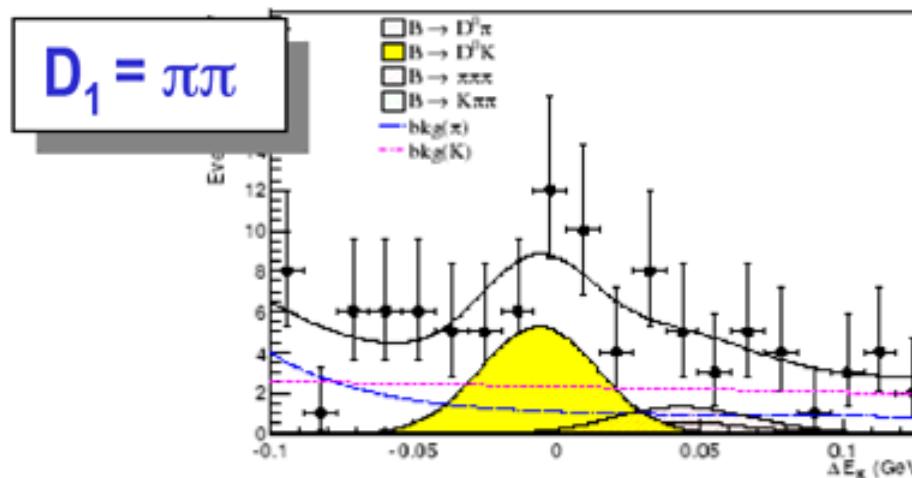
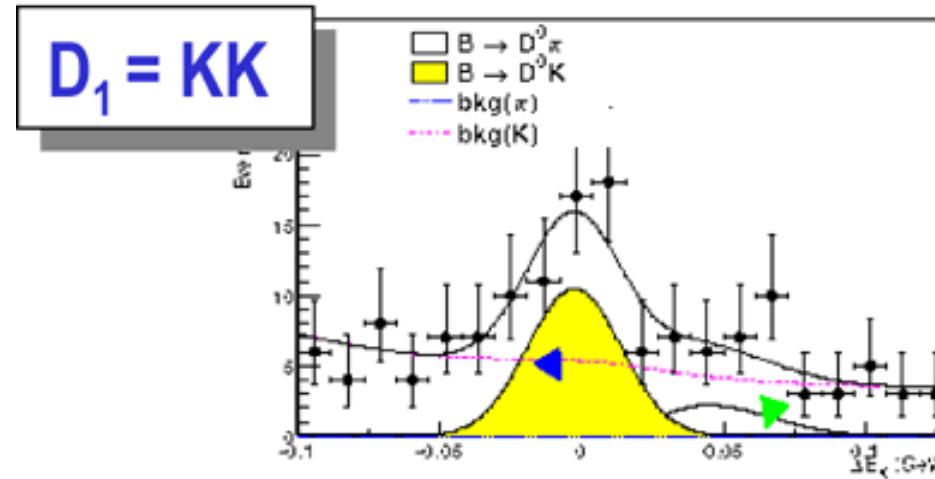
$$\text{CP- } (D_2) : \\ K_S\pi^0, K_S\omega, K_S\eta, K_S\eta'$$

PID (π/K separation) important.



$B^- \rightarrow D_{CP} K^-$ (**BaBar** 81.2 fb $^{-1}$)

$B^\pm \rightarrow D_I K^\pm$



$\Delta E(\text{GeV})$

$B^- \rightarrow D_{CP} K^-$ Parameters

Rate asymmetry :

$$A_{1/2} = \frac{\mathcal{B}(B^- \rightarrow D_i K^-) - \mathcal{B}(B^+ \rightarrow D_i K^+)}{\mathcal{B}(B^- \rightarrow D_i K^-) + \mathcal{B}(B^+ \rightarrow D_i K^+)} = \frac{\pm 2r \sin \phi_3 \sin \delta}{1 + r^2 \pm 2r \cos \phi_3 \cos \delta}$$

Ratio of Cabibbo suppression factors, D_i vs D^0 :

$$R_i = \frac{CS_{D_i}}{CS_{D^0}} \quad (i = 1, 2), \quad CS_X = \frac{\Gamma(B^- \rightarrow XK^-) + c.c.}{\Gamma(B^- \rightarrow X\pi^-) + c.c.} \quad (X = D_i, D^0)$$

$$R_{1/2} = 1 + r^2 \pm 2r \cos \phi_3 \cos \delta$$

(Error at $O(r^2)$ if $K^-\pi^+$ is used for D^0 (DCSD).)

Sensitivity to r at $O(r^2) \rightarrow r$ cannot be obtained by fit to $A_{1/2}$ and $R_{1/2}$.

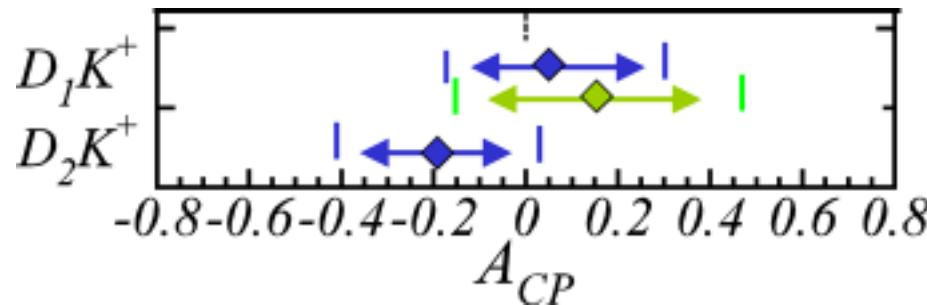
However,

$$A_2 \sim -A_1 \quad O(r), \quad \frac{A_1 - A_2}{2} \sim 2r \sin \phi_3 \sin \delta \quad O(r^2)$$

Also, $A_1 R_1 = -A_2 R_2$

$B^\pm \rightarrow D_{CP} K^\pm$ Results

	$CP+$	$CP-$
Belle <i>(DK)</i>	$A_1 = 0.06 \pm 0.19 \pm 0.04$ $R_1 = 1.21 \pm 0.25 \pm 0.14$	$A_2 = -0.19 \pm 0.17 \pm 0.05$ $R_2 = 1.41 \pm 0.27 \pm 0.15$
BaBar <i>(DK)</i>	$A_1 = 0.17 \pm 0.23 \pm 0.08$ $R_1 = 1.06 \pm 0.26 \pm 0.17$	
Belle(DK*)	$A_1 = -0.02 \pm 0.33 \pm 0.07$	$A_2 = 0.09 \pm 0.50 \pm 0.04$



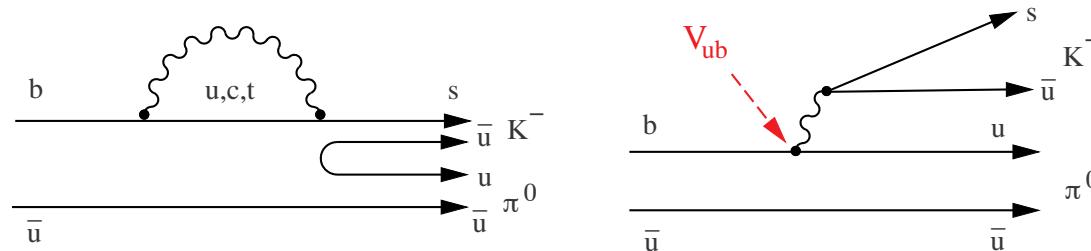
From *DK* results,

$$2r \sin \phi_3 \sin \delta = \frac{A_1 - A_2}{2} = 0.15 \pm 0.12 .$$

$B \rightarrow$ non-charm Rate Asymmetries

Direct CPV by tree-penguin interference.

e.g. for $K^- \pi^0$:



Statistically more favorable than DK modes,
but theoretically challenging.

Future: use theoretical models (PQCD, QCD factorization,
Charming penguin, etc.) for A_{CP} and Br 's to extract ϕ_3 .

$B \rightarrow$ non-charm Rate Asymmetries

$$A_{CP} \equiv \frac{\Gamma(\bar{B} \rightarrow \bar{f}) - \Gamma(B \rightarrow f)}{\Gamma(\bar{B} \rightarrow \bar{f}) + \Gamma(B \rightarrow f)}$$

A_{CP} by HFAG (Heavy Flavor Averaging Group) 2003 Winter

RPP#	Mode	PDG2002 Avg.	BABAR	Belle	CLEO	A_{CP} Avg.
86	$K^0\pi^+$	-0.05 ± 0.14	$-0.17 \pm 0.10 \pm 0.02$	$0.02 \pm 0.09 \pm 0.01$	$0.18 \pm 0.24 \pm 0.02$	-0.05 ± 0.07
87	$K^+\pi^0$	-0.10 ± 0.12	$-0.09 \pm 0.09 \pm 0.01$	$-0.02 \pm 0.19 \pm 0.02$	$-0.29 \pm 0.23 \pm 0.02$	-0.10 ± 0.08
88	$\eta'K^+$	-0.02 ± 0.07	$0.04 \pm 0.05 \pm 0.01$	$-0.02 \pm 0.07 \pm 0.01$	$0.03 \pm 0.12 \pm 0.02$	0.02 ± 0.04
92	ωK^+			$-0.21 \pm 0.28 \pm 0.03$		-0.28 ± 0.19
117	ϕK^+	-0.05 ± 0.20	$-0.05 \pm 0.20 \pm 0.03$			-0.05 ± 0.20
120	ϕK^{*+}	$-0.43^{+0.36}_{-0.31}$	$0.16 \pm 0.17 \pm 0.04$			0.16 ± 0.17
131	$\pi^+\pi^0$		$-0.03^{+0.18}_{-0.17} \pm 0.02$	$0.30 \pm 0.30^{+0.30}_{-0.06}$		0.05 ± 0.15
143	$\omega\pi^+$	-0.21 ± 0.19	$-0.01^{+0.29}_{-0.31} \pm 0.03$		$-0.34 \pm 0.25 \pm 0.02$	-0.21 ± 0.19
88	$K^+\pi^-$	-0.09 ± 0.06	$-0.10 \pm 0.05 \pm 0.02$	$-0.06 \pm 0.09^{+0.09}_{-0.01}$	$-0.04 \pm 0.16 \pm 0.02$	-0.05 ± 0.05
89	$K^0\pi^0$		$0.03 \pm 0.36 \pm 0.09$			0.03 ± 0.37
99	$K^+\rho^-$		$0.19 \pm 0.14 \pm 0.11$			0.19 ± 0.18
103	$K^{*+}\pi^-$				$0.26^{+0.33+0.10}_{-0.34-0.08}$	$0.26^{+0.33+0.10}_{-0.34-0.08}$
115	ϕK^{*0}	0.00 ± 0.27	$0.04 \pm 0.12 \pm 0.02$			0.04 ± 0.12
53	$K^*\gamma$	-0.01 ± 0.07	$-0.044 \pm 0.076 \pm 0.012$	$-0.022 \pm 0.048 \pm 0.017$	$-0.08 \pm 0.13 \pm 0.03$	-0.03 ± 0.04

(In PDG 2002 New since PDG2002)

$B \rightarrow$ non-charm Rate Asymmetries (New)

New since HFAG03,Winter:

A_{CP}	BaBar	Belle
$K^+ \pi^-$	$-0.07 \pm 0.06 \pm 0.01$	
$K^+ \pi^0$	$0.23 \pm 0.11^{+0.01}_{-0.04}$	
$K^0 \pi^+$		$0.07^{+0.09+0.01}_{-0.08-0.03}$
$\pi^+ \pi^0$	$-0.14 \pm 0.24^{+0.05}_{-0.04}$	
$\eta \pi^+$	$-0.51^{+0.20}_{-0.18} \pm 0.01$	
ηK^+	$-0.32^{+0.22}_{-0.18} \pm 0.01$	
$\omega \pi^+$	$0.04 \pm 0.17 \pm 0.01$	$0.48^{+0.23}_{-0.20} \pm 0.02$
ωK^+	$-0.05 \pm 0.16 \pm 0.01$	$0.06^{+0.20}_{-0.18} \pm 0.01$
ϕK^+	$0.039 \pm 0.086 \pm 0.011$	$0.01 \pm 0.12 \pm 0.05$
$\rho^0 \pi^+$	$-0.17 \pm 0.11 \pm 0.02$	
$\rho^+ \pi^0$	$0.23 \pm 0.16 \pm 0.06$	
$\rho^+ K^-$	$0.28 \pm 0.17 \pm 0.08$	$0.22^{+0.22+0.06}_{-0.23-0.02}$
$K^+ \pi^- \pi^0$		$0.07 \pm 0.11 \pm 0.01$
$\pi^+ \pi^- \pi^+$	$-0.39 \pm 0.33 \pm 0.12$	
$K^+ \pi^- \pi^+$	$0.01 \pm 0.07 \pm 0.03$	
$K^+ K^- K^+$	$0.02 \pm 0.07 \pm 0.03$	

Remarks on $B \rightarrow$ non-charm Rate Asymmetries

- Some modes are penguin-dominated.
 $(K^0\pi^+, \eta'K^+) \rightarrow A_{CP} \sim 0$. OK.
- $A_{CP}(\eta\pi^+) = -0.51 \pm 0.20$ significant?
 $\eta\pi^+, \eta K^+, \eta'\pi^+$ are theoretically expected to have large A_{CP} . Interesting to see more stat.
- Theoretical uncertainties are still large.

A_{CP}	exp.	PQCD	QCDF	Charming Penguin
$K^+\pi^-$	-0.08 ± 0.04	$-0.129 \sim -0.219$	0.05 ± 0.09	0.21 ± 0.22
$K^+\pi^0$	0.00 ± 0.07	$-0.100 \sim -0.173$	0.07 ± 0.09	0.22 ± 0.13
$K^0\pi^+$	0.02 ± 0.06	$-0.006 \sim 0.0015$	0.01 ± 0.01	0.0

Models do not agree well, except for $K^0\pi^+$ (penguin dom.).

Future Prospects

e^+e^- machines

- CLEO-c : 30M $D\bar{D}$'s (now running).
- Belle/BaBar : 3-400 fb^{-1} each by 2005
($\times 5$ more than presented today)
- Proposed :
Super-KEKB/Belle, Super-PEPII/BaBar.

	Super-Belle	Super-BaBar	now
$I_{\text{beam}}(A)$	3.5/8	9.6/22	1/1.5
$\mathcal{L}(/cm^2s)$	10^{35}	10^{36}	10^{34}
Starts	~ 2007	~ 2010	
sensitivities	(3yrs)	(1yr)	
$\sigma_{\sin 2\phi_{2\text{eff}}}$	0.060	0.032	0.2
$\sigma_{\sin(2\phi_1+\phi_3)}$	0.077	0.030	0.3
$\sigma_{\phi_3}(DK)$	$\sim 10^\circ$	$\sim 2.5^\circ$	-
$N(X_s\nu\bar{\nu})$		160	
$N(\tau\nu)$		350	

General Purpose Detectors at Hadron Machines

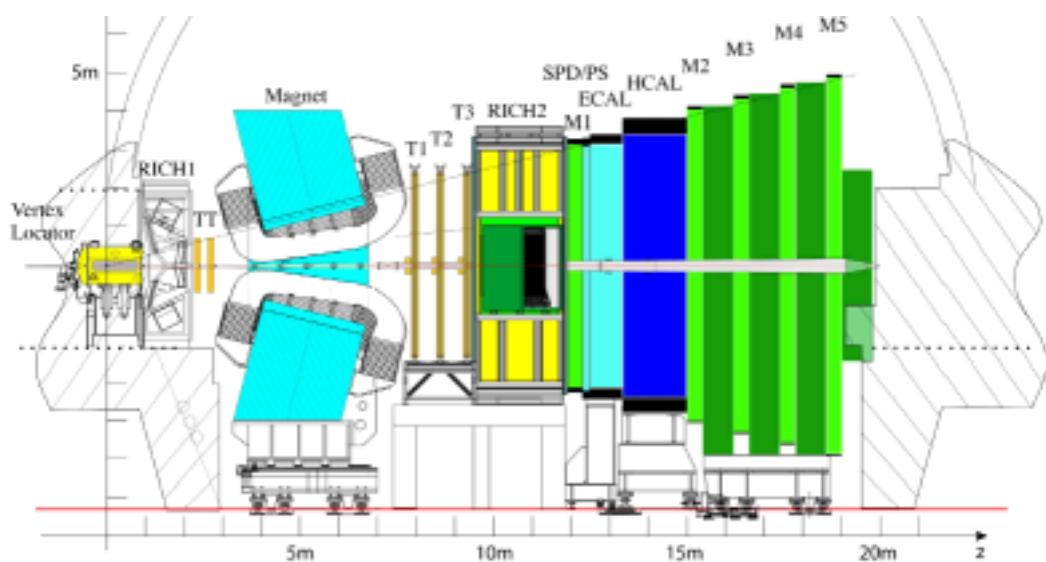
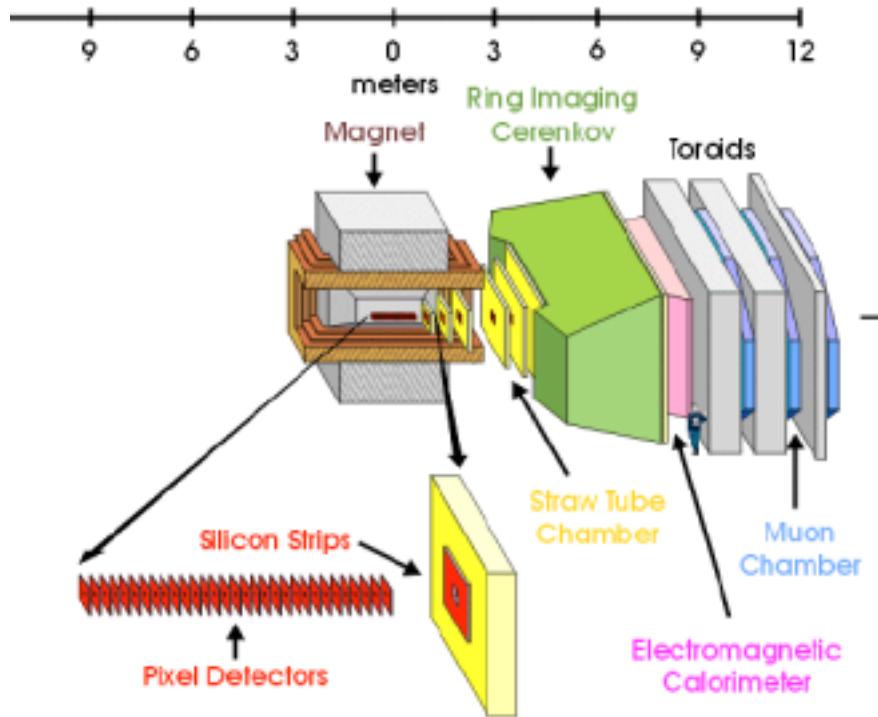
1. Tevatron Run2. (CDF, D0)

- 150 pb^{-1} now $\rightarrow 4\text{-}5 \text{ fb}^{-1}$ by LHC (2007)
- With 2 fb^{-1} ($+B_s, \Lambda_b$ physics)
 $\sigma_{\sin 2\beta} \sim 0.06$ (\sim B-factory now, different sys.)
 $\sigma_{A_{CP}(K^+\pi^-)} \sim 1 \sim 10\%$.

2. LHC. (ATLAS, CMS)

- B -physics while intensity is not too high.
- $\sigma_{\sin 2\alpha_{\text{eff}}} \sim 0.09$ ($\#\pi^+\pi^- \sim 2.3K$)
Not as good as BTeV/LHCb.
- $\#(B \rightarrow \mu\mu) \sim 30$
 $\#(B \rightarrow s\mu\mu) \sim 5K$
As good as BTeV/LHCb

Dedicated B-Facilities at Hadron Machines



BTeV at Tevatron

$p\bar{p}$ at $E_{CM} = 2 \text{ TeV}$

Approved by lab.

Pending P5 panel. 2009→

LHCb at LHC

pp at $E_{CM} = 14 \text{ TeV}$

Under construction.

2007→

BTeV/LHCb Sensitivities/1yr(10^7 s)

(#events sensitivity)

	LHCb	BTeV
$\sigma_{b\bar{b}}$	$500\mu b$	$100\mu b$
# $b\bar{b}$	10^{12}	1.5×10^{11}
$B_d \rightarrow J/\Psi K_S$	$119K$ $\sigma_\beta \sim 0.6^\circ$	$168K$ $\sigma_{\sin 2\beta} \sim 0.017$
$B_d \rightarrow \rho^0 \pi^0$		$0.78K$ $\sigma_\alpha \sim 4^\circ$
$\begin{cases} B_d \rightarrow \pi^+ \pi^- \\ B_s \rightarrow K^+ K^- \end{cases}$	$27K$ $\sigma_\alpha^* \sim 5-10^\circ$ $35K$	$14.6K$ $\sigma_A \sim 0.03$ $18.9K$ $\sigma_A \sim 0.02$
$B_s \rightarrow D_s K$	$8K$ $\sigma_\gamma \sim 10^\circ$	$7.5K$ $\sigma_{\gamma-2\chi} \sim 8^\circ$
$B_s \rightarrow J/\Psi \phi$	$128K$ $\sigma_{2\delta\gamma} \sim 2^\circ$	
$B_s \rightarrow J/\Psi \eta/\eta'$		$12.6K$ $\sigma_{\sin 2\chi} \sim 0.024$

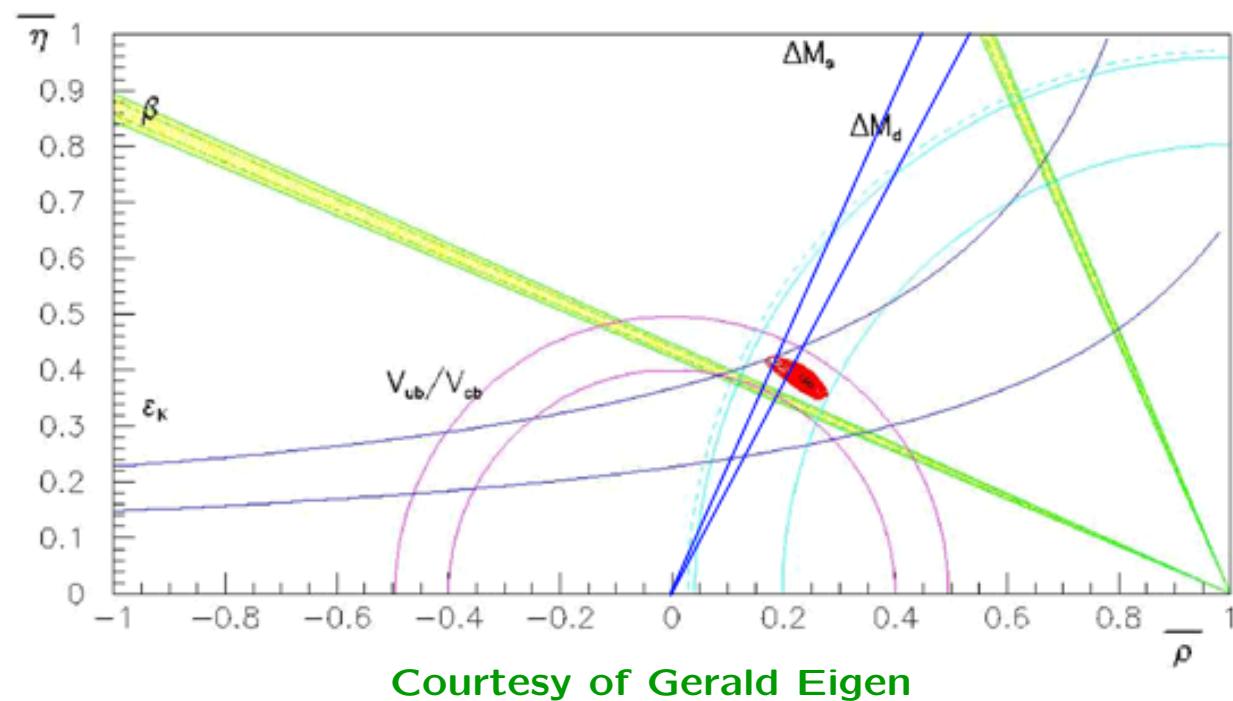
* Requires SU(3) modeling.

pros: B_s , PID, long decay lengths

Summary

- ϵ'/ϵ of K_L has established direct CPV.
- CPV in charmonium $K_{S,L}$ modes firmly established.
 $\sin 2(\phi_1/\beta) = 0.734 \pm 0.055$ consistent with SM.
- Hint of deviation of " $\sin 2\phi_1$ " (ϕK_S) from SM by Belle, but not by BaBar.
- Hint of direct CPV in $\pi^+\pi^-$ by Belle, but not by BaBar.
- Hint of direct CPV in $\rho^+\pi^-$ (BaBar).
- Accuracy of ϕ_3/γ by $D^{(*)}\pi$ modes is becoming meaningful.
- Sensitivity in A_{CP} of DK modes is approaching interesting region.
- No clear direct CPV in rate asymmetries A_{CP} , except for some hint in $\eta\pi^+$.

In around 2010, it may look like,



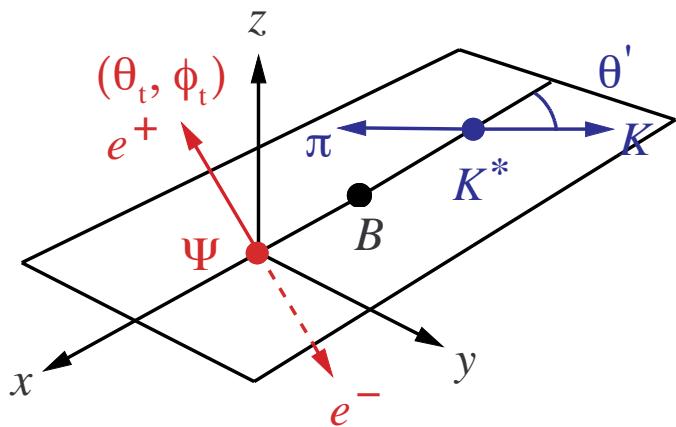
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CP contents in $\Psi K^{*0} (\rightarrow K_S \pi^0)$

B (spin-0) $\rightarrow \Psi$ (spin-1) K^{*0} (spin-1)

3 polarization states: helicities = $(++, --, 00) \rightarrow A_{\parallel}, A_0, A_{\perp}$

Extract P (CP) contents by full angular analysis
of the isospin-related modes.



$$|A_{\parallel}|^2 + |A_0|^2 + |A_{\perp}|^2 = 0$$

$ A_0 ^2$	0.617 ± 0.020
$ A_{\perp} ^2$	0.192 ± 0.023
$\arg(A_{\parallel})$	2.83 ± 0.19
$\arg(A_{\perp})$	-0.09 ± 0.13

(Belle 29.4 fb^{-1})

No indication of FSI phases.

$$\text{frac}(CP-) = 0.191 \pm 0.023(\text{stat}) \pm 0.026(\text{sys})$$

(ΨK^{*0} used as incoherent sum of $CP\pm$ in the previous analysis)

Time-dependent CPV of $\Psi K^{*0}(\rightarrow K_S\pi^0)$ (78fb^{-1})

$$\frac{d\Gamma}{d\vec{\theta} d\Delta t} \propto e^{-\frac{|\Delta t|}{\tau_B}} \sum_{i=1}^6 g_i(\vec{\theta}) a_i(\Delta t)$$

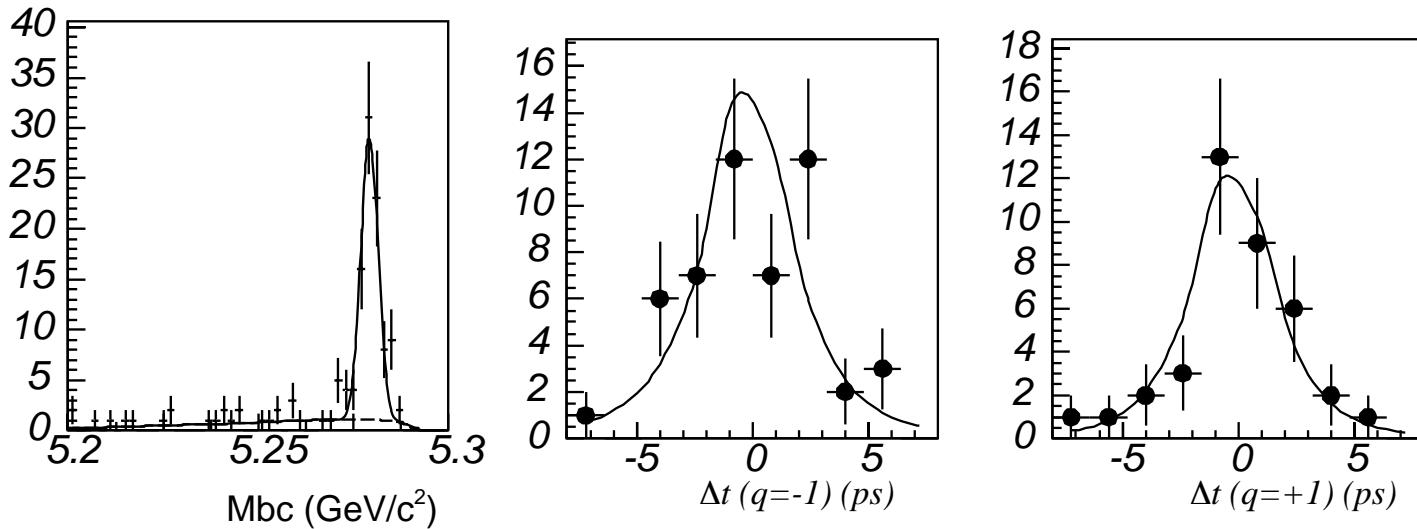
$$\vec{\theta} \equiv (\cos \theta_t, \phi_t, \cos \theta')$$

Information on $\cos 2\phi_1$ (as well as on $\sin 2\phi_1$)
 through interference of $A_{\parallel/0}$ and A_{\perp} : (B. Kaiser)

$$a_{5/6} = q [\text{Im}(A_{\parallel/0}^* A_{\perp}) \cos \delta m \Delta t - \text{Re}(A_{\parallel/0}^* A_{\perp}) \cos 2\phi_1 \sin \delta m \Delta t]$$

$$\begin{cases} g_5 = \sin^2 \theta' \sin 2\theta_t \sin \phi_t \\ g_6 = \frac{1}{\sqrt{2}} \sin 2\theta' \sin 2\theta_t \cos \phi_t \end{cases}$$

Time-dependent CPV of $\Psi K^{*0}(\rightarrow K_S \pi^0)$



Unbinned likelihood fit to $(\vec{\theta}, \Delta t)$ distribution.

$\sin 2\phi_1$ floated:

$$\sin 2\phi_1 = 0.13 \pm 0.51 \pm 0.06, \quad \cos 2\phi_1 = 1.40 \pm 1.28 \pm 0.19.$$

$\sin 2\phi_1 = 0.82$ fixed:

$$\cos 2\phi_1 = 1.02 \pm 1.05 \pm 0.19.$$