

1

$B^0 \rightarrow D^* \pi$ 崩壊事象を用いた CP対称性の破れの測定

板垣 憲之輔 (東北大学)

and Belle collaboration

内容

- 導入
- Signal MC の再構成
- Generic MC を使用した Signal fraction の見積もり
- Generic MC の Δt fit
- Signal MC + Generic MC の Δt fit
- まとめ

導入

- 動機：CP非保存角 $\phi_3 \equiv \arg\left(\frac{V_{ud}V_{ub}^*}{-V_{cd}V_{cb}^*}\right) \cong -\arg(V_{ub}^*)$ の精密測定
- $B^0 \rightarrow D^* \pi$ 崩壊

- 二つの崩壊経路

$$B^0 \rightarrow D^{*\mp} \pi^\pm, \bar{B}^0 \rightarrow D^{*\pm} \pi^\mp$$

- DCSD が V_{ub} を含む

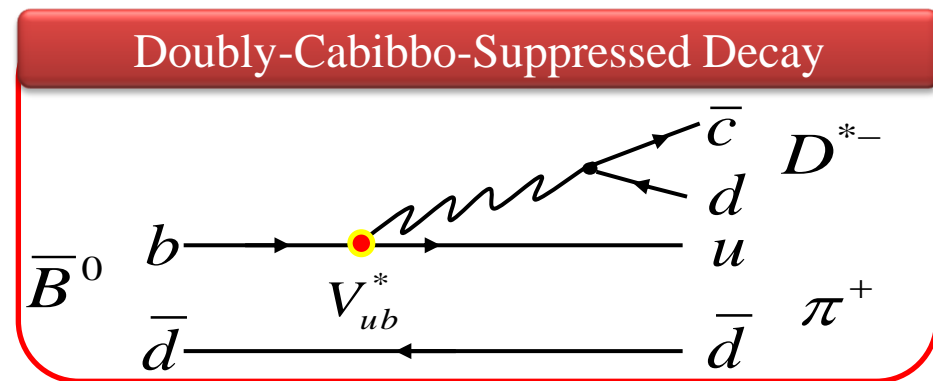
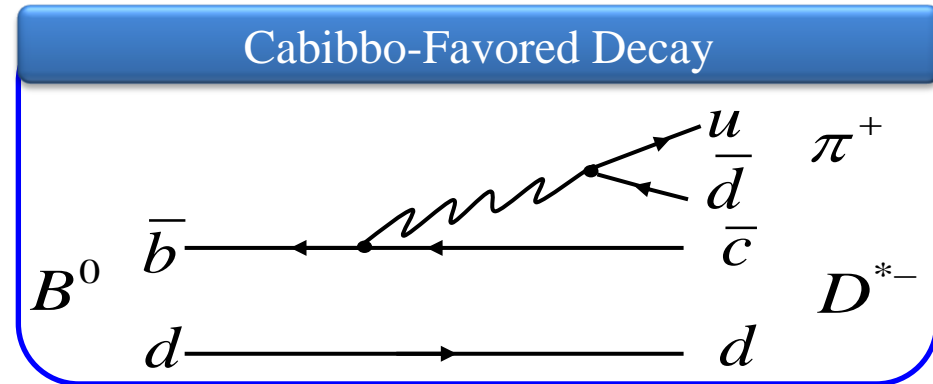
崩壊率

$$P(B^0 \rightarrow D^{*\mp} \pi^\pm) \propto 1 \pm C \cos(\Delta m \Delta t) - S^\mp \sin(\Delta m \Delta t)$$

$$P(\bar{B}^0 \rightarrow D^{*\pm} \pi^\mp) \propto 1 \pm C \cos(\Delta m \Delta t) + S^\pm \sin(\Delta m \Delta t)$$

$$S^\pm = -\frac{2R}{1+R^2} \sin(2\phi_1 + \phi_3 \pm \delta)$$

$$R = \frac{\Gamma(B^0 \rightarrow D^{*+} \pi^-)}{\Gamma(B^0 \rightarrow D^{*-} \pi^+)} \sim 0.02, \delta = \text{強い相互作用の位相差}$$



➡ S^\pm が小さく、精密な測定が必要

導入：今までの結果

- 再構成方法

- Partial reconstruction: 検出効率が良い
- Full reconstruction: 信号/背景事象の比が良い

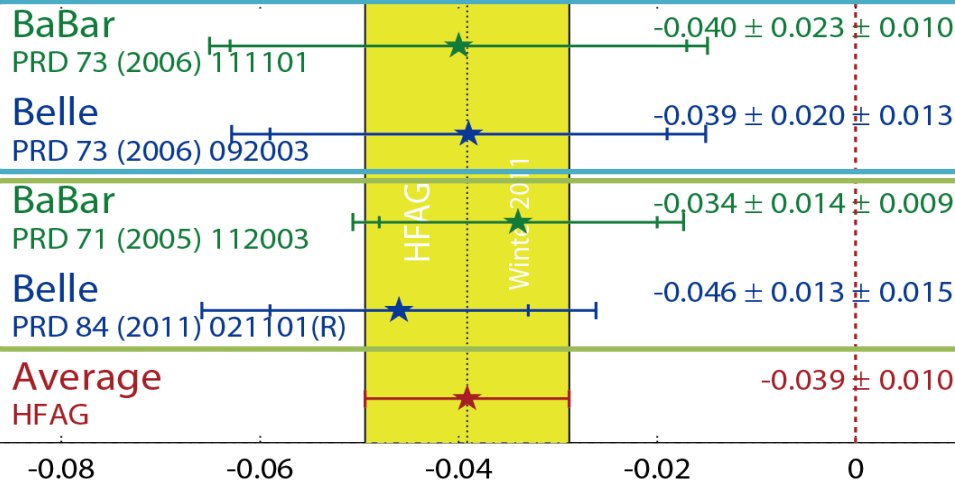
$$B^0 \rightarrow D^* \pi$$

$$D^* \rightarrow D^0 \pi$$

$$D^* \rightarrow D\pi^0$$

Merged $D^*\pi$ a

HFAG
Winter 2011
PRELIMINARY

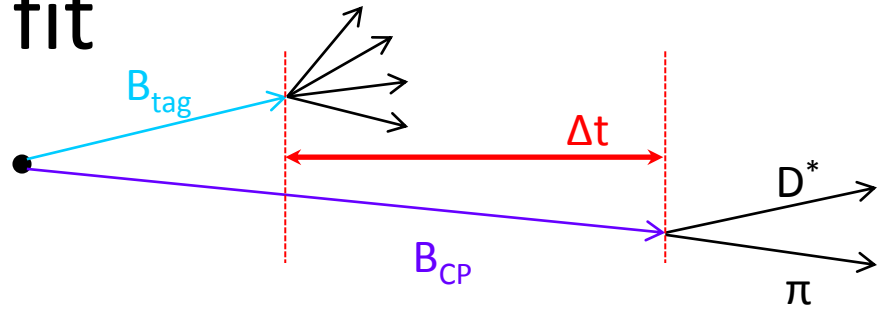


Full reconstruction

Partial reconstruction

独立

- Full reconstruction, $386 \times 10^6 \rightarrow 772 \times 10^6$ BB ペア
- 統計誤差: $0.020 \rightarrow 0.014$

Δt fit

Δt の情報を失った
イベントの補正

- Δt : B_{tag} と B_{CP} の崩壊時間差
 - B_{CP} : $B^0 \rightarrow D^* \pi$
 - B_{tag} : flavor 同定に使用

PDF

$$P(\Delta t) = (1 - f_{ol}) \left[\underbrace{f_{sig} P_{sig}}_{\text{信号}} + (1 - f_{sig}) \left\{ \underbrace{f_{B^0 \bar{B}^0} P_{B^0 \bar{B}^0}}_{\text{中性B}} + \underbrace{f_{B^+ B^-} P_{B^+ B^-}}_{\text{荷電B}} + \underbrace{(1 - f_{B^0 \bar{B}^0} - f_{B^+ B^-}) P_{con}}_{\text{B以外}} \right\} \right] + \underbrace{f_{ol} P_{ol}}_{\text{補正}}$$

– P_{sig} : 信号事象項

前回はまとめていた
→ より精密な測定のため、
個別に求めることとした

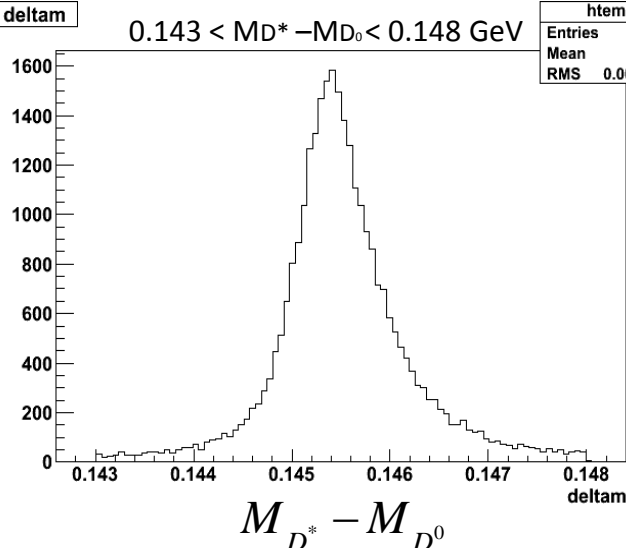
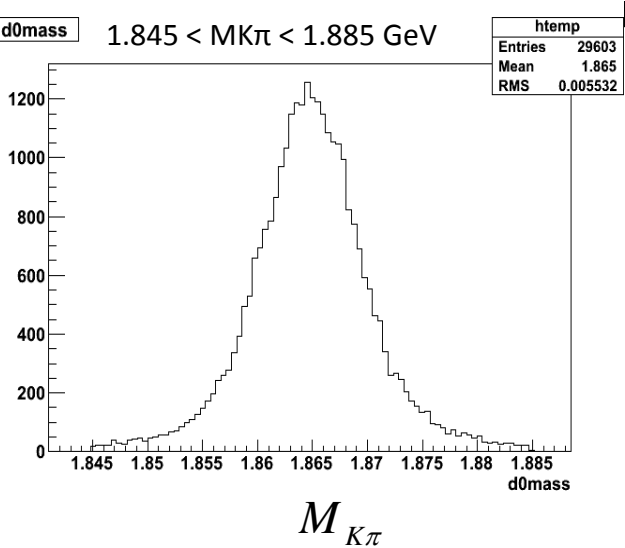
$$P(D^{*\mp} \pi^\pm, q_{tag}) = \int \frac{e^{-|\Delta t'|/\tau_{B^0}}}{8\tau_{B^0}} \left\{ 1 - q_{tag} \Delta w_i \pm q_{tag} (1 - 2w_i) \right. \\ \left. \times (C \cos(\Delta m \Delta t') - q_{tag} S^\mp \sin(\Delta m \Delta t')) \right\} \\ \times R(\Delta t - \Delta t') d\Delta t'$$

検出器のresolution補正項

- B の崩壊を模擬したデータサンプル(Generic MC)で、上記を求めた

再構成: $B^0 \rightarrow D^* \pi$, $D^* \rightarrow D^0 \pi$, $D^0 \rightarrow K \pi$

- Signal MC 100,000 events を生成、再構成 (Data : $\sim 56,000$ events)



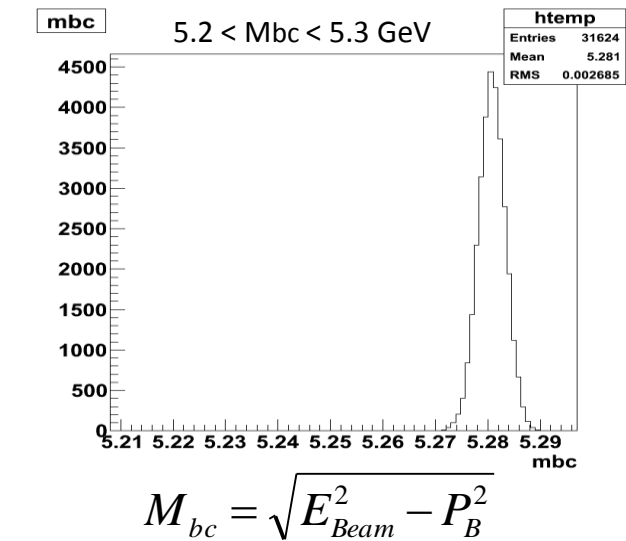
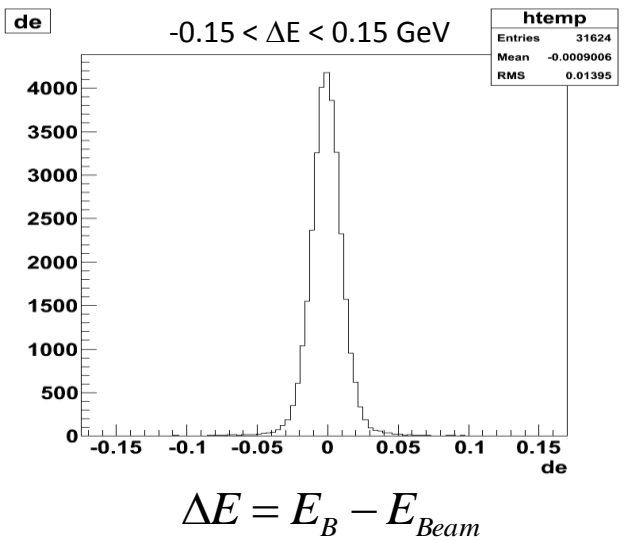
事象選別

1.845 < $M_{K\pi}$ < 1.885 GeV

0.143 < $M_{D^*} - M_{D^0}$ < 0.148 GeV

5.27 < M_{bc} < 5.29 GeV

-0.045 < ΔE < 0.045 GeV

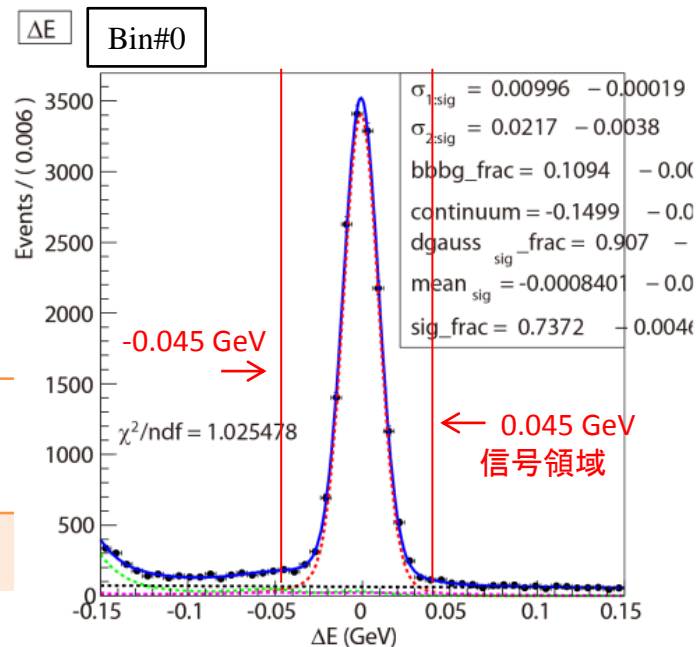


再構成数: 29,603 \sim 30%

Generic MCを使用した Signal fraction 決定

- ΔE を使用して、含まれる信号事象の比を求めた。

Bin#0 → Bin#6 Flavor tag 信頼度高
変数
信号事象: ダブルガウシアン B以外の背景事象: 直線 信号事象比
B 背景事象: 固定



信号事象 ~ 89%
 B^0 BG ~ 2%, B^\pm BG ~ 4%
 B 以外 ~ 5%

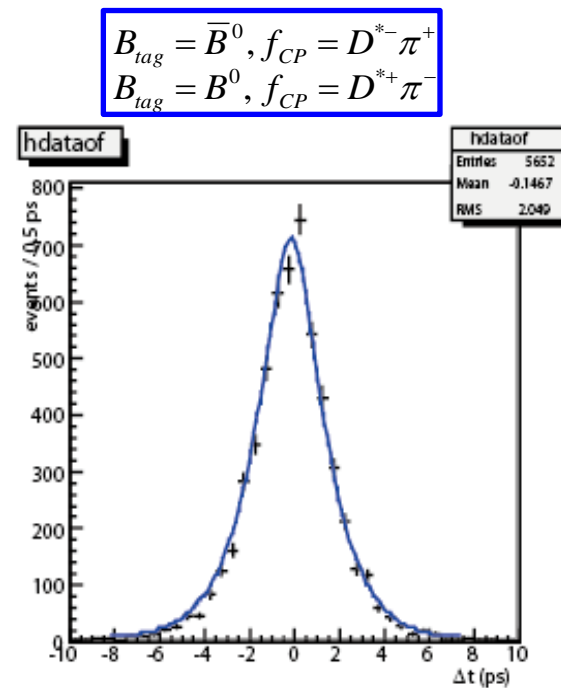
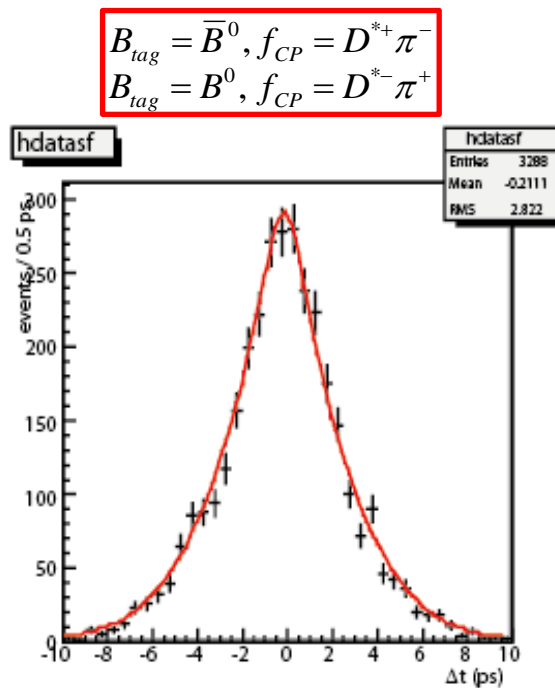
Flavor tag 信頼度	信号事象	中性B 背景事象	荷電B 背景事象	B以外の 背景事象
Bin#0	89%	2%	4%	5%
Bin#1	89%	2%	4%	5%
Bin#2	90%	3%	4%	3%
Bin#3	90%	2%	3%	5%
Bin#4	89%	3%	4%	5%
Bin#5	91%	3%	3%	3%
Bin#6	95%	3%	2%	0%

中性B中間子背景事象の Δt fit

$$P_{B^0BG}(\Delta t, q_{tag}, q_{cp}) = \int \underbrace{\frac{e^{-|\Delta t'|/\tau_{B^0BG}}}{\delta\tau_{B^0BG}}}_{\text{寿命項}} \left\{ \underbrace{1 - q_{tag}q_{cp}(1 - 2w_{rbin})}_{\text{Flavor tag 補正}} \underbrace{\cos(\Delta m\Delta t')}_{\text{B}^0\text{B}^0\text{bar mixing 項}} \right\} \times \underbrace{R(|\Delta t - \Delta t'|)}_{\text{Resolution 補正}} d\Delta t'$$

Fit 結果

Name	Value
τ_{B^0BG}	1.525 ± 0.019 (ps)
Δm	0.516 ± 0.013
w_0	0.50 (fixed)
w_1	0.45 ± 0.02
w_2	0.29 ± 0.02
w_3	0.23 ± 0.02
w_4	0.18 ± 0.02
w_5	0.12 ± 0.02
w_6	0.03 ± 0.01



荷電B中間子背景事象の Δt fit

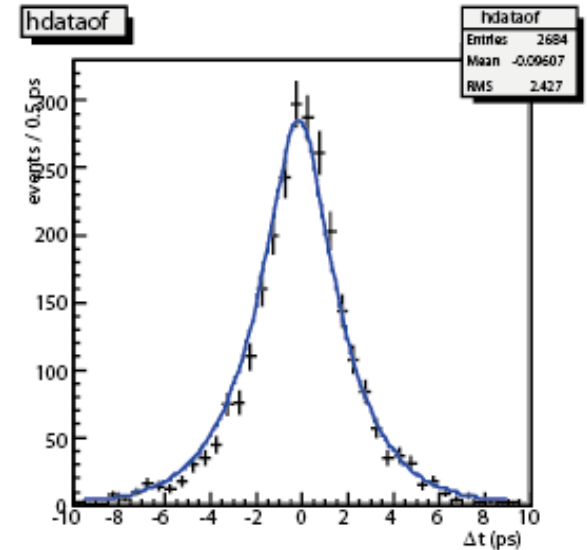
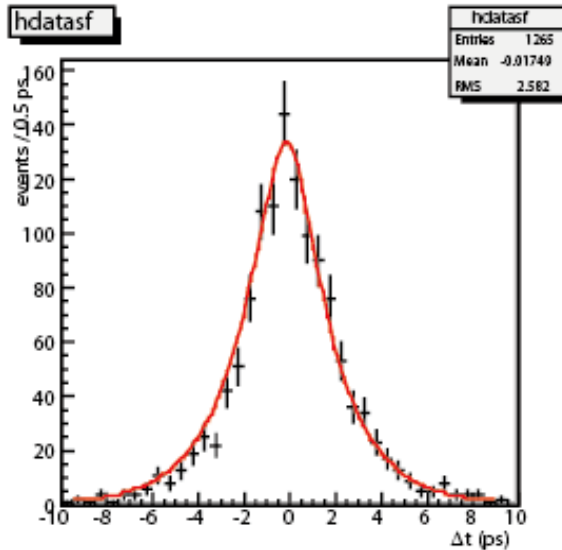
$$P_{chg}(\Delta t, q_{tag}, q_{cp}) = \int \frac{e^{-|\Delta t'|/\tau_{chgB}}}{8\tau_{chgB}} \left\{ 1 - q_{tag} q_{cp} (1 - 2w_{rbin}) \right\} \times R(\Delta t - \Delta t') d\Delta t'$$

Fit 結果

Name	Value
τ_{chgB}	1.599 ± 0.029 (ps)
w_0	0.50 (fixed)
w_1	0.44 ± 0.02
w_2	0.32 ± 0.02
w_3	0.26 ± 0.02
w_4	0.16 ± 0.02
w_5	0.13 ± 0.02
w_6	0.04 ± 0.01

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*+} \pi^- \\ B_{tag} &= B^0, f_{CP} = D^{*-} \pi^+ \end{aligned}$$

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*-} \pi^+ \\ B_{tag} &= B^0, f_{CP} = D^{*+} \pi^- \end{aligned}$$



B以外の背景事象の Δt fit

$$P_{con}(\Delta t) = \int P_{con}(\Delta t') \cdot R_{con}(\Delta t - \Delta t') \cdot d\Delta t'$$

$$P_{con}(\Delta t) = f_{\delta} \delta(\Delta t - \mu_{\delta}) + (1 - f_{\delta}) \cdot \exp\left(-\frac{|\Delta t - \mu_{\tau}|}{\tau_{con}}\right)$$

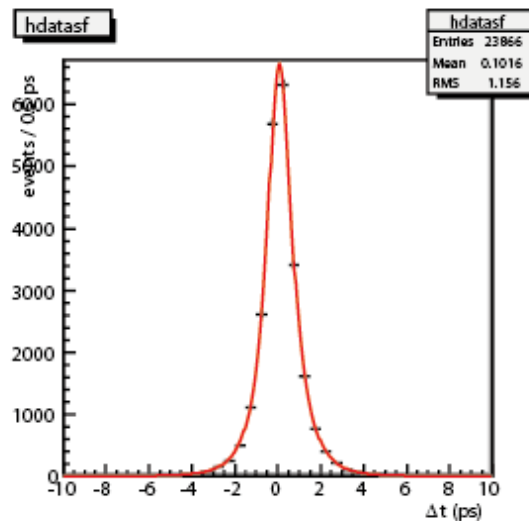
$$R_{con}(\Delta t) = (1 - f_{con}^{tail}) \cdot G(\Delta t; s_{con}^{main}, \sigma_{vtx}) + f_{con}^{tail} \cdot G(\Delta t; s_{con}^{tail}, \sigma_{vtx})$$

Fit 結果

	Single-track vertex Either CP or tag B	Multi-track vertex Both CP and tag B
f_d	0.26 ± 0.04	0.39 ± 0.02
m_d	0.046 ± 0.007	
m_{τ}	0.14 ± 0.01	
τ_{con}	0.58 ± 0.02	
s_{bkg}^{main}	1.07 ± 0.03	1.34 ± 0.02
s_{bkg}^{tail}	5.40 ± 0.42	4.87 ± 0.26
f_{bkg}^{tail}	0.088 ± 0.010	0.047 ± 0.007

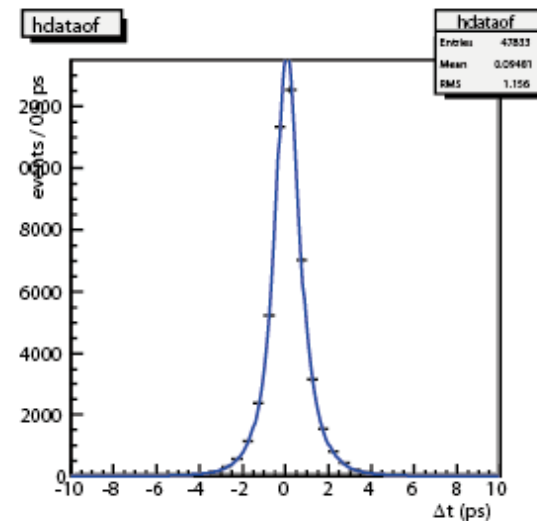
$$B_{tag} = \bar{B}^0, f_{CP} = D^{*+} \pi^{-}$$

$$B_{tag} = B^0, f_{CP} = D^{*-} \pi^{+}$$



$$B_{tag} = \bar{B}^0, f_{CP} = D^{*-} \pi^{+}$$

$$B_{tag} = B^0, f_{CP} = D^{*+} \pi^{-}$$



信号事象 + 背景事象での Δt fit

• PDF

$$P(\Delta t) = (1 - f_{ol}) \left[f_{sig} P_{sig} + (1 - f_{sig}) \left\{ f_{B^0\bar{B}^0} P_{B^0\bar{B}^0} + f_{B^+B^-} P_{B^+B^-} + (1 - f_{B^0\bar{B}^0} - f_{B^+B^-}) P_{con} \right\} \right] + f_{ol} P_{ol}$$

- 信号事象/背景事象比: $f_{sig}, f_{B^0\bar{B}^0}, f_{B^+B^-}$

- $P_{B^0\bar{B}^0}$: 中性B中間子背景事象項

- $P_{B^+B^-}$: 荷電B中間子背景事象項

- P_{con} : B中間子以外の背景事象項

- $f_{ol} P_{ol}$: Δt の情報を失った成分 ← 40 ps の幅を持つガウシアン

- P_{sig} : 信号事象項

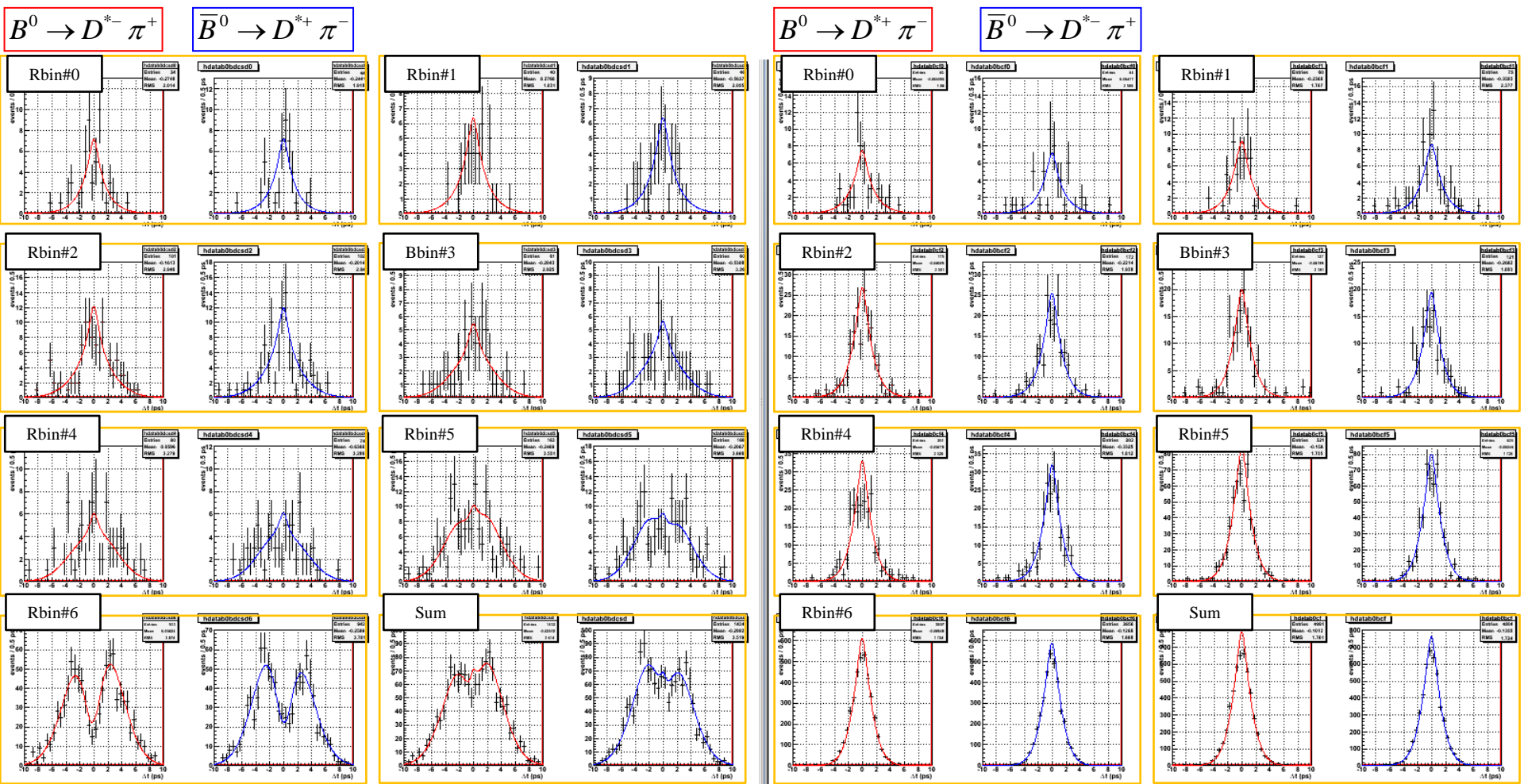
$$P(D^{*\mp} \pi^\pm, q_{tag}) = \int \frac{e^{-|\Delta t'|/\tau_{B^0}}}{8\tau_{B^0}} \left\{ 1 - q_{tag} \Delta w_i \pm q_{tag} (1 - 2w_i) \times (C \cos(\Delta m \Delta t') - q_{tag} S^\mp \sin(\Delta m \Delta t')) \right\} \times R(\Delta t - \Delta t') d\Delta t'$$

Flavor tag 補正, 信頼度ごと

検出器のresolutionの補正項

→ signal MC + generic MC について S^\pm を fit

$$2\phi_1 + \phi_3 = 1.8, \delta = 0, R = 0.02$$

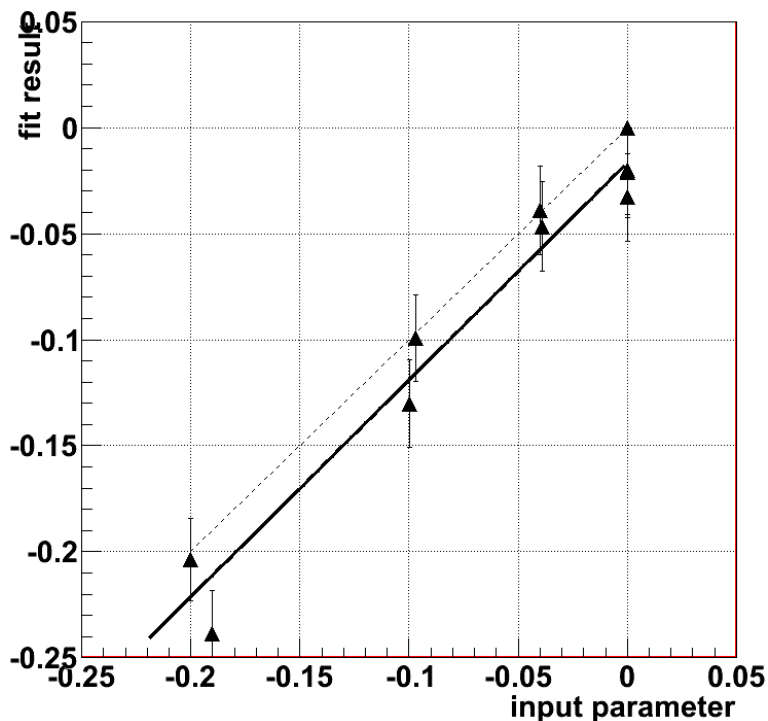


S^\pm (input)	S^+ (diff)	S^- (diff)
-0.039	-0.047 ± 0.0055 (0.36 σ)	-0.032 ± 0.0055 (0.35 σ)

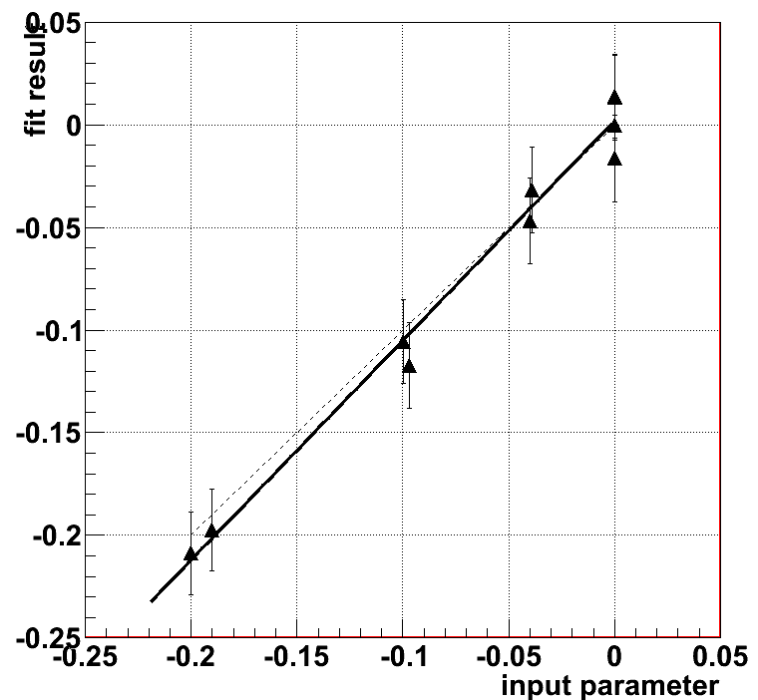
信号事象 + 背景事象での Δt fit

- 9通りのMCを作り、 S^\pm のリニアリティを確認した
 - Fit function : $y = P1x + P0$

S^+ $P0 = -0.017 \pm 0.0098$
 $P1 = 1.02 \pm 0.091$



S^- $P0 = 0.0020 \pm 0.0097$
 $P1 = 1.07 \pm 0.091$



まとめ

- 目的: ϕ_3 の測定
- Belle 全データ: 統計誤差 0.020(前回) \rightarrow \sim 0.014
- $D^* \rightarrow D^0\pi$, $D^0 \rightarrow K\pi$
 - Signal fraction を見積もった
 - Continuum BG, B^0 BG, B^\pm BG の Δt PDF を求めた ← new
 - 9 通りのMC を作り、fit した S^\pm のリニアリティを確認した

計画

- 使用する下位崩壊について、背景事象を求める
- Tag-side interference の取り扱い
- 系統誤差の見積もり
- Data fit

系統誤差

Signal Δt resolution

continuum Background Δt shape

Neutral B Background Δt shape

Charged B Background Δt shape

Signal Background fraction

Wrong tag fraction

Vertexing

Physics parameters(τ , Δm)

Fit bias



Buck up

信号事象の Δt fit

- $\tau, \Delta m$ を fit

$$P_{sig}(\Delta t, q_{tag}, q_{cp}) = \frac{1}{8\tau} e^{-|\Delta t|/\tau} \left\{ 1 - q_{tag} \Delta w_{rbin}^{official} - q_{tag} q_{cp} (1 - 2w_{rbin}^{official}) \cos(\Delta m \Delta t) \right\}$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*-} \pi^+ \text{ と } B_{tag} = B^0, f_{CP} = D^{*+} \pi^-$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*+} \pi^- \text{ と } B_{tag} = B^0, f_{CP} = D^{*-} \pi^+$$

を $\delta = 0$ として統合 \rightarrow sin 項を無視

$w, \Delta w$: flavor tag の間違いを補正

$$w = \frac{w_{B^0} + w_{\bar{B}^0}}{2}, \Delta w = w_{B^0} - w_{\bar{B}^0}$$

Official wrong tag fraction を使用

R bin #	official wrong tag fraction	
Bin#0	w = 0.5	$\Delta w = 0.$
Bin#1	w = 0.412222	$\Delta w = 0.00408778$
Bin#2	w = 0.307838	$\Delta w = 0.010326$
Bin#3	w = 0.212765	$\Delta w = -0.00479522$
Bin#4	w = 0.149933	$\Delta w = 0.00151989$
Bin#5	w = 0.0913264	$\Delta w = 0.0143633$
Bin#6	w = 0.0218754	$\Delta w = 0.00189979$

背景事象の Δt fit

- 背景事象のPDFを得るため、各々を fit
- Fit 範囲 : $-0.15 \text{ GeV} < \Delta E < 0.15 \text{ GeV}$, $5.2 \text{ GeV} < M_{bc} < 5.3 \text{ GeV}$

中性B中間子背景事象 PDF

$$P_{B^0BG}(\Delta t, q_{tag}, q_{cp}) = \frac{1}{8\tau_{B^0BG}} e^{-|\Delta t|/\tau_{B^0BG}} \left\{ 1 - q_{tag} q_{cp} (1 - 2w_{rbin}) \cos(\Delta m \Delta t) \right\}$$

荷電B中間子背景事象 PDF

$$P_{chg}(\Delta t, q_{tag}, q_{cp}) = \frac{1}{8\tau_{chgB}} e^{-|\Delta t|/\tau_{chgB}} \left\{ 1 - q_{tag} q_{cp} (1 - 2w_{rbin}) \right\}$$

B中間子以外からの背景事象 PDF

$$P_{con}(\Delta t) = \int P_{con}(\Delta t') \cdot R_{bkg}(\Delta t - \Delta t') \cdot d\Delta t'$$

$$P_{con}(\Delta t) = f_{\delta} \cdot \delta(\Delta t - \mu_{\delta}) + (1 - f_{\delta}) \cdot \exp\left(-\frac{|\Delta t - \mu_{\tau}|}{\tau_{con}}\right)$$

$$R_{con}(\Delta t) = (1 - f_{con}^{tail}) \cdot G(\Delta t; s_{con}^{main} \cdot \sigma_{vtx}) + f_{con}^{tail} \cdot G(\Delta t; s_{con}^{tail} \cdot \sigma_{vtx})$$

ΔE PDF

- Signal fraction を計算するため、

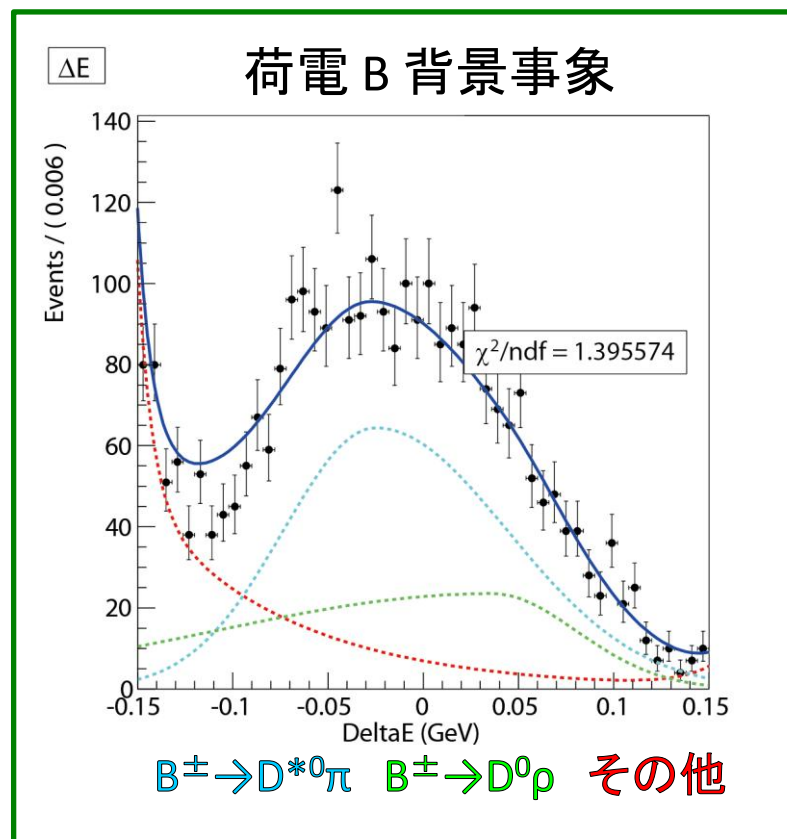
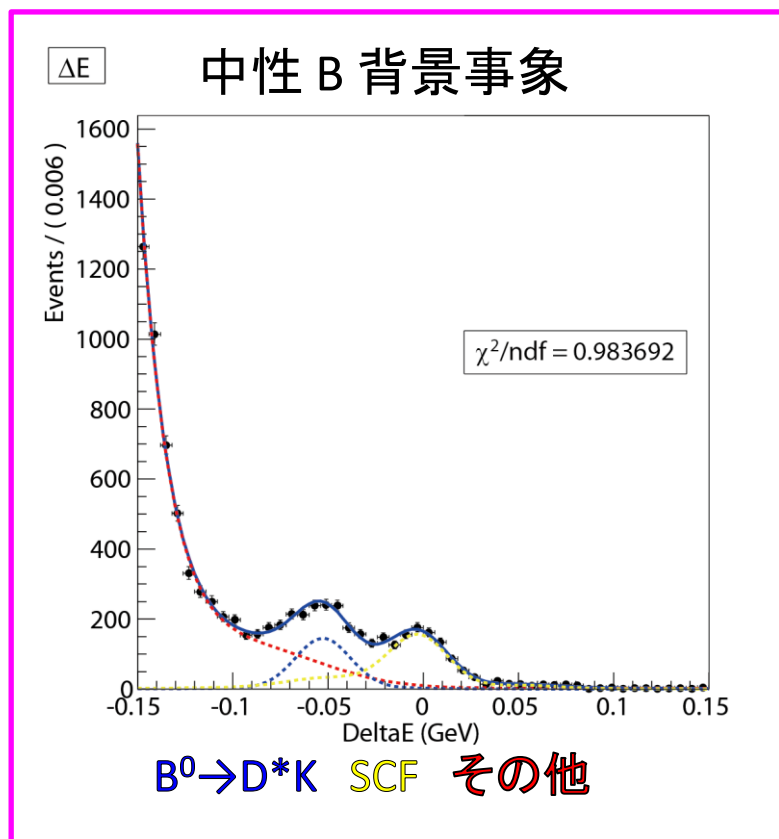
ΔE PDF を見積もった

実験データの 5 倍の統計量を使用

範囲 : $5.27 \text{ GeV} < M_{bc} < 5.29 \text{ GeV}$

$-0.15 \text{ GeV} < \Delta E < 0.15 \text{ GeV}$

- 得られた 中性/荷電 B 背景事象の ΔE PDF



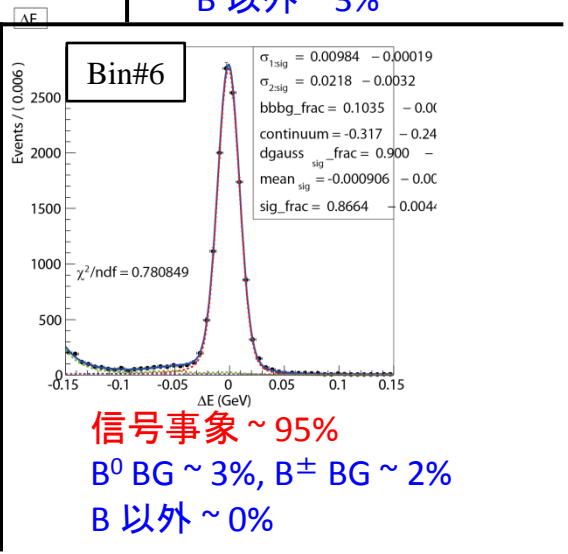
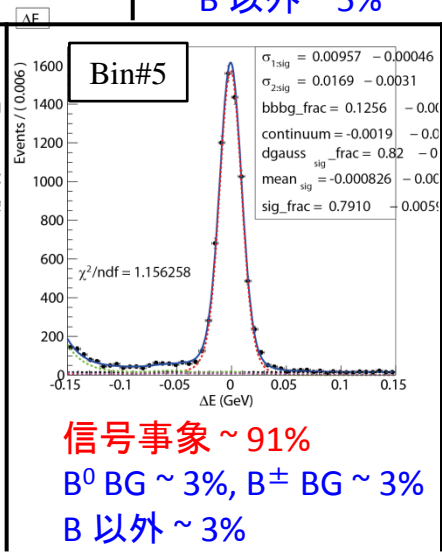
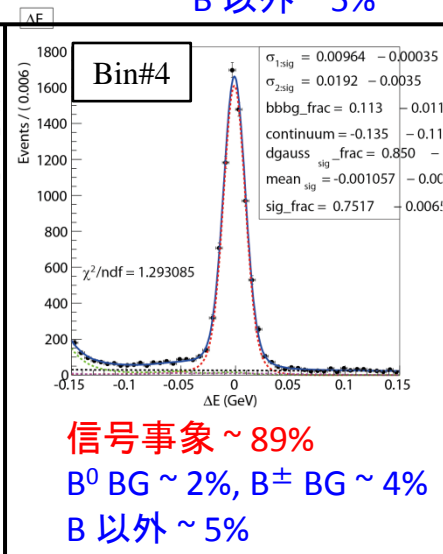
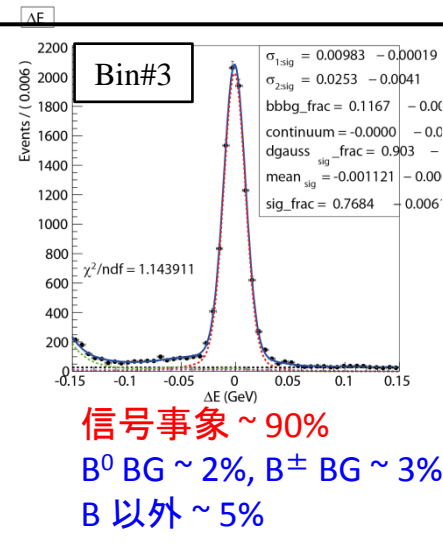
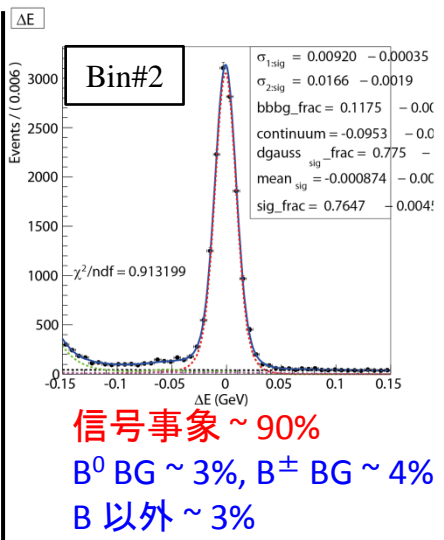
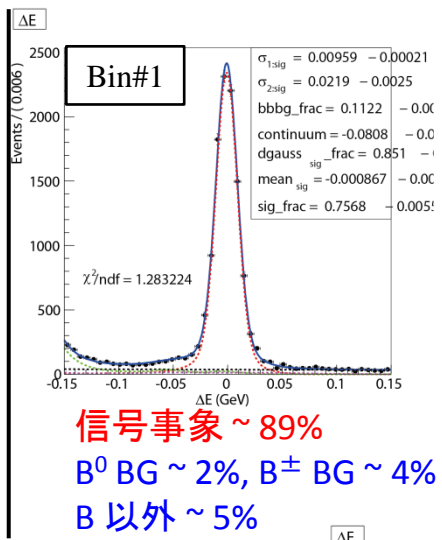
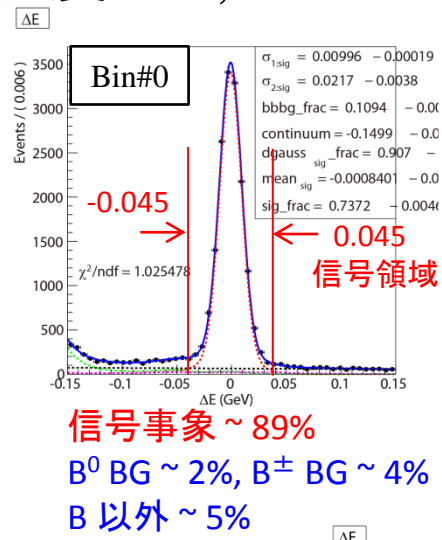
Signal fraction

- ΔE を使用して、含まれる信号事象の比を求めた。
 - flavor tag の信頼度ごと, Generic MC

Bin#0 → Bin#6
信頼度高

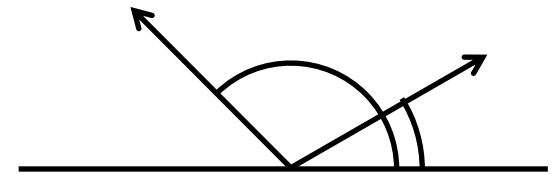
変数
信号事象: ダブルガウシアン
B以外の背景事象: 直線
信号事象比

B 背景事象: 固定



Partial recon Signal event selection

- 正確なvertex の決定のための Fast pion への要求
 - Impact parameter
 - radial : $dr < 0.1 \text{ cm}$
 - longitudinal : $|dz| < 2.0 \text{ cm}$
 - SVDにヒットをもつ
 - Polar angle in the laboratory frame : $30^\circ < \theta_{lab} < 135^\circ$
- The vertex positions are obtained by fits of the candidate tracks with the IP.
- Lepton, kaon hypothesis と一致しない
 - Based on information from the CDC, TOF and ACC.
- Fast pion cms momentum : $1.83 \text{ GeV}/c < p_{\pi_f} < 2.43 \text{ GeV}/c$



Partial recon Signal event selection

- Slow pion cms momentum : $0.05 \text{ GeV}/c < p_{\pi_s} < 0.30 \text{ GeV}/c$
- Particle identification のとき、slow pion には何の条件も課さない
- Vertexing に使用しない
- IP から生じることのみ要求する

- fast pion とslow pion は逆の電荷をもつ

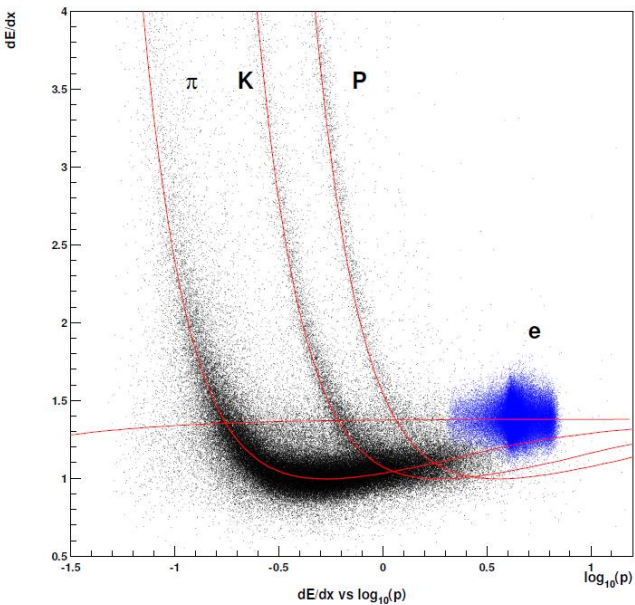
D* π 数

- $771.581 \times 10^6 \times 2.76 \times 10^{-3} = 2.13 \times 10^6$
– $K\pi : \times 67.7 \times 10^{-2} \times 3.89 \times 10^{-2} = 56000$
- 使用する下位崩壊
 - D* \rightarrow D⁰ π (67.7%)
 - D⁰ \rightarrow K π (3.89%), K $\pi\pi^0$ (13.9%), K $\pi\pi\pi$ (8.09%), K_s $\pi\pi$ (2.94%)
 - D* \rightarrow D π^0 (30.7%)
 - D \rightarrow K $\pi\pi$ (9.4%)

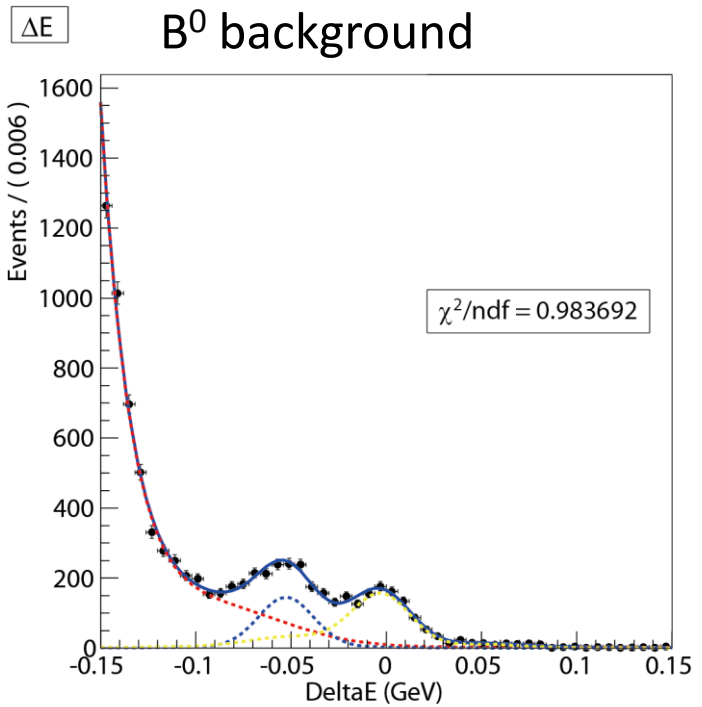
再構成

- $D^* \rightarrow D^0 \pi, D^0 \rightarrow K \pi$ 信号選択

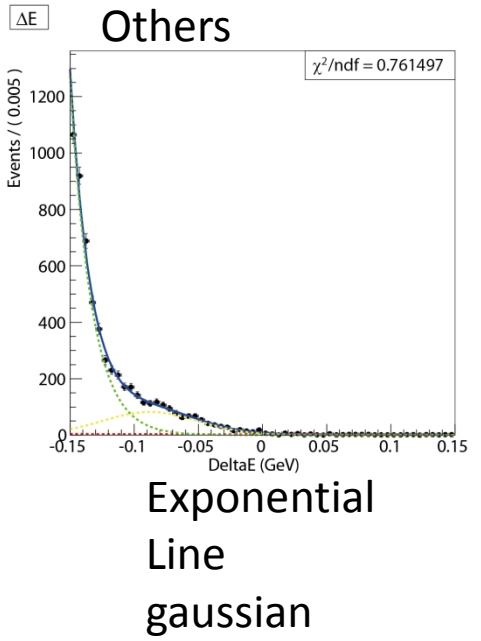
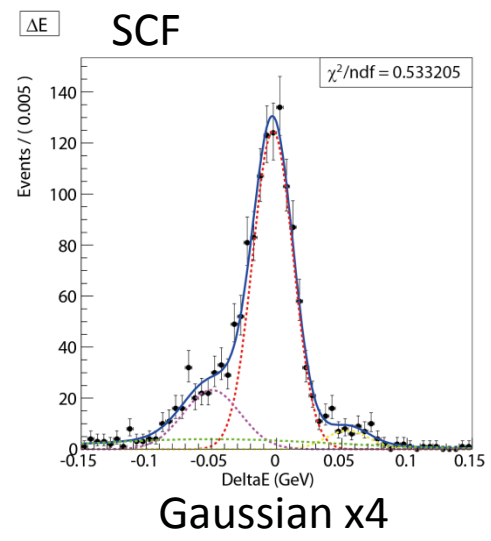
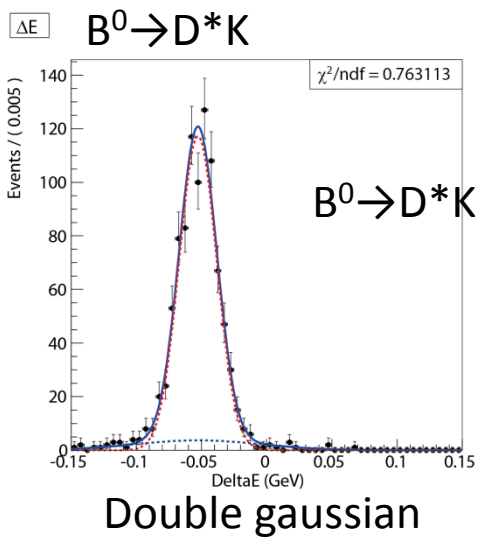
Slow π 以外の π SVD hit in $r-\phi \geq 1, z \geq 2$ $Pid(K/\pi) \leq 0.7$	D^0 $1.82 \text{ GeV} < M_{K\pi} < 1.92 \text{ GeV}$
K SVD hit : π と同じ $Pid(K/\pi) \geq 0.3$	D^* $0.143 \text{ GeV} < M_{D^*} - M_{D^0} < 0.148 \text{ GeV}$
Slow π 要求なし	B $5.2 \text{ GeV} < M_{bc} < 5.3 \text{ GeV}$ $-0.15 \text{ GeV} < \Delta E < 0.15 \text{ GeV}$ 最良候補選択 ($M_{bc}, M_{D^*} - M_{D^0}$)



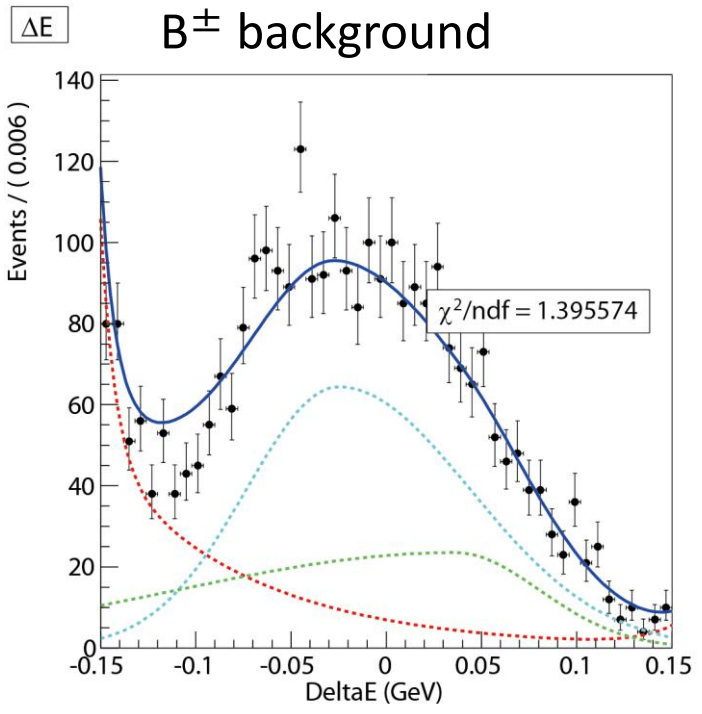
Neutral B BG ΔE PDF



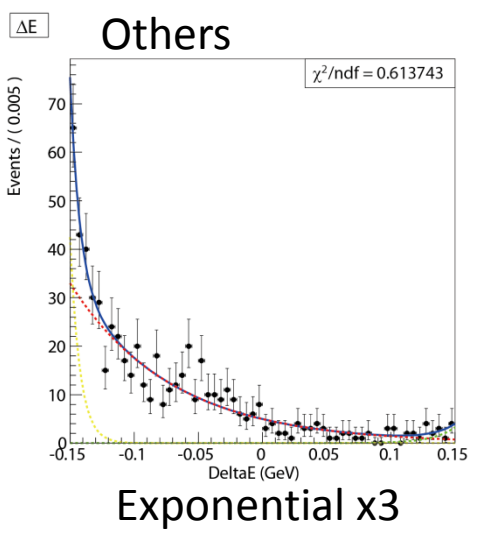
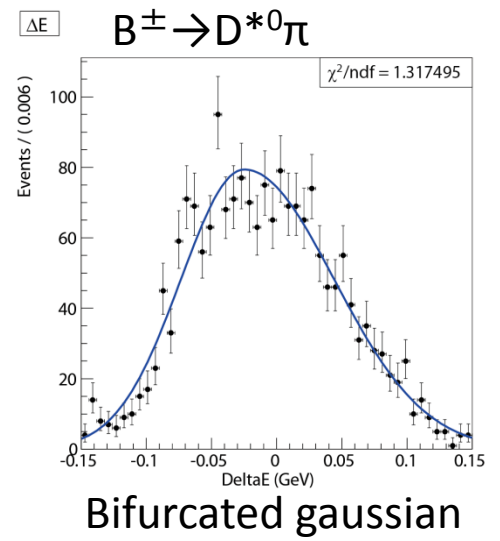
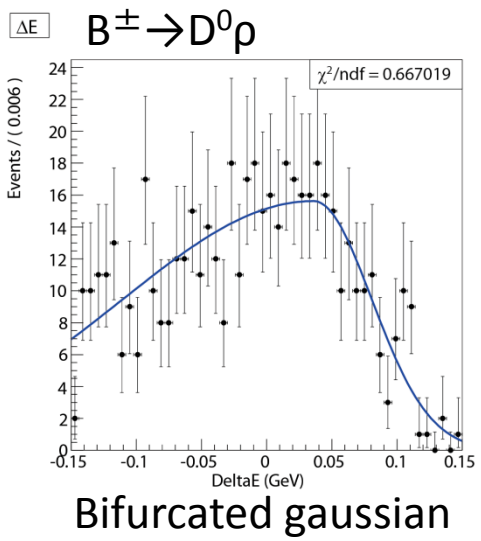
$B^0 \rightarrow D^* K$
SCF
Others



Charged B BG ΔE PDF



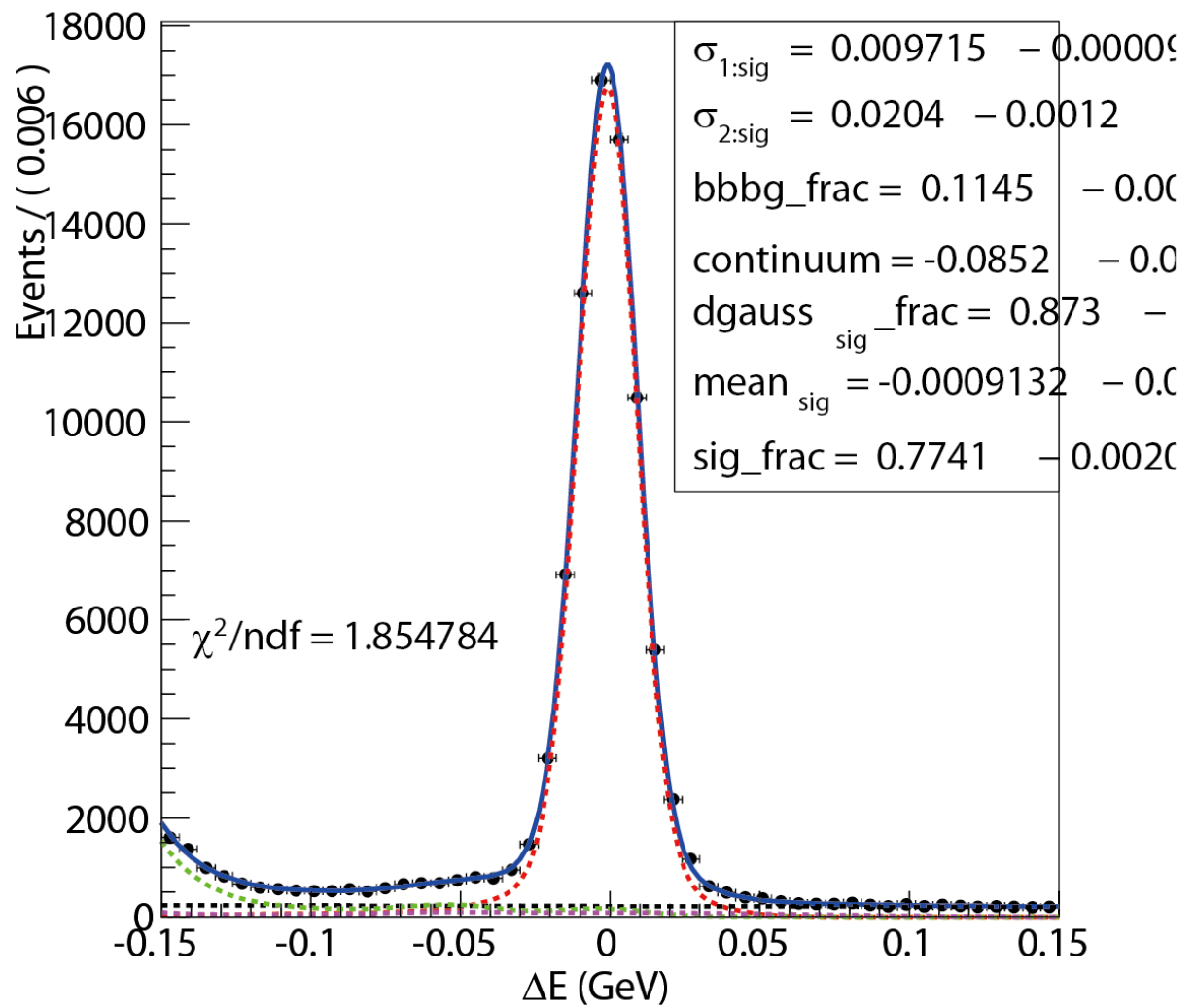
$B^\pm \rightarrow D^0 \pi$
 $B^\pm \rightarrow D^0 \rho$
 Others



B reconstruction

- Generic MC were reconstructed.
 - Case B
 - 5 streams

ΔE



r bin

- r bin : bin definition of the flavor tagging category

R bin #		wrong tag fraction for SVD2 MC	
Bin#0	$0 \leq r \leq 0.1$	$w = 0.5$	$\Delta w = 0.$
Bin#1	$0.1 < r \leq 0.25$	$w = 0.412222$	$\Delta w = 0.0569661$
Bin#2	$0.25 < r \leq 0.5$	$w = 0.307838$	$\Delta w = 0.0126192$
Bin#3	$0.5 < r \leq 0.625$	$w = 0.212765$	$\Delta w = 0.0147724$
Bin#4	$0.625 < r \leq 0.75$	$w = 0.149933$	$\Delta w = 0.000550289$
Bin#5	$0.75 < r \leq 0.875$	$w = 0.0913264$	$\Delta w = 0.00887704$
Bin#6	$0.875 < r \leq 1.0$	$w = 0.0218754$	$\Delta w = 0.00465683$

信号事象の Δt fit

Fit 結果

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*+} \pi^-$$

$$B_{tag} = B^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = B^0, f_{CP} = D^{*+} \pi^-$$

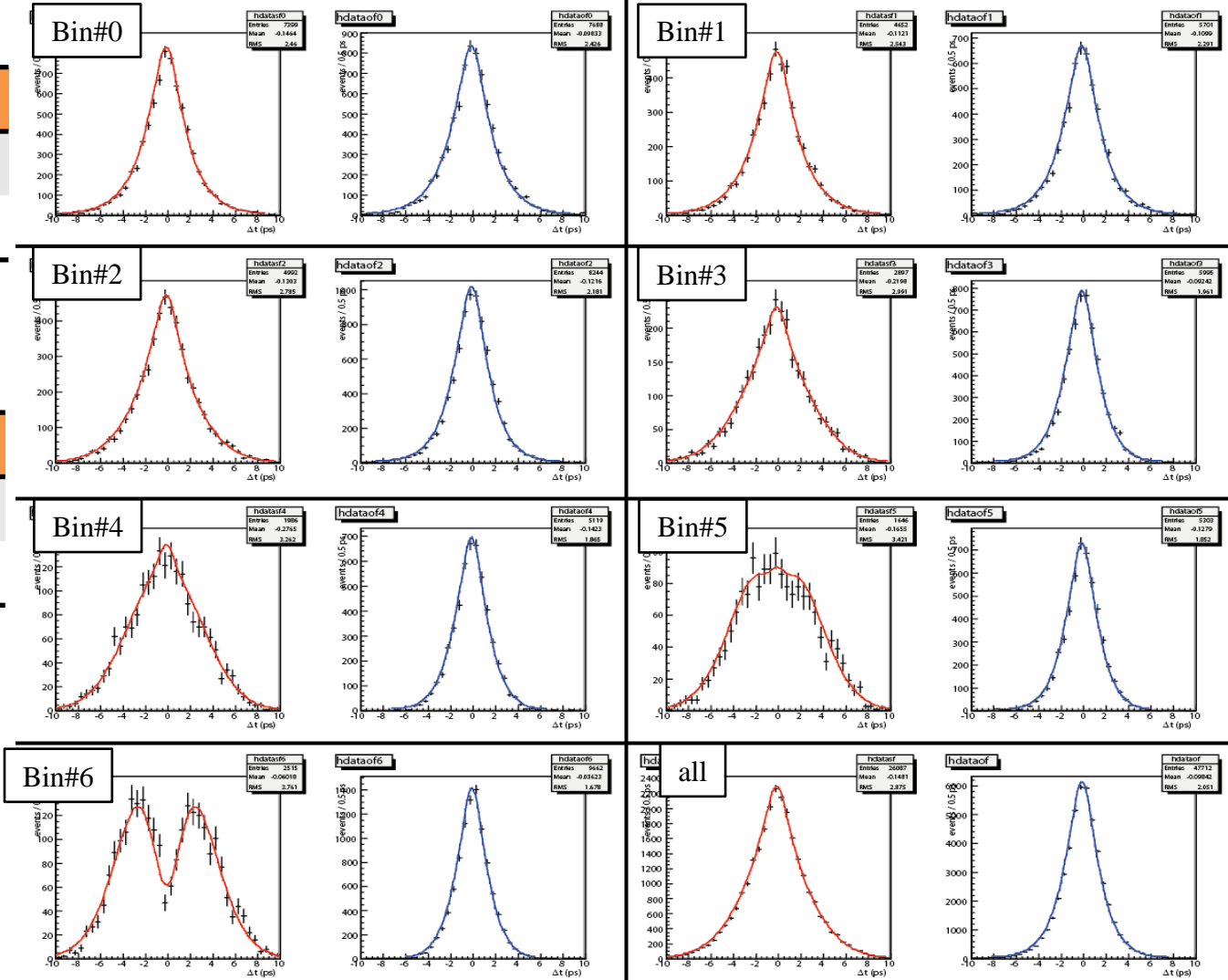
MC 入力値

Name	Value
τ_{B0}	1.534
Δm	0.507

Fit 結果

Name	Value
τ_{B0}	1.533 ± 0.006 (ps)
Δm	0.505 ± 0.004

Fit 結果は入力値と consistent



Signal + $B^0\bar{B}^0$ Background

- To check the correctness of BG PDF, Signal + $B^0\bar{B}^0$ BG was fitted.

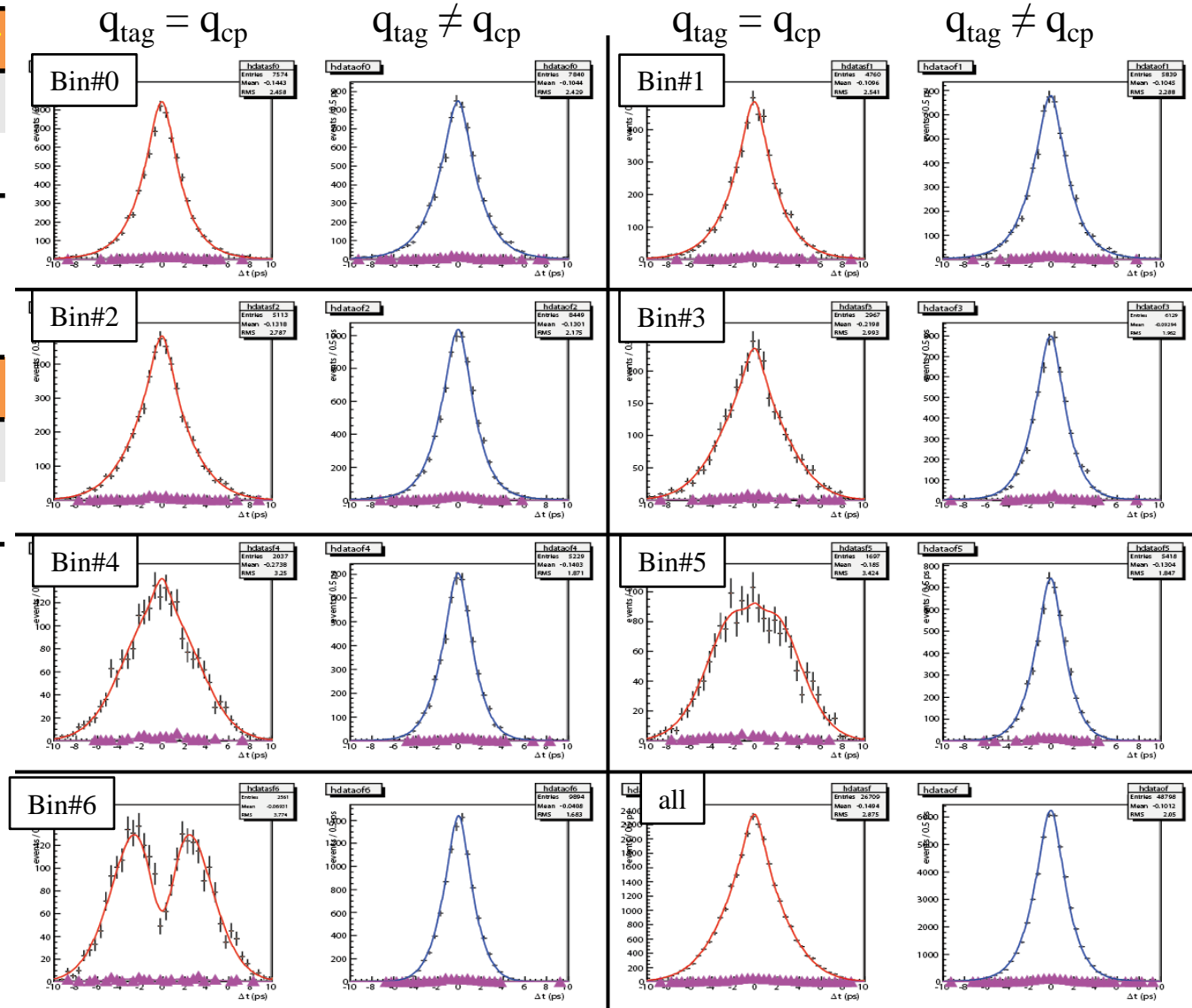
Name	Value	Signal Only
τ_{B^0}	1.533 ± 0.006 (ps)	
Δm	0.505 ± 0.004	

↓

+ $B^0\bar{B}^0$ BG

Name	Value
τ_{B^0}	1.535 ± 0.006 (ps)
Δm	0.505 ± 0.004

- Fit results for signal and signal + $B^0\bar{B}^0$ BG are consistent.
- $B^0\bar{B}^0$ BG PDF were obtained.



Signal + B⁺B⁻ Background

- To check the correctness of BG PDF, Signal + B⁺B⁻ BG was fitted.

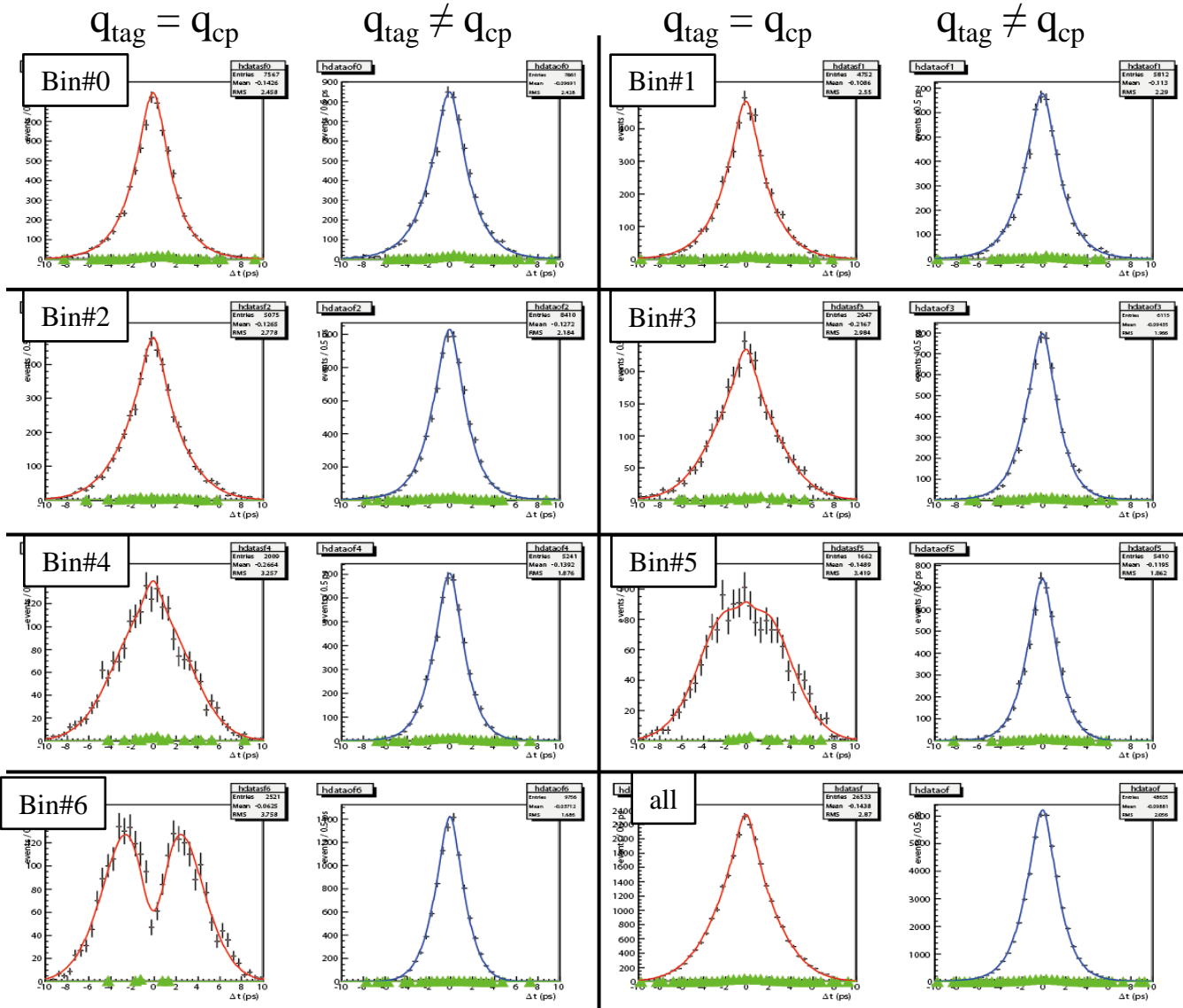
Name	Value	Signal Only
τ_{B0}	1.533 ± 0.006 (ps)	
Δm	0.505 ± 0.004	

↓

+ B⁺B⁻ BG

Name	Value
τ_{B0}	1.535 ± 0.006 (ps)
Δm	0.506 ± 0.004

- Fit results for signal and signal + B⁺B⁻ BG are consistent.
- B⁺B⁻ BG PDF were obtained.



Signal + continuum Background

- To check the correctness of BG PDF, Signal + continuum BG was fitted.

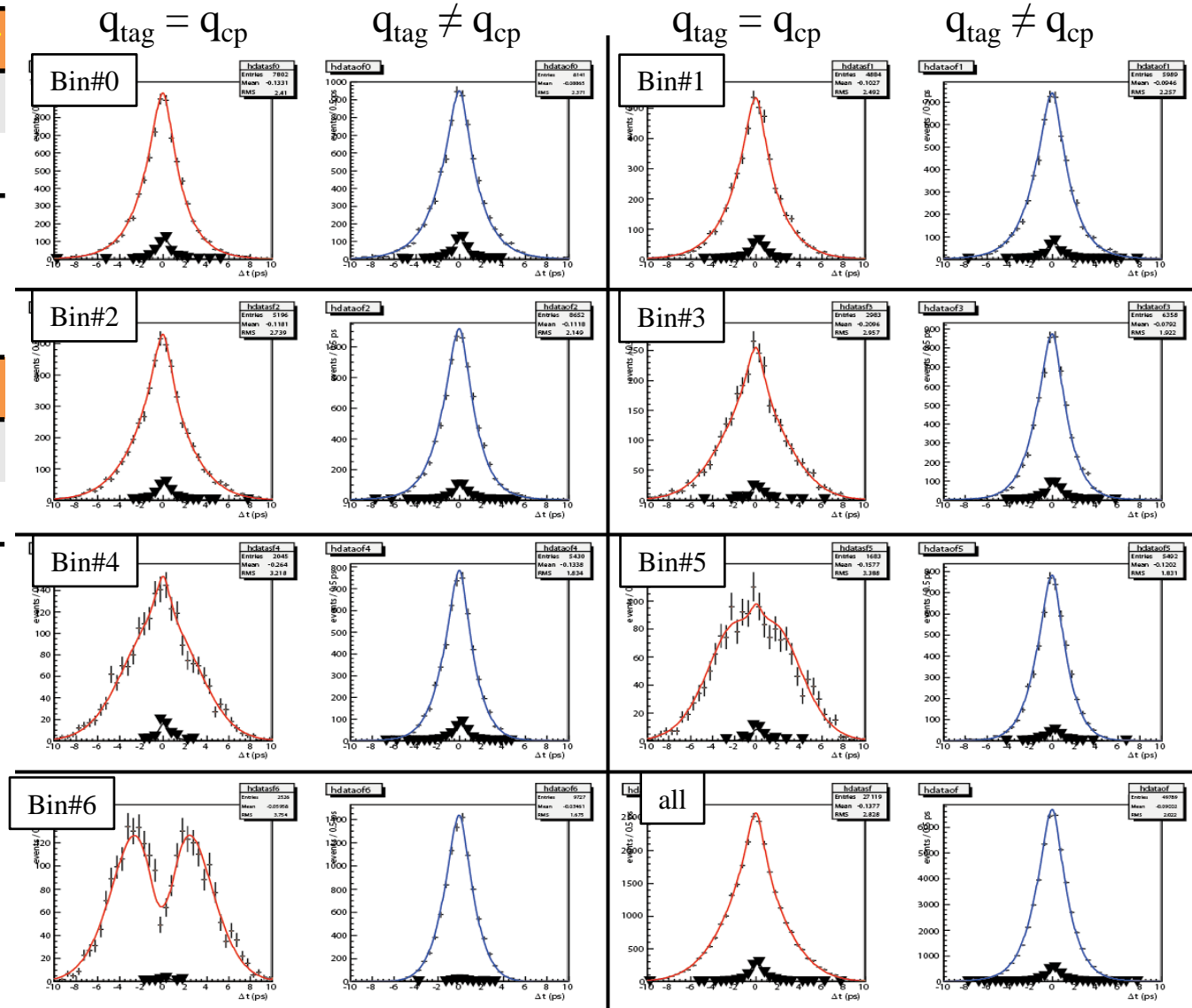
Name	Value	Signal Only
τ_{B0}	1.533 ± 0.006 (ps)	
Δm	0.505 ± 0.004	

↓

+ continuum BG

Name	Value
τ_{B0}	1.534 ± 0.006 (ps)
Δm	0.505 ± 0.004

- Fit results for signal and signal + continuum BG are consistent.
- continuum BG PDF were obtained.



信号事象 + 背景事象

- signal fraction に従って背景事象を加え、信号事象の τ , Δm を fit

Name	Value	信号事象のみ
τ_{B0}	1.533 ± 0.006 (ps)	
Δm	0.505 ± 0.004	

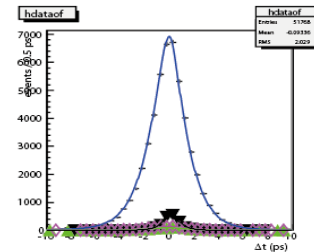
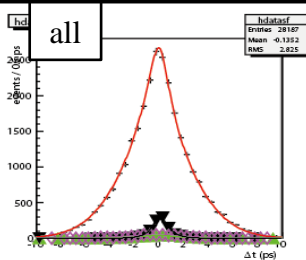
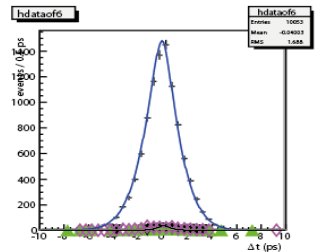
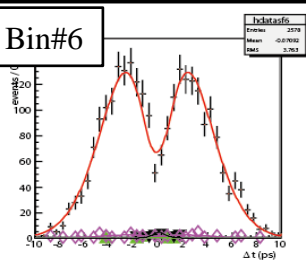
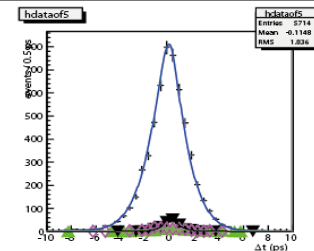
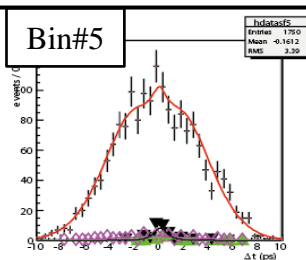
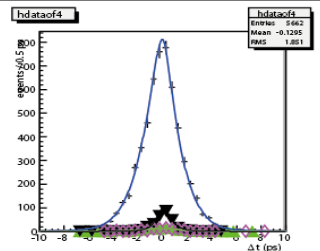
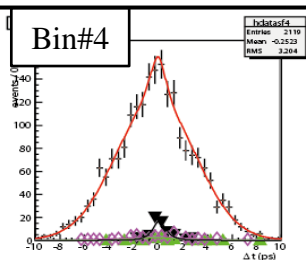
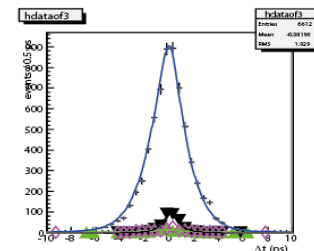
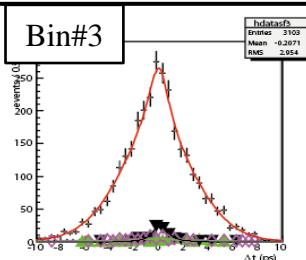
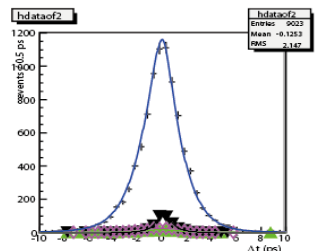
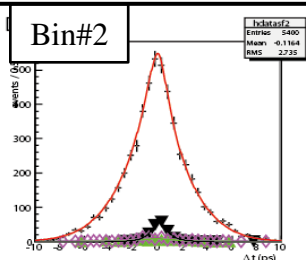
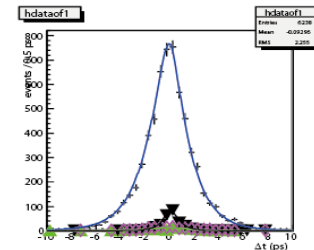
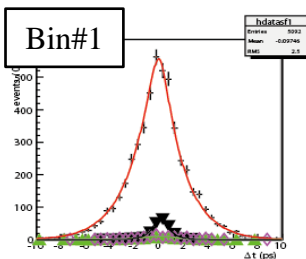
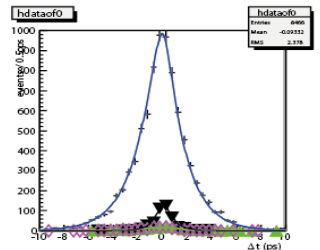
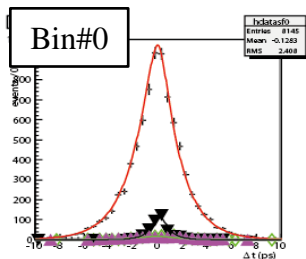


+ 背景事象

Name	Value
τ_{B0}	1.534 ± 0.006 (ps)
Δm	0.506 ± 0.004

Fit 結果は信号事象のみ
と consistent.

背景事象 PDF
が得られた



中性B中間子背景事象の Δt fit

$$P_{B^0BG}(\Delta t, q_{tag}, q_{cp}) = \underbrace{\frac{1}{8\tau_{B^0BG}}}_{\text{寿命項}} e^{-|\Delta t|/\tau_{B^0BG}} \underbrace{\left\{1 - q_{tag} q_{cp} (1 - 2w_{rbin})\right\}}_{\text{Flavor tag 補正}} \underbrace{\cos(\Delta m \Delta t)}_{B^0B^0\text{bar mixing 項}}$$

寿命項

Flavor tag 補正

 $B^0B^0\text{bar}$ mixing 項

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*+} \pi^- \\ B_{tag} &= B^0, f_{CP} = D^{*-} \pi^+ \end{aligned}$$

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*-} \pi^+ \\ B_{tag} &= B^0, f_{CP} = D^{*+} \pi^- \end{aligned}$$

Fit 結果

Name	Value
τ_{B^0BG}	1.525 ± 0.019 (ps)

$$\Delta m = 0.516 \pm 0.013$$

$$w_0 = 0.50 \text{ (fixed)}$$

$$w_1 = 0.45 \pm 0.02$$

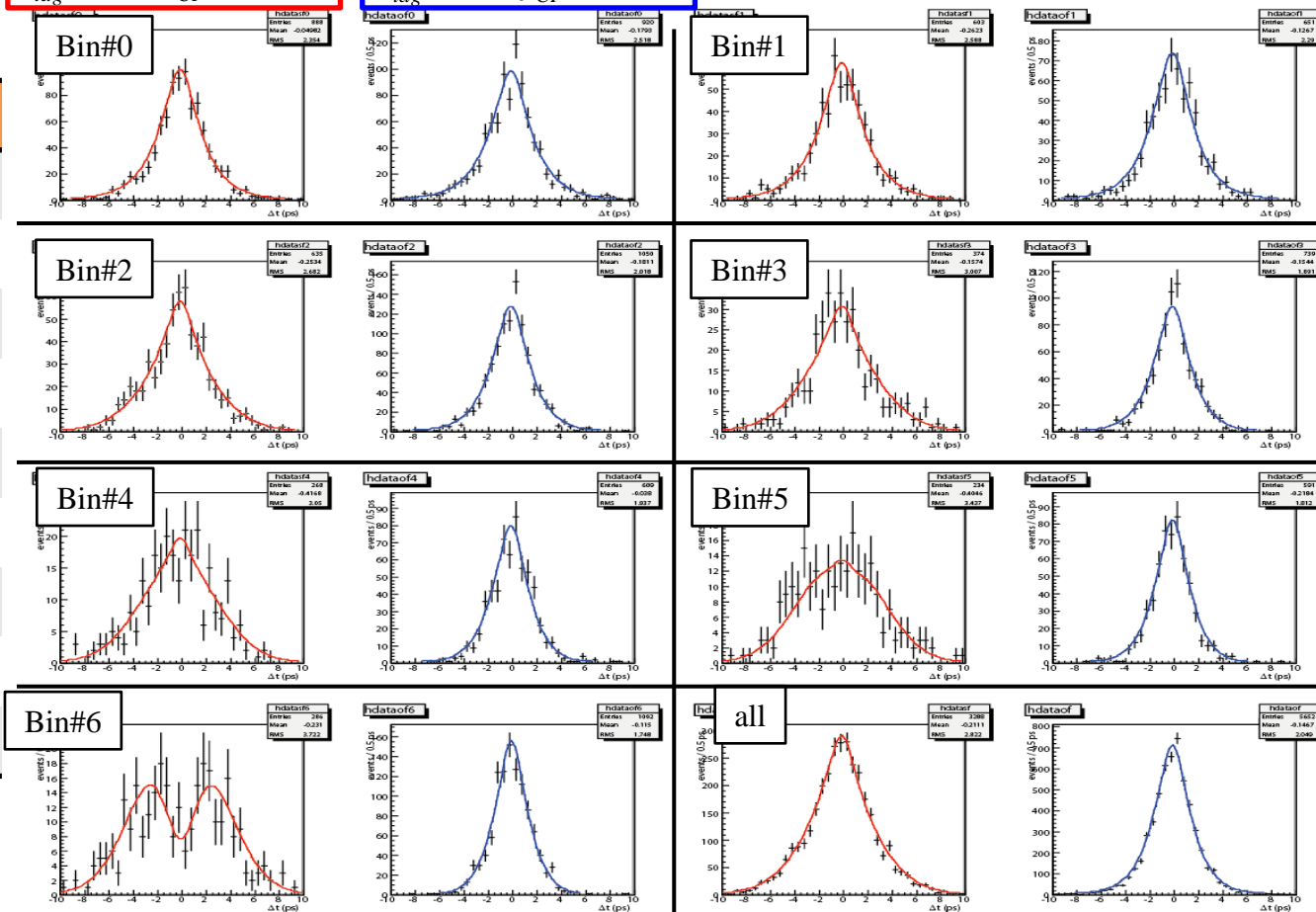
$$w_2 = 0.29 \pm 0.02$$

$$w_3 = 0.23 \pm 0.02$$

$$w_4 = 0.18 \pm 0.02$$

$$w_5 = 0.12 \pm 0.02$$

$$w_6 = 0.03 \pm 0.01$$



荷電B中間子背景事象の Δt fit

$$P_{chg}(\Delta t, q_{tag}, q_{cp}) = \frac{1}{8\tau_{chgB}} e^{-|\Delta t|/\tau_{chgB}} \left\{ 1 - q_{tag} q_{cp} (1 - 2w_{rbin}) \right\}$$

Fit 結果

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*+} \pi^- \\ B_{tag} &= B^0, f_{CP} = D^{*-} \pi^+ \end{aligned}$$

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*-} \pi^+ \\ B_{tag} &= B^0, f_{CP} = D^{*+} \pi^- \end{aligned}$$

Name	Value
------	-------

τ_{chgB}	1.599 ± 0.029 (ps)
---------------	------------------------

w_0	0.50 (fixed)
-------	--------------

w_1	0.44 ± 0.02
-------	-----------------

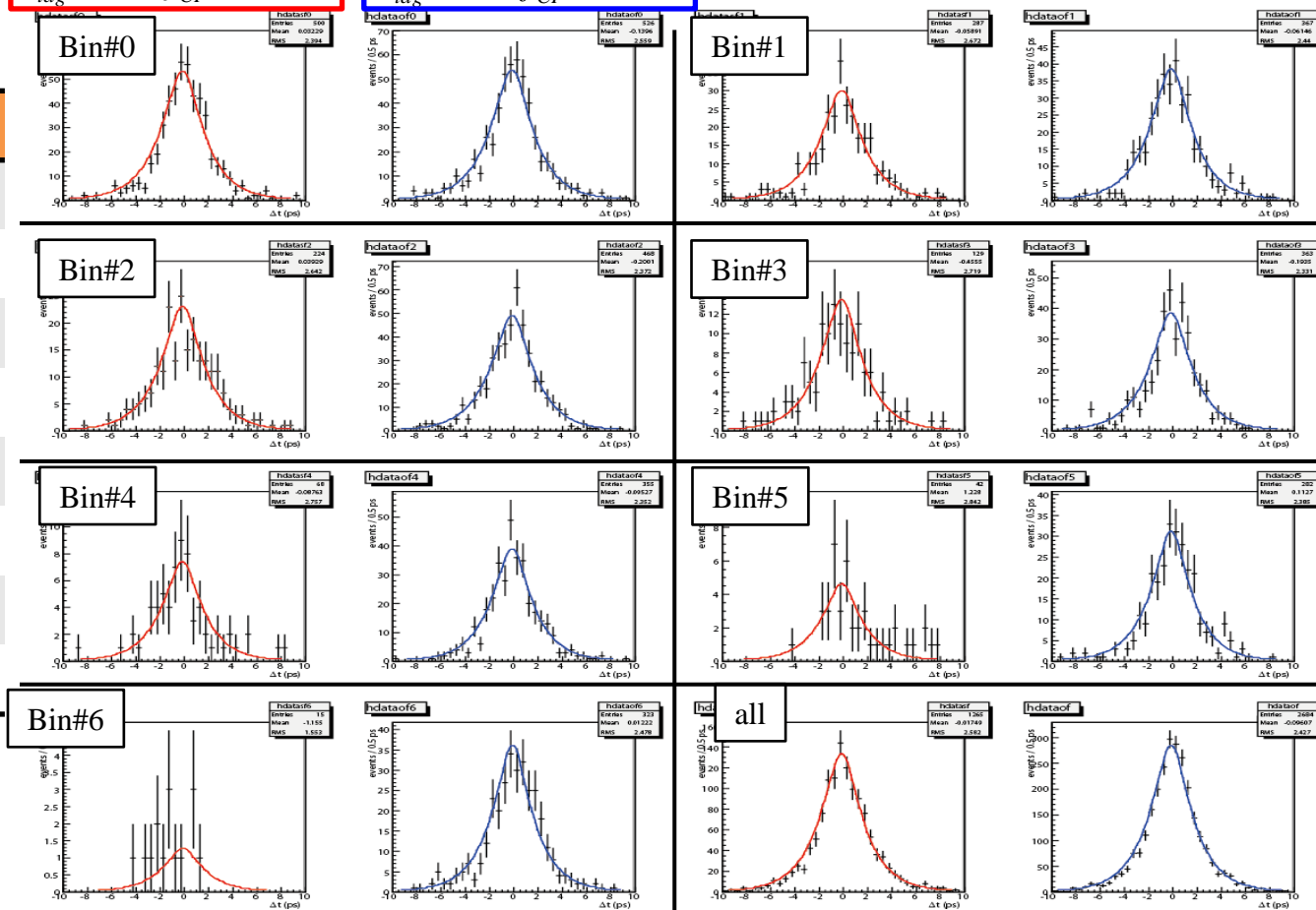
w_2	0.32 ± 0.02
-------	-----------------

w_3	0.26 ± 0.02
-------	-----------------

w_4	0.16 ± 0.02
-------	-----------------

w_5	0.13 ± 0.02
-------	-----------------

w_6	0.04 ± 0.01
-------	-----------------



B以外の背景事象の Δt fit

$$P_{con}(\Delta t) = \int P_{con}(\Delta t') \cdot R_{bkg}(\Delta t - \Delta t') \cdot d\Delta t'$$

$$P_{con}(\Delta t) = f_{\delta} \cdot \delta(\Delta t - \mu_{\delta}) + (1 - f_{\delta}) \cdot \exp\left(-\frac{|\Delta t - \mu_{\tau}|}{\tau_{con}}\right)$$

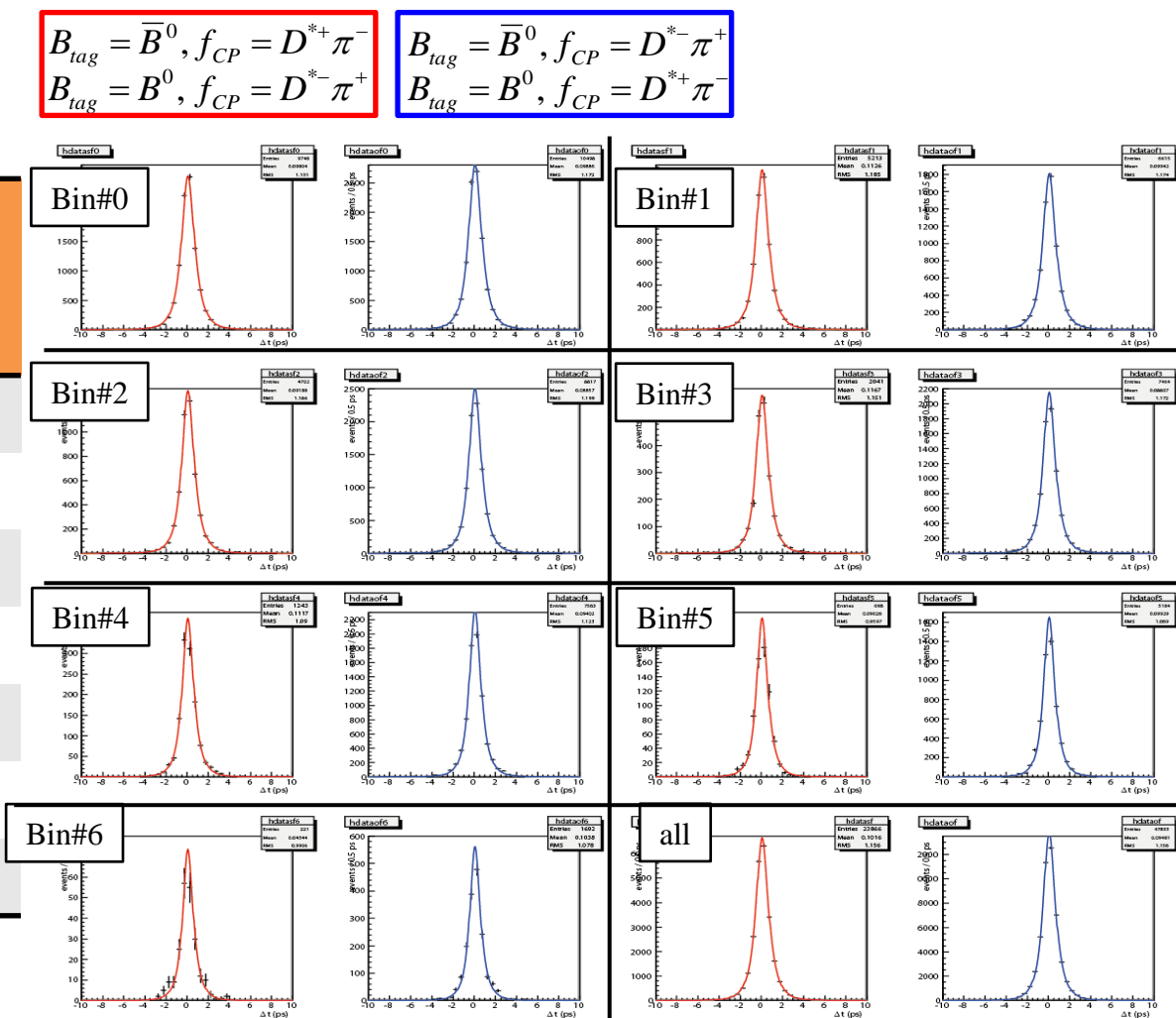
$$R_{con}(\Delta t) = (1 - f_{con}^{tail}) \cdot G(\Delta t; s_{con}^{main} \cdot \sigma_{vtx}) + f_{con}^{tail} \cdot G(\Delta t; s_{con}^{tail} \cdot \sigma_{vtx})$$

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*+} \pi^{-} \\ B_{tag} &= B^0, f_{CP} = D^{*-} \pi^{+} \end{aligned}$$

$$\begin{aligned} B_{tag} &= \bar{B}^0, f_{CP} = D^{*-} \pi^{+} \\ B_{tag} &= B^0, f_{CP} = D^{*+} \pi^{-} \end{aligned}$$

Fit 結果

	Single-track vertex Either CP or tag B	Multi-track vertex Both CP and tag B
f_d	0.26 ± 0.04	0.39 ± 0.02
m_d	0.046 ± 0.007	
m_{τ}	0.14 ± 0.01	
τ_{con}	0.58 ± 0.02	
s_{bkg}^{main}	1.07 ± 0.03	1.34 ± 0.02
s_{bkg}^{tail}	5.40 ± 0.42	4.87 ± 0.26
f_{bkg}^{tail}	0.088 ± 0.010	0.047 ± 0.007



信号事象 + 背景事象での Δt fit

$$P(B^0 \rightarrow D^{*\mp} \pi^\pm) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{8\tau_{B^0}} [1 \pm C \cos(\Delta m \Delta t) - S^\mp \sin(\Delta m \Delta t)]$$

$$P(\bar{B}^0 \rightarrow D^{*\pm} \pi^\mp) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{8\tau_{B^0}} [1 \pm C \cos(\Delta m \Delta t) + S^\pm \sin(\Delta m \Delta t)]$$

• fit results

$\phi_1 + \phi_3 / 2$	ratio	S^\pm (input)	S^+ (diff)	S^- (diff)
0.89685	0.02	-0.039	-0.047 ± 0.021 (0.36 σ)	-0.032 ± 0.021 (0.35 σ)
	0.05	-0.097	-0.099 ± 0.021 (0.11 σ)	-0.12 ± 0.021 (0.98 σ)
	0.1	-0.19	-0.24 ± 0.020 (2.4 σ)	-0.20 ± 0.020 (0.38 σ)
$\pi/2$	0.02	0.0	-0.021 ± 0.021 (0.98 σ)	0.013 ± 0.021 (0.65 σ)
	0.05	0.0	-0.033 ± 0.021 (1.60 σ)	0.014 ± 0.020 (0.69 σ)
	0.1	0.0	-0.020 ± 0.021 (0.96 σ)	-0.016 ± 0.021 (0.78 σ)
$\pi/4$	0.02	-0.040	-0.039 ± 0.021 (0.049 σ)	-0.047 ± 0.021 (0.32 σ)
	0.05	-0.10	-0.13 ± 0.021 (1.49 σ)	-0.11 ± 0.020 (0.28 σ)
	0.1	-0.20	-0.20 ± 0.019 (0.20 σ)	-0.21 ± 0.020 (0.43 σ)