



Measurements of Top quark Mass, Width and Yukawa coupling near threshold at the ILC

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➤ Update of $t\bar{t}$

$\sigma_{t\bar{t}}$ study

– Measurements of

m_t , Γ_t and y_t

➤ A_{FB} study

– Measurements of Γ_t
and α_s

σ_{tt}
(Measurements of “ m_t ”, “ Γ_t ” and “ y_t ”)

σ_{tt} Measurement

Since near the threshold of top pair production ($\sqrt{s}=2m_t$), the energy dependence of σ_{tt} is large, measuring the σ_{tt} precisely and fitting it, fundamental parameters are determined.

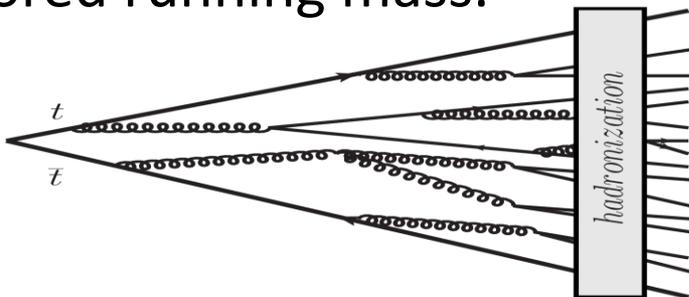
©Well-defined mass

$$\sigma_{tt} \propto f(\sqrt{s}, m_t, \Gamma_t, \alpha_s, y_t, m_h)$$

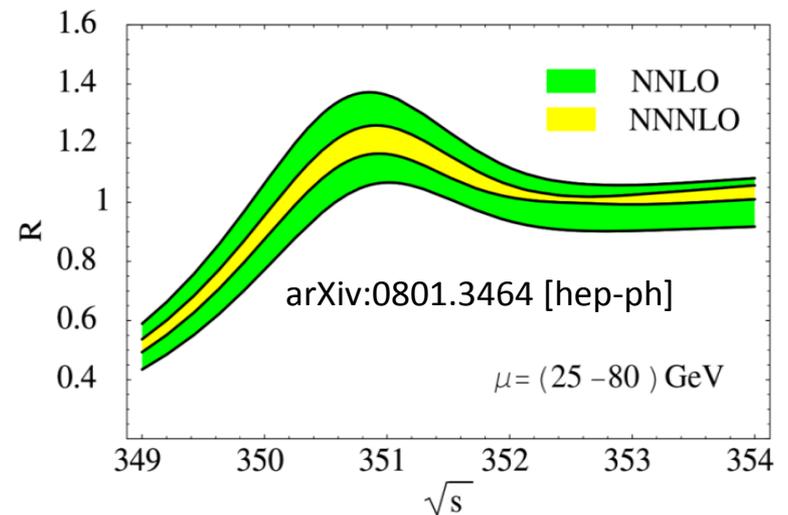
Here **potential subtracted(PS) mass**

Phys.Lett. B434 (1998) 115-125

Invariant mass from three jets is hard to interpret to theoretical favored running mass.



©Theoretical σ_{tt}



$\delta\sigma/\sigma(\text{theoretical}) \sim 4\text{-}5\%$

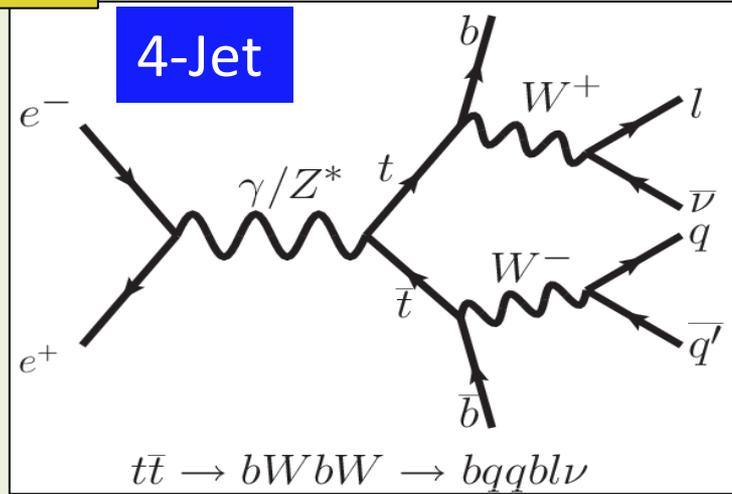
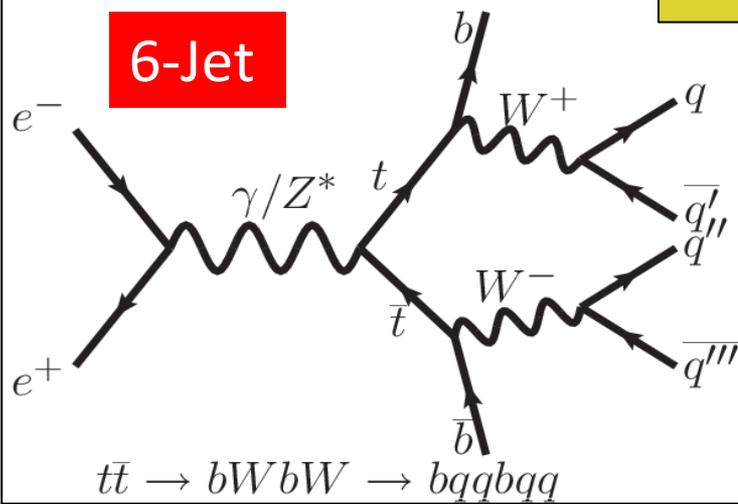
For prediction of m_t with precision of 100 MeV requires $\delta\sigma/\sigma \sim 2\%$

Simulation set up

Top quark mass	174 GeV
\sqrt{s} (<u>threshold scan</u>)	<u>341 - 350 GeV (every 1 GeV, 10 points)</u>
<u>Polarization</u>	$p(e^+, e^-) = (-30\%, +80\%), (+30\%, -80\%)$ (In this talk, I call them “ Right ” and “ Left ”)
Integrated Luminosity	5 fb ⁻¹ (each \sqrt{s} & pol, total 100fb ⁻¹)
Event Generation	Physsim (LO ,QCD enhancement, on ISR/ beamstrahlung/beam energy spread)
Simulation	ILD_01_v05 (DBD ver.)

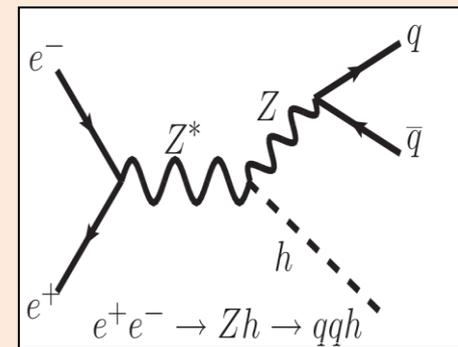
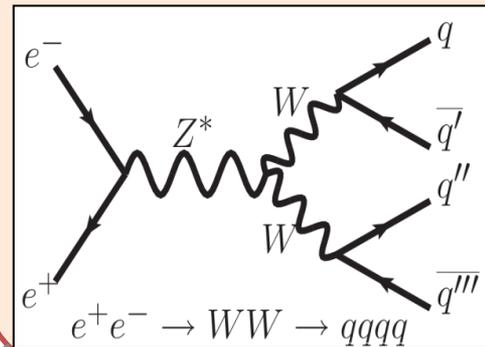
Signal and background

Signal



background

SM bkg. which have 4 or 6 fermions in final state
Main bkg.: WW, ZZ, ZH



Branching Ratio

6-Jet	45%
4-Jet	44%
2-Jet	11%

Top Quark Reconstruction (6-Jet & 4-Jet)

Reconstruction method	6-Jet	4-Jet
Isolated Lepton(l_{iso}) finding using cone energy cut ($\cos\theta_{cone} > 0.96, P_{track} > 15 \text{ GeV}, E_{cone} < 10 \text{ GeV}$)	# of $l_{iso} = 0$	# of $l_{iso} = 1$
Jet clustering using Durham algorithm	6jets	4jets
Extraction of 2 b-likeness jets		
Reconstruction of top quark pair and finding the best candidate by χ^2 from invariant mass	(b+q+q') \times 2	(b+q+q') & (b+ l_{iso} +v)

$$\chi_{6\text{-Jet}}^2 = \frac{(m_{3j^a \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{3j^b \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{2j^a \text{reco.}} - m_w)^2}{\sigma_w^2} + \frac{(m_{2j^b \text{reco.}} - m_w)^2}{\sigma_w^2}$$

$$\chi_{4\text{-Jet}}^2 = \frac{(m_{3j \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{j_l \nu \text{reco.}} - m_t)^2}{\sigma_t^2} + \frac{(m_{2j \text{reco.}} - m_w)^2}{\sigma_w^2}$$

Selection Table @ $\sqrt{s}=350\text{GeV}$

Table : 6-Jet Left handed

$$\int \mathcal{L}(t)dt = 5(\text{fb}^{-1}) \quad S = \frac{N_{\text{Sig}}}{\sqrt{N_{\text{Sig}} + N_{\text{BG}}}}$$

(e+,e-)=(+30,-80%)	tt6j	tt4j	tt2j	SM bkg.	S_{6j}	ε_{6j}
Generated	1643	1583	381	0.13M	4.4	100
# of lepton = 0	1590	353	18	0.11M	5.0	96.8
btag > 0.09 × 2	1499	330	17	19336	10.3	91.2
Thrust<0.825	1439	285	11	2447	22.3	87.6
Evis>300 GeV	1424	61	0	1092	28.0	86.6
m _t >107 GeV × 2	1383	37	0	492	31.6	84.1
# of pfos>84	1376	33	0	442	32.0	83.8
y ₄₅ > 0.0012						
y ₅₆ >0.0006	1362	31	0	392	32.2	82.9
Sphericity>0.22	1347	24	0	329	32.7	82.0

√s=350 GeV	S_{n-Jet}	ε_{n-Jet}
6-Jet (e+,e-)=(-30, +80%)	23.5	84.6
4-Jet (e+,e-)=(+30, -80%)	31.0	66.3
4-Jet (e+,e-)=(-30, +80%)	21.9	68.2

toyMC to extract m_t , Γ_t , y_t

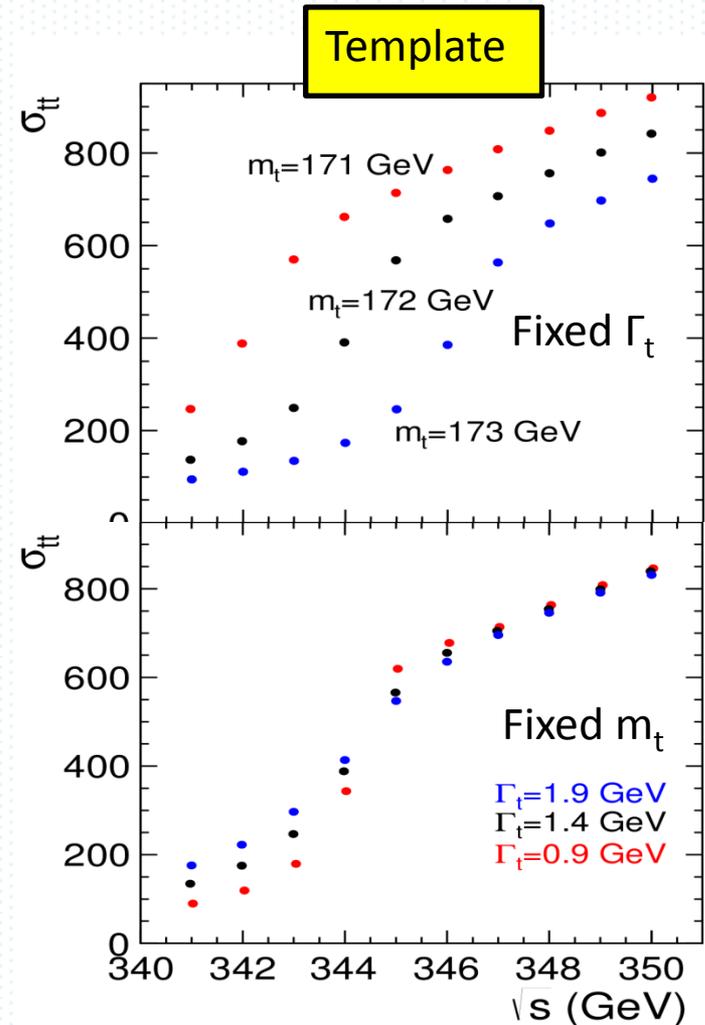
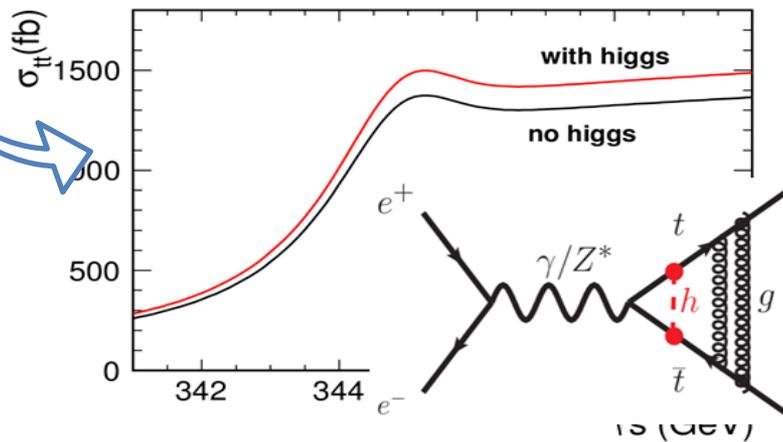
➤ Preparing the Templates:

- Theoretical σ_{tt} is convoluted using luminosity spectrum.
- Making the template by changing m_t^{PS} and Γ_t / Fixed $\alpha_s (=0.12)$

➤ Fitting to σ_{tt} :

- Since the measurement of δy_t is extracted from normalization of σ_{tt} , the normalization is used for σ_{tt} fit.
- By using the templates, σ_{tt} s are fitted to extract y_t , m_t and Γ_t simultaneously.

new



Fit Result

Stat. Error (m_t, Γ_t :MeV/ y_t :%)	6-Jet			4-Jet		
	m_t^{PS}	Γ_t	y_t	m_t^{PS}	Γ_t	y_t
Left(50fb ⁻¹)	47	65	9.6	52	71	11
Right(50fb ⁻¹)	68	94	14	75	106	16
Left (50fb ⁻¹) + Right(50fb ⁻¹)	39	53	7.9	43	59	9.1

Combined ALL

m_t^{PS} (GeV)	Γ_t (GeV)	y_t
172 ± 0.029	1.4 ± 0.039	5.9 %

Systematic err.

- Theoretical err.
 $\delta m_t \sim 100 \text{ MeV}$
- Luminosity spectrum
 $\delta m_t \sim 80 \text{ MeV}$

Ph.D thesis F. Gournaris (2009)

⊙ $\overline{PS} \rightarrow \overline{MS}$

$$m_t^{\overline{MS}} \sim m_t^{PS} - \frac{4}{3\pi} (m_t^{PS} - 20) \alpha_s + \dots$$

$$m_t^{\overline{MS}} = 163.800 \pm 0.028 \text{ (stat.) (GeV)}$$

Comparison of (2+1) param fits and 3 param fits

previous result : 2D fit of m_t and Γ_t , y_t is measured individually.

New result : **3D fit** of m_t , Γ_t and y_t .

	(2 + 1) param fit	3 param fit
m_t	19 MeV	29 MeV
Γ_t	38 MeV	39 MeV
y_t	4.6%	5.9%

Correlation coefficients

	(2 + 1) param fit	3 param fit
m_t vs Γ_t	0.52	0.57
m_t vs y_t	-	0.72
Γ_t vs y_t	-	0.33

A_{FB}

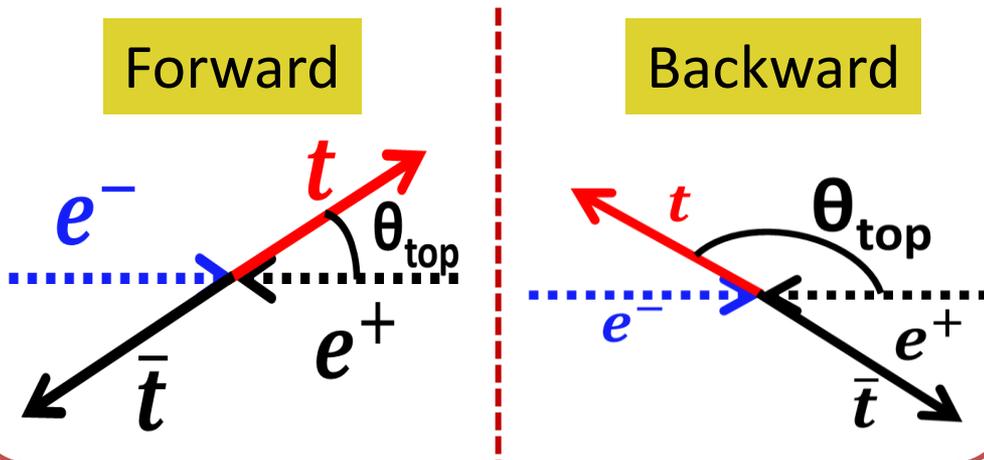
(Measurement of “ Γ_t ”, “ α_s ”)

A_{FB} near $t\bar{t}$ threshold

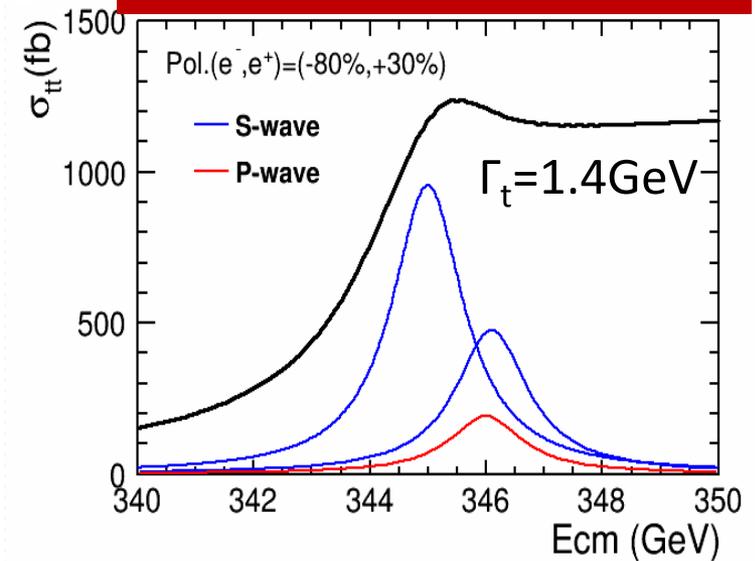
★ Forward backward asymmetry of top quark (A_{FB})

- Since top has large Γ_t , we can measure A_{FB} by interfering the resonance of S- and P- wave.
- The level split which is separation of two resonances depends on α_s .

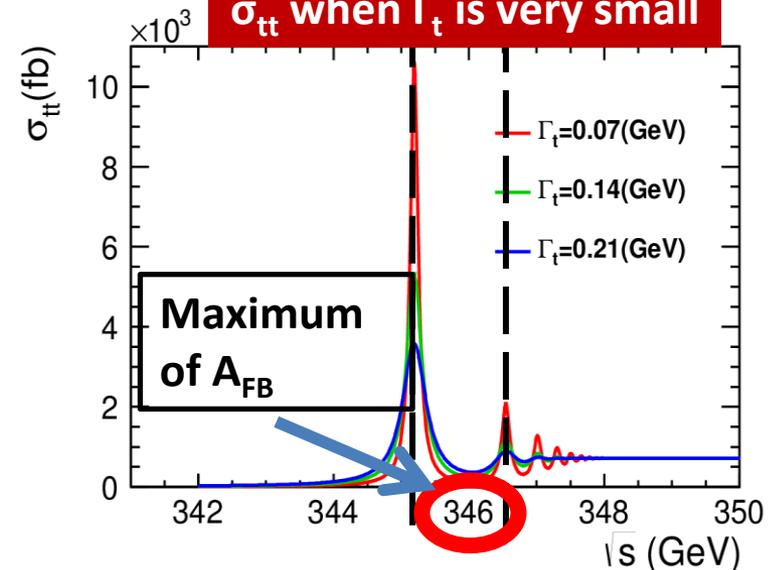
$$A_{FB} \equiv \frac{N(\cos\theta_{top} > 0) - N(\cos\theta_{top} < 0)}{N(\cos\theta_{top} > 0) + N(\cos\theta_{top} < 0)}$$



Interference of S- and P-wave

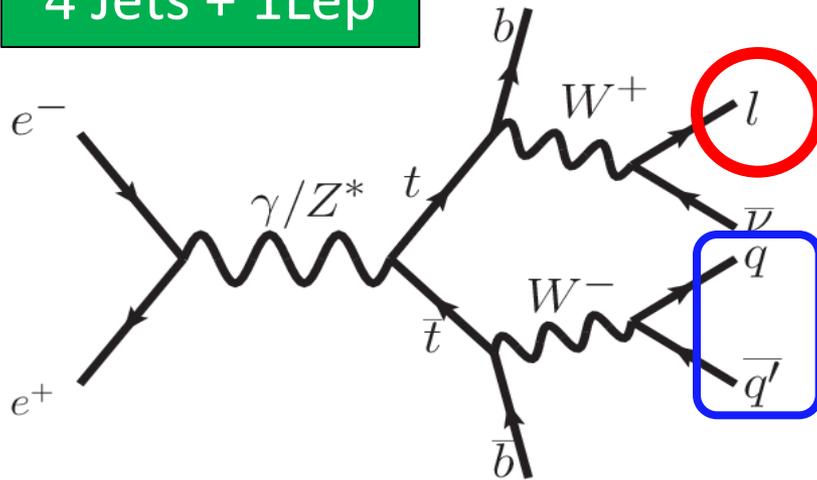


σ_{tt} when Γ_t is very small



Analysis method and MC Set up

Signal
4 Jets + 1Lep



$$t\bar{t} \rightarrow bWbW \rightarrow bqql\nu$$

○ Semi-leptonic side

Since charge tag of jets is too difficult, isolated lepton is used for ID of top or anti-top.

○ Hadronic side

Since leptonic decayed top quark has missing 4-vector, hadronic decayed one is used to determine angle of top quark.

Set up

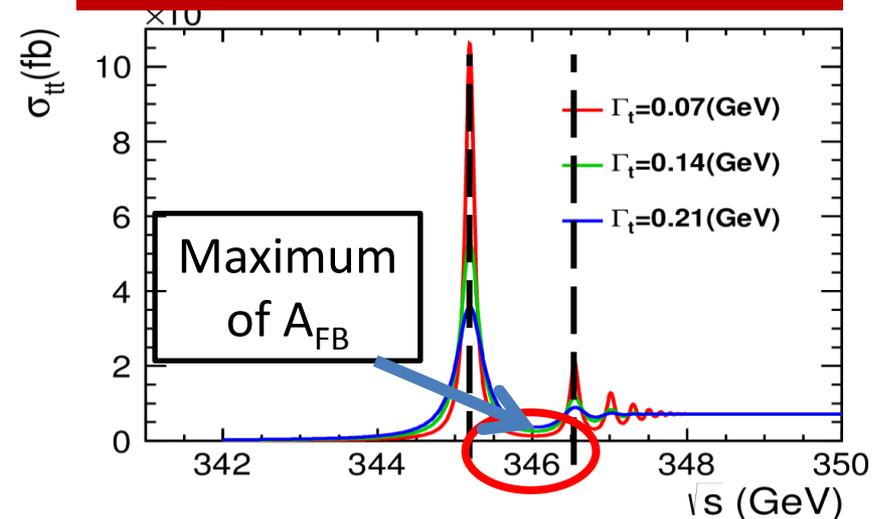
BKG. : SM bkg.

$\sqrt{s} = 346 \text{ GeV}$ (between S- and P- wave)

$\mathcal{L} = 50\text{fb}^{-1}$ (e^+, e^-) = (+0.3, -0.8)

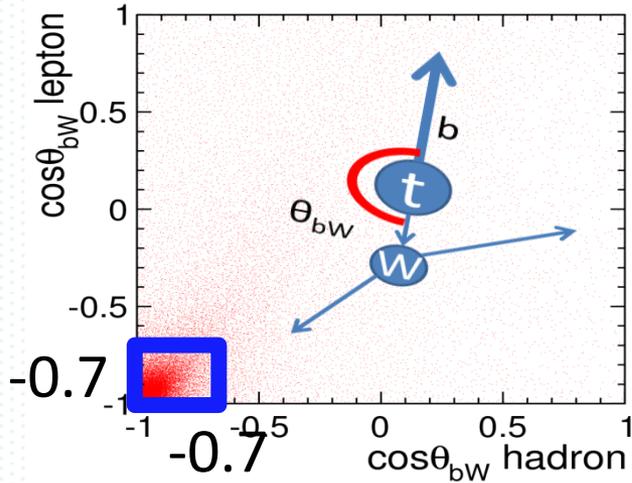
$\mathcal{L} = 50\text{fb}^{-1}$ (e^+, e^-) = (-0.3, +0.8)

$\sigma_{t\bar{t}}$ when Γ_t is very small

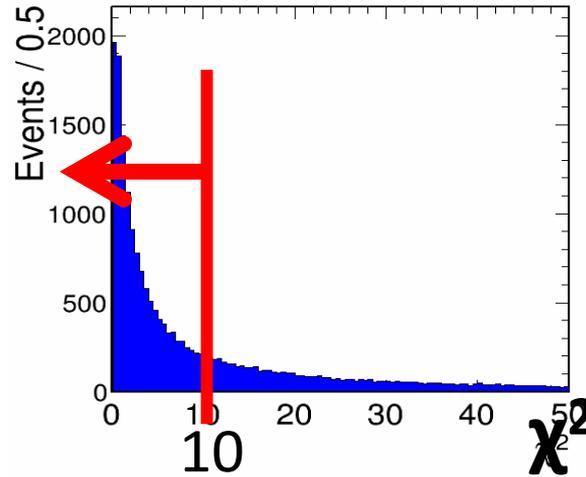


Reconstruction of top quark

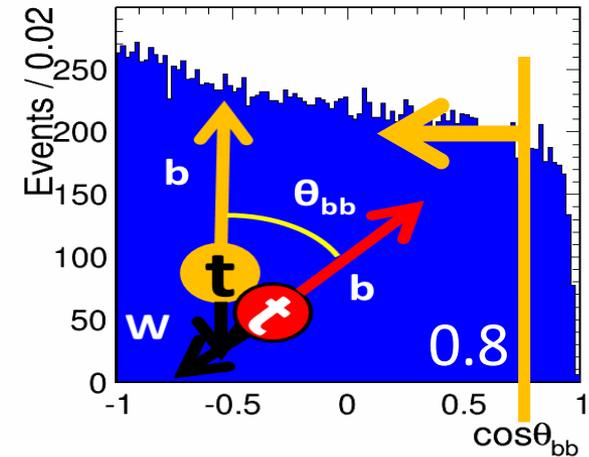
Angle of b and W
at rest frame



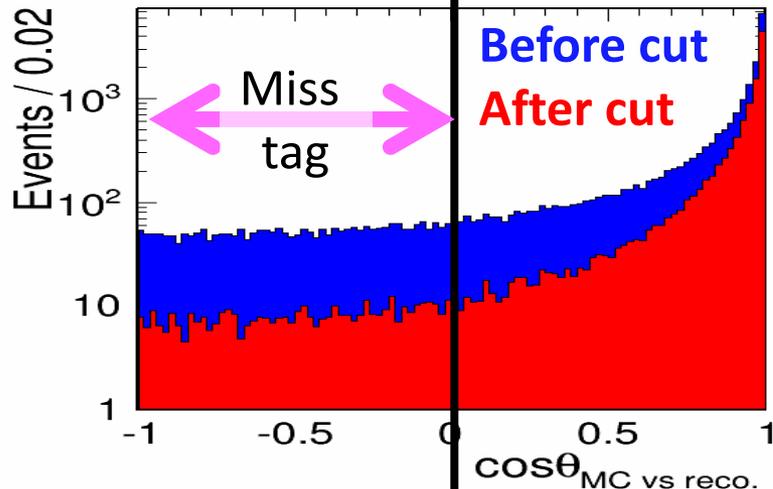
χ^2 from mass



Closeness
of 2 b quarks



Cos $\theta_{(MCtruth vs MCreco.)}$



$$\chi^2 = \frac{(m_t - m_{3j})^2}{\sigma_t^2} + \frac{(m_t - m_{jl\nu})^2}{\sigma_t^2} + \frac{(m_w - m_{2j})^2}{\sigma_w^2}$$

Cut for top ID

$$\cos\theta_{bW} < -0.7, \chi^2 < 10, \cos\theta_{bb} < 0.8$$

Misreconstruction is reduced.

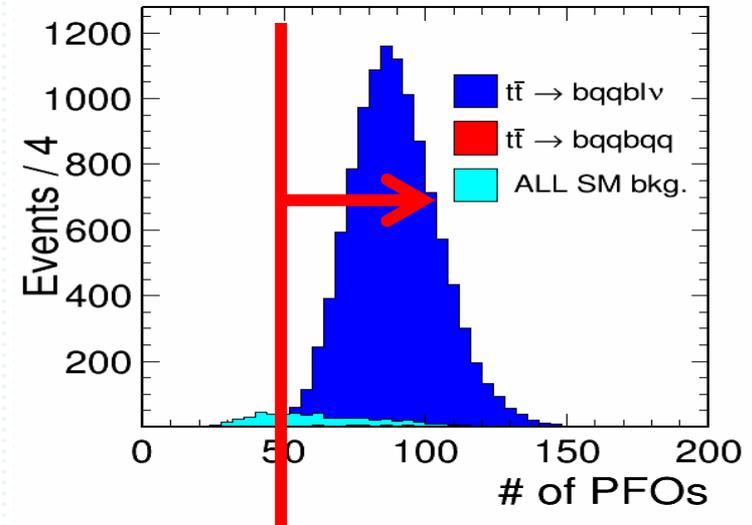
13% \Rightarrow 3.7%

Background suppression

- For maximizing the significance (S_{top}), bkg. are rejected.

$$S_{top} = \frac{N_{signal}}{\sqrt{N_{signal} + N_{bkg.}}}$$

- # of PFOs is used except top tagging cut (previous page).



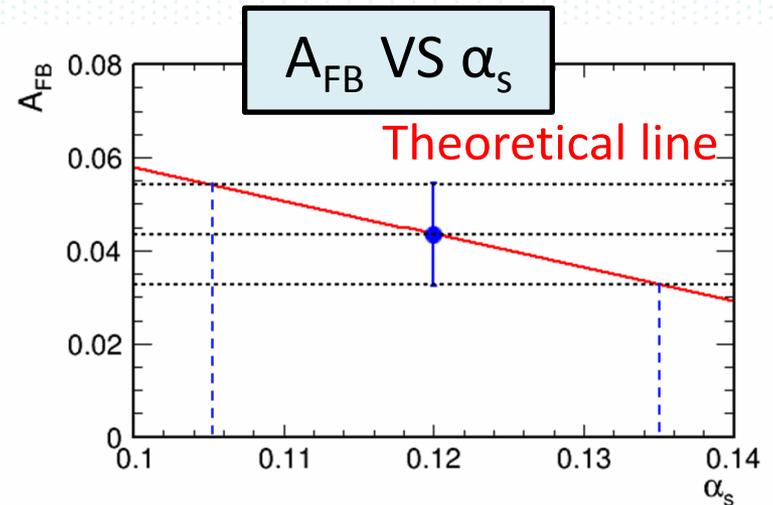
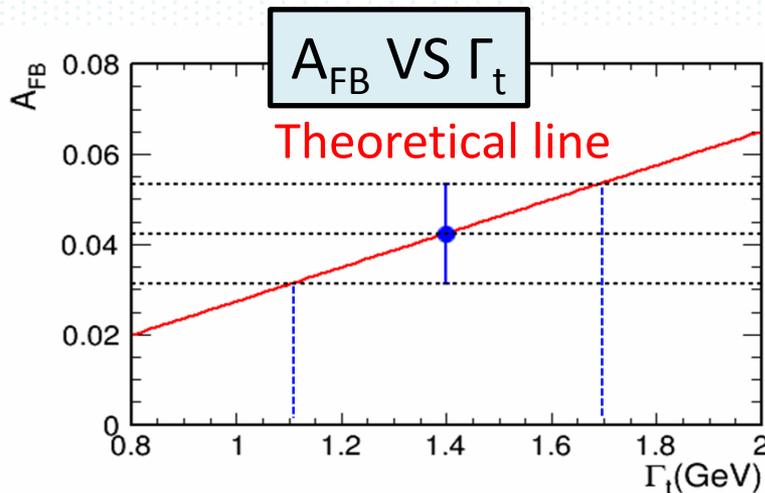
Left 50fb ⁻¹	tt4j	tt6j	tt2j	SM bkg.	S_{top}	Efficiency
Gen.	12619	13101	3039	1 M	12.2	100
# of $l_{iso} = 1$	9648	418	909	0.3M	16.9	76.5
$\cos\theta_{bW} < -0.7$	8989	397	834	0.2M	18.4	71.2
$\chi^2 < 10$	6856	65	164	13134	48.2	54.3
$\cos\theta_{bb} < 0.8$	4881	3	6	271	67.9	38.7
# of PFOs > 50	4872	3	4	182	68.5	38.6

Γ_t and α_s measurement

From the 1σ error, we estimate the accuracy of Γ_t and α_s .

Center value is $A_{FB} = 0.0427$

50 fb ⁻¹	# of events (NNLO)	δA_{FB}
Left handed	5537	0.013
Right handed	2564	0.020
Left + Right (100 fb ⁻¹)	8101	0.011



Red lines show theoretical line assuming polarization of $(e^+, e^-) = (0, 0)$. Theoretical calculation for polarized case is not calculated. In the future when ILC will be built, theorists will calculate it.

$$\mathcal{L} = 100 \text{ fb}^{-1} \quad \underline{\delta\Gamma_t = 290 \text{ MeV}, \delta\alpha_s = 0.015}$$

Summary

- σ_{tt} measurement (mass, width, y_t)
 - Simultaneous fit to extract m_t , Γ_t and y_t was performed.
 - Integrated luminosity : $5 \text{ fb}^{-1} \times 20$ points, total 100 fb^{-1}
 - We can measure at $\delta m_t^{\text{PS}} = 29 \text{ MeV}$, $\delta \Gamma_t = 39 \text{ MeV}$ and $\delta y_t = 5.9 \%$ with 3D fit.

- A_{FB} measurement
 - Near $t\bar{t}$ threshold, A_{FB} measurement is sensitive to Γ_t and α_s .
 - At $\sqrt{s}=346 \text{ GeV}$ where A_{FB} is maximum, δA_{FB} of top quark were measured and $\delta \Gamma_t$ and $\delta \alpha_s$ are estimated.
 - If we accumulate $\mathcal{L} = 100 \text{ fb}^{-1}$, we can measure at $\Gamma_t = 290 \text{ MeV}$ and $\delta \alpha_s = 0.015$.
 - Theoretical predictions of A_{FB} vs Γ_t and α_s for polarized case exist but not calculated numerically.

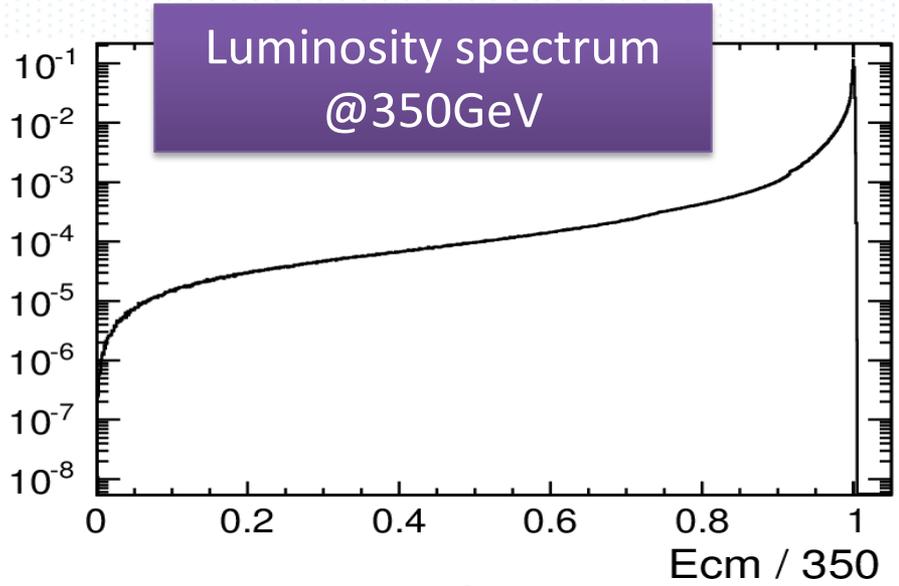
backup

Fit - convolution -

© We must consider **“Beam effects”** around threshold.



Using luminosity spectrum,
theoretical cross section is convoluted.



$$\sigma_{conv.}(\sqrt{s}) = \int \mathcal{L}(t) \sigma_{th}(t) dt$$

\mathcal{L} : luminosity spectrum, \sqrt{s} : nominal, σ_{th} : theoretical σ ,
 $\sigma_{conv.}$: convoluted σ , $t(=\sqrt{s'/s})$ where $\sqrt{s'}$ is collision energy

