

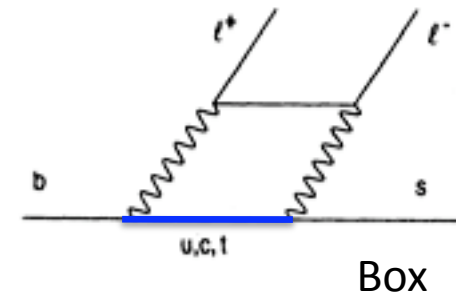
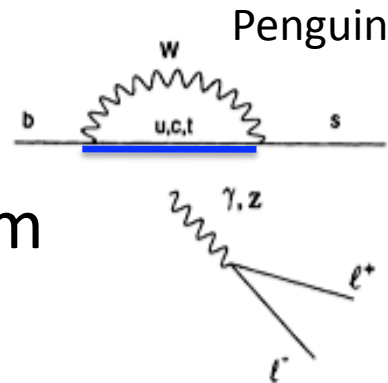
Measurement of the Differential Branching Fraction and Forward- Backward Asymmetry for $B \rightarrow K^{(*)} l^+ l^-$

1/12 論文購読
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Motivation

- $b \rightarrow s l^+ l^-$

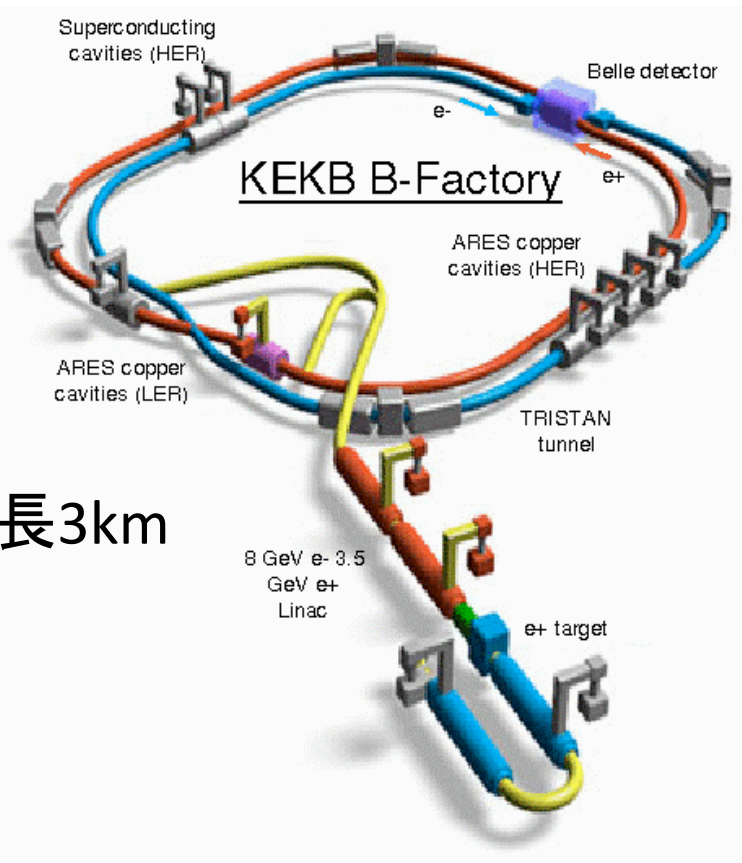
- Z/γ penguin diagram
- $W^+ W^-$ box diagram



- In various extended models some expectations differ from SM's
 - A_{FB} : Lepton forward-backward asymmetry
 - $B(B \rightarrow K^* l l)$: Differential branching fraction
- Searching for the beyond SM clue

Belle実験

KEKB加速器：電子(e^-)8.0GeV、陽電子(e^+)3.5GeV
重心エネルギー10.6GeVの非対称衝突型加速器
(10.6GeV = B中間子一対がしきい値で生成)

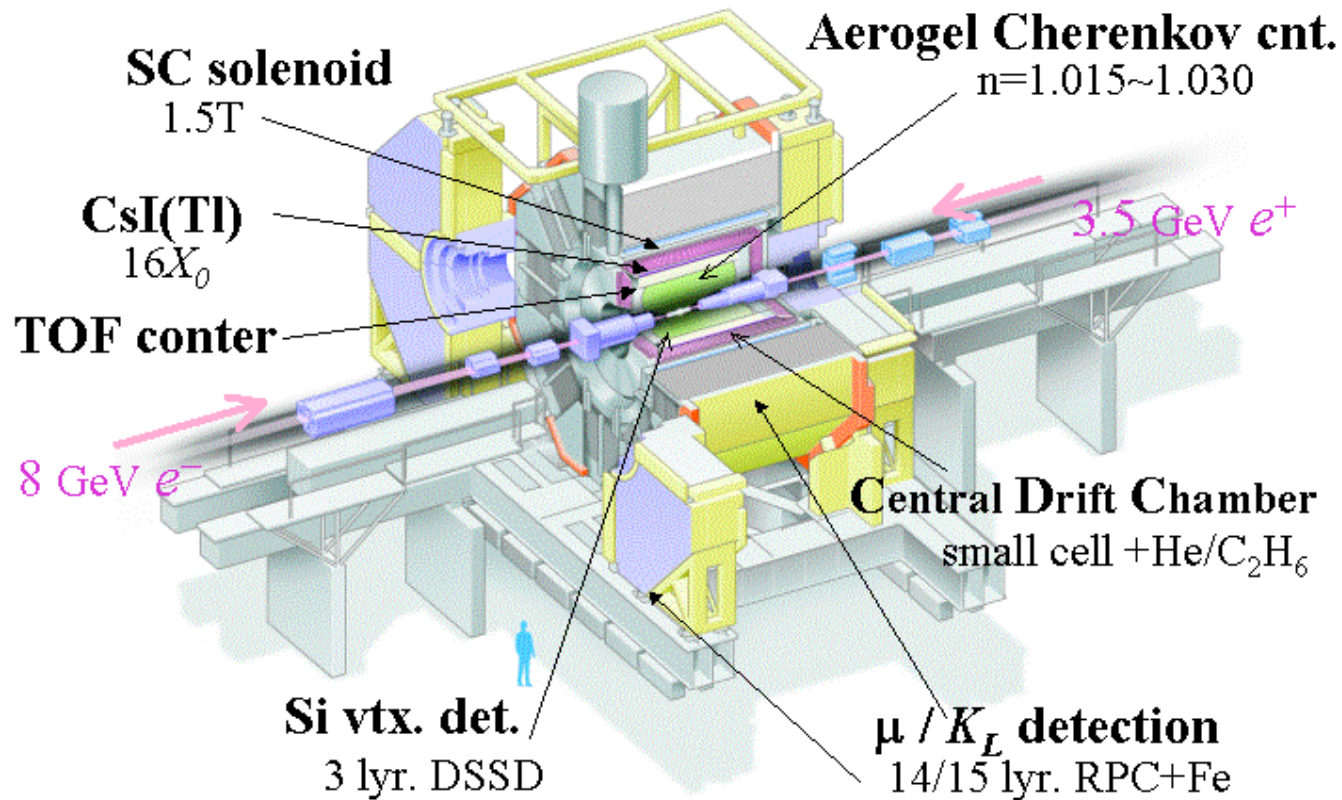


周長3km

e^-e^+ 衝突器として世界一のルミノシティ

B中間子の崩壊はBelle検出器でとらえる

Belle Detector



Belle検出器はいくつかのサブ検出器からなる

Measurement

- $q^2 (= M_{ll}^2)$: dilepton invariant mass
 - Differential branching fraction
 - F_L : K^* longitudinal polarization fraction
 - A_{FB} : lepton forward-backward asymmetry
 - A_I : Isospin asymmetry

Sample Data

- 605 fb^{-1} @Belle
= $657 * 10^6$ BB pairs
- $B \rightarrow K^{(*)} l^+ l^-$
 - $K^{(*)} \rightarrow K^+ \pi^-, Ks^0 \pi^+, K^+ \pi^0, K^+, Ks^0$
 - $l^+ l^- = \mu^+ \mu^-$ or $e^+ e^-$

Selection criteria

- All charged track are associated with the IP (other than $K_s^0 \rightarrow \pi^+\pi^-$)
- Particle ID
 - K : efficiency $> 85 \%$, remove $\pi > 92 \%$
 - π : efficiency $> 89 \%$, remove K $> 91 \%$
 - μ : retain $93.4 \pm 2.0 \%$, remove $98.8 \pm 0.2 \%$ π
 - e : retain $92.3 \pm 1.7 \%$, remove $99.7 \pm 0.1 \%$ π
 - e^\pm is contained neutral clusters (20 ~ 500 MeV) within 50 mrad. \leftarrow Bremsstrahlung γ

Reconstruction (K_s^0 , π^0)

- Pairs of opposite charged tracks are $K_s^0 \rightarrow \pi^+\pi^-$ candidates (483 ~ 513 MeV)
- K_s^0 vertex direction and distance from IP
- $\pi^0 \rightarrow \gamma\gamma$ candidates are required m_{π^0} , minimum γ energy, γ energy asymmetry, π^0 momentum.

Reconstruction (B)

$$M_{bc} \equiv \sqrt{E_{\text{beam}}^2 - p_B^2}$$
$$\Delta E \equiv E_B - E_{\text{beam}}$$

- B candidate
 - $5.20 \text{ GeV} < M_{bc}$
 - $-35 < \Delta E < 35 \text{ MeV}$ ($l = \mu$)
 - $-55 < \Delta E < 35 \text{ MeV}$ ($l = e$)
 - $K^* : M_{K\pi} < 1.2 \text{ GeV}$

- Signal region
 - $5.27 < M_{bc} < 5.29 \text{ GeV}$
 - $K^* : |M_{K\pi} - m_{K^*}| < 80 \text{ MeV}$

Background

- Continuum ($e^+e^- \rightarrow qq$)
 - using the some variables and likelihood ratio
- Semileptonic B decay
 - Fisher discriminant (with 16 Fox-Wolfram moment), M_{miss} , $\cos\theta_B$, lepton separation are combined to form likelihood ratio R
- Combinatorial
 - q^2 , B-flavor tagging information

Background

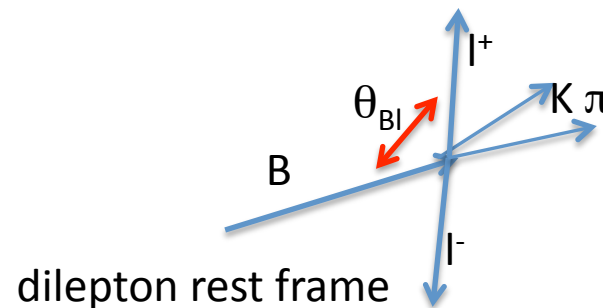
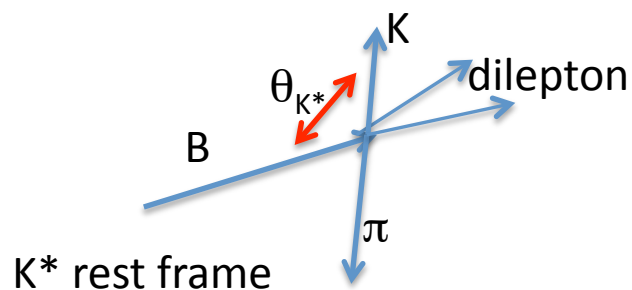
- $B \rightarrow J/\psi X, \psi' X$ have a peak in signal region.
 - rejecting some q^2 region
 - $8.68 < q^2 < 10.09, 12.86 < q^2 < 14.18$ GeV ($\mu\mu$)
 - $8.11 < q^2 < 10.03, 12.15 < q^2 < 14.11$ GeV (ee)
 - consider $\mu\pi$ misidentification
 - $-0.10 < M_{\pi\mu} - m_{J/\psi(\psi')} < 0.08$ GeV
- Rejecting $B \rightarrow D X$
 - $|M_{K\mu(K\pi\mu)} - m_D| < 0.02$ GeV μ is assigned m_π
- Removing γ conversion and $\pi^0 \rightarrow \gamma ee$
 - $M_{ee} < 0.14$ GeV
- Multiple B candidate
 - select smallest $|\Delta E|$

- To determine the signal yields, an extended unbinned maximum likelihood fit to M_{bc} (and $M_{K\pi}$) is performed.
- likelihood function
 - signal
 - combinatorial
 - $B \rightarrow J/\psi(\psi') X, K^{(*)} \pi \pi$

- F_L and A_{FB} are extracted from fits to $\cos\theta_{K^*}$ and $\cos\theta_{B\ell}$.
- The signal PDFs for fit to $\cos\theta_{K^*}$ and $\cos\theta_{B\ell}$
 - $\cos\theta_{K^*}$: $[\frac{3}{2}F_L \cos^2\theta_{K^*} + \frac{3}{4}(1 - F_L)(1 - \cos^2\theta_{K^*})]\epsilon(\cos\theta_{K^*})$
 - $\cos\theta_{B\ell}$: $[\frac{3}{4}F_L(1 - \cos^2\theta_{B\ell}) + \frac{3}{8}(1 - F_L)(1 + \cos^2\theta_{B\ell}) + A_{FB} \cos\theta_{B\ell}]\epsilon(\cos\theta_{B\ell})$

dilepton polarization function
correspond to the production K^* 's with longitudinal and transverse polarization

forward-backward asymmetry



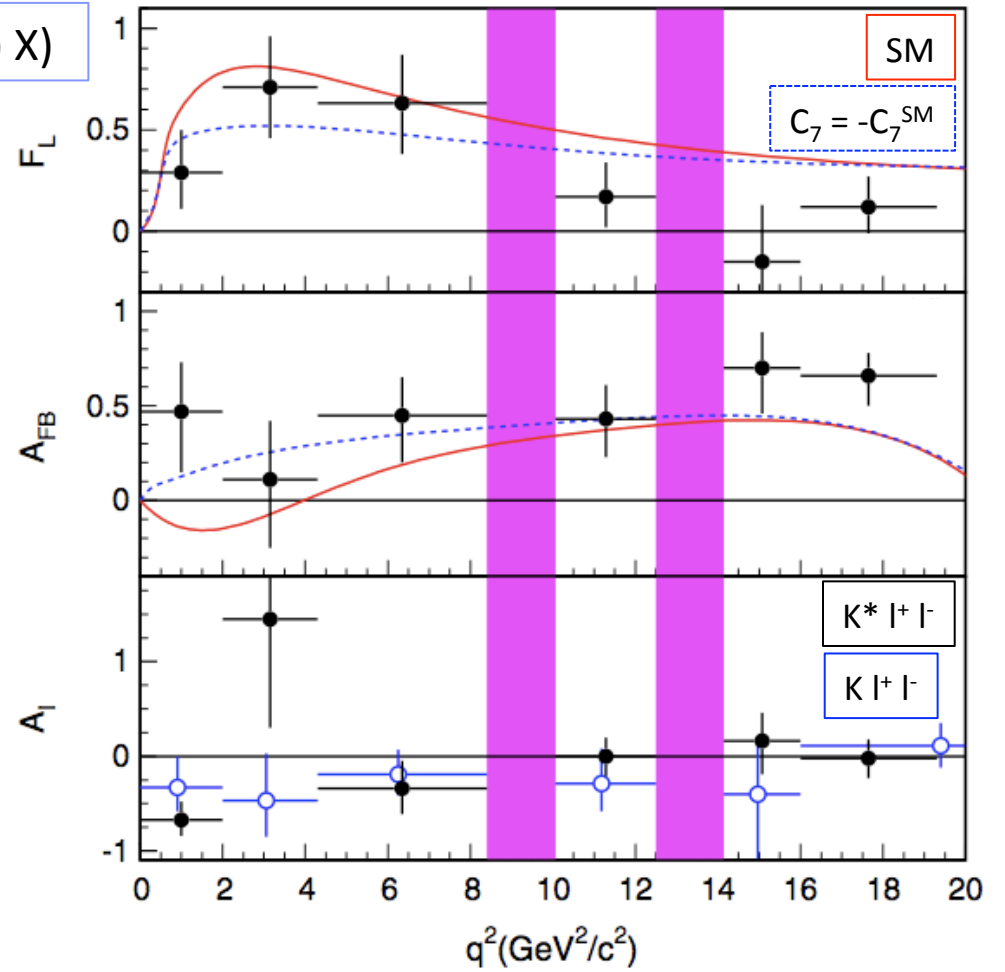
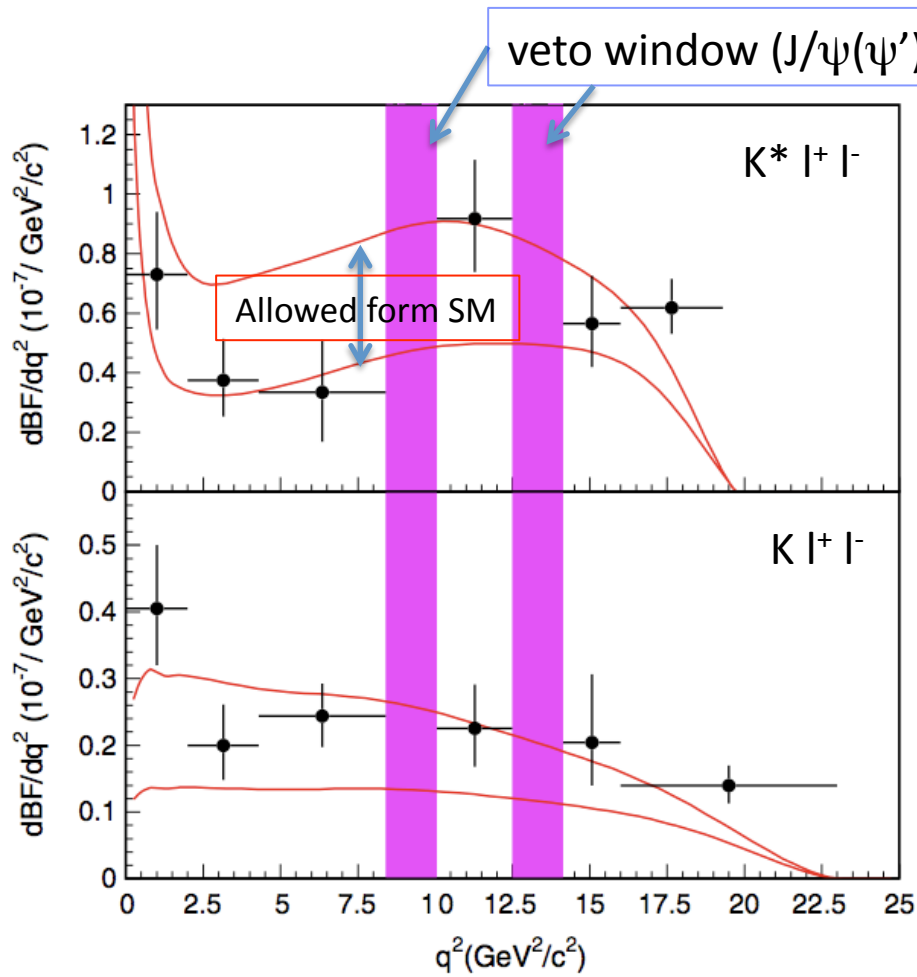
q^2 (GeV ² /c ²)	N_s	$\mathcal{B}(10^{-7})$	F_L	A_{FB}	A_I
$B \rightarrow K^* \ell^+ \ell^-$					
0.00–2.00	$27.4^{+7.4}_{-6.6}$	$1.46^{+0.40}_{-0.35} \pm 0.11$	$0.29^{+0.21}_{-0.18} \pm 0.02$	$0.47^{+0.26}_{-0.32} \pm 0.03$	$-0.67^{+0.18}_{-0.16} \pm 0.05$
2.00–4.30	$16.8^{+6.1}_{-5.3}$	$0.86^{+0.31}_{-0.27} \pm 0.07$	$0.71^{+0.24}_{-0.24} \pm 0.05$	$0.11^{+0.31}_{-0.36} \pm 0.07$	$1.45^{+1.04}_{-1.15} \pm 0.10$
4.30–8.68	$27.9^{+9.5}_{-8.5}$	$1.37^{+0.47}_{-0.42} \pm 0.39$	$0.64^{+0.23}_{-0.24} \pm 0.07$	$0.45^{+0.15}_{-0.21} \pm 0.15$	$-0.34^{+0.29}_{-0.27} \pm 0.14$
10.09–12.86	$54.0^{+10.5}_{-9.6}$	$2.24^{+0.44}_{-0.40} \pm 0.19$	$0.17^{+0.17}_{-0.15} \pm 0.03$	$0.43^{+0.18}_{-0.20} \pm 0.03$	$0.00^{+0.20}_{-0.21} \pm 0.09$
14.18–16.00	$36.2^{+9.9}_{-8.8}$	$1.05^{+0.29}_{-0.26} \pm 0.08$	$-0.15^{+0.27}_{-0.23} \pm 0.07$	$0.70^{+0.16}_{-0.22} \pm 0.10$	$0.16^{+0.30}_{-0.35} \pm 0.09$
>16.00	$84.4^{+11.0}_{-9.9}$	$2.04^{+0.27}_{-0.24} \pm 0.16$	$0.12^{+0.15}_{-0.13} \pm 0.02$	$0.66^{+0.11}_{-0.16} \pm 0.04$	$-0.02^{+0.20}_{-0.21} \pm 0.09$
1.00–6.00	$29.42^{+8.9}_{-8.0}$	$1.49^{+0.45}_{-0.40} \pm 0.12$	$0.67^{+0.23}_{-0.23} \pm 0.05$	$0.26^{+0.27}_{-0.30} \pm 0.07$	$0.33^{+0.37}_{-0.43} \pm 0.08$
$B \rightarrow K \ell^+ \ell^-$					
0.00–2.00	$27.0^{+6.0}_{-5.4}$	$0.81^{+0.18}_{-0.16} \pm 0.05$...	$0.06^{+0.32}_{-0.35} \pm 0.02$	$-0.33^{+0.33}_{-0.25} \pm 0.08$
2.00–4.30	$17.6^{+5.5}_{-4.8}$	$0.46^{+0.14}_{-0.12} \pm 0.03$...	$-0.43^{+0.38}_{-0.40} \pm 0.09$	$-0.47^{+0.50}_{-0.38} \pm 0.07$
4.30–8.68	$39.1^{+7.5}_{-6.9}$	$1.00^{+0.19}_{-0.18} \pm 0.06$...	$-0.20^{+0.12}_{-0.14} \pm 0.03$	$-0.19^{+0.25}_{-0.21} \pm 0.08$
10.09–12.86	$22.0^{+6.2}_{-5.5}$	$0.55^{+0.16}_{-0.14} \pm 0.03$...	$-0.21^{+0.17}_{-0.15} \pm 0.06$	$-0.29^{+0.37}_{-0.29} \pm 0.08$
14.18–16.00	$15.6^{+4.9}_{-4.3}$	$0.38^{+0.19}_{-0.12} \pm 0.02$...	$0.04^{+0.32}_{-0.26} \pm 0.05$	$-0.40^{+0.61}_{-0.69} \pm 0.07$
>16.00	$40.3^{+8.2}_{-7.5}$	$0.98^{+0.20}_{-0.18} \pm 0.06$...	$0.02^{+0.11}_{-0.08} \pm 0.02$	$0.11^{+0.24}_{-0.21} \pm 0.08$
1.00–6.00	$52.0^{+8.7}_{-8.0}$	$1.36^{+0.23}_{-0.21} \pm 0.08$...	$-0.04^{+0.13}_{-0.16} \pm 0.05$	$-0.41^{+0.25}_{-0.20} \pm 0.07$

- The SM lepton flavor ratio of the full q^2 is

- $R_{K^*}^{\text{SM}} = 0.75$ ($B \rightarrow K^* \ell \ell$)

- $R_K^{\text{SM}} = 1$ ($B \rightarrow K \ell \ell$)

$$R_{K^{(*)}} \equiv \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)}$$



- Fit result

C_7 : Wilson coefficients
 which are evaluated perturbatively
 at the electroweak scale.

- Total branching fractions

$$\mathcal{B}(B \rightarrow K^* \ell^+ \ell^-) = (10.7_{-1.0}^{+1.1} \pm 0.9) \times 10^{-7},$$

$$\mathcal{B}(B \rightarrow K \ell^+ \ell^-) = (4.8_{-0.4}^{+0.5} \pm 0.3) \times 10^{-7},$$

- CP asymmetries

$$A_{CP}^{K^{(*)}} \equiv \frac{\mathcal{B}(\bar{B} \rightarrow \bar{K}^{(*)} \ell^+ \ell^-) - \mathcal{B}(B \rightarrow K^{(*)} \ell^+ \ell^-)}{\mathcal{B}(\bar{B} \rightarrow \bar{K}^{(*)} \ell^+ \ell^-) + \mathcal{B}(B \rightarrow K^{(*)} \ell^+ \ell^-)} \equiv (N_b - N_{\bar{b}})/(N_b + N_{\bar{b}})$$

– $N_{b(\bar{b})}$: \bar{B} (B) yeild

$$A_{CP}(K^* \ell^+ \ell^-) = -0.10 \pm 0.10 \pm 0.01$$

$$A_{CP}(K^+ \ell^+ \ell^-) = 0.04 \pm 0.10 \pm 0.02.$$

- Lepton flavor ratio $R_{K^{(*)}} \equiv \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)}$

– sensitive to Higgs emission

$$R_{K^*} = 0.83 \pm 0.17 \pm 0.08$$

$$R_K = 1.03 \pm 0.19 \pm 0.06$$

$$R_{K^*}^{\text{SM}} = 0.75$$

$$R_K^{\text{SM}} = 1$$

- Isospin asymmetry

$$A_I \equiv \frac{(\tau_{B^+}/\tau_{B^0})\mathcal{B}(K^{(*)0}\ell^+\ell^-) - \mathcal{B}(K^{(*)\pm}\ell^+\ell^-)}{(\tau_{B^+}/\tau_{B^0})\mathcal{B}(K^{(*)0}\ell^+\ell^-) + \mathcal{B}(K^{(*)\pm}\ell^+\ell^-)}$$

– $\tau_{B^+}/\tau_{B^0} = 1.071$: lifetime ratio

$$A_I(B \rightarrow K^*\ell^+\ell^-) = -0.29_{-0.16}^{+0.16} \pm 0.09 \quad \sigma = 1.37$$

$$A_I(B \rightarrow K\ell^+\ell^-) = -0.31_{-0.14}^{+0.17} \pm 0.08 \quad \sigma = 1.75$$

$$A_I(B \rightarrow K^{(*)}\ell^+\ell^-) = -0.30_{-0.11}^{+0.12} \pm 0.08 \quad \sigma = 2.22$$

– $\sigma \equiv \sqrt{-2 \ln(\mathcal{L}_0/\mathcal{L}_{\max})}$: significance from a null asymmetry

- \mathcal{L}_0 : likelihood with $A_I = 0$
- \mathcal{L}_{\max} : maximum likelihood

- No significant A_I is found at $q^2 < 8.68$ GeV

Summary

- Consistent with the SM prediction
 - Differential branching fraction
 - Lepton flavor ratio
 - K^* polarization
- No significant CP asymmetry is found.
- The isospin asymmetry does not deviate significantly from the null value.
- The $A_{FB}(q^2)$ spectrum for $B \rightarrow K^* \ell \ell$ decays tends to be shifted toward the positive side from the SM expectation.
- The cumulative difference between the SM prediction and measured points is found to be 2.7σ .

Back up

- Previous result

- @Belle 2003/12 152*10⁶BB

$$\mathcal{B}(B \rightarrow K^* \ell^+ \ell^-) = (11.5_{-2.4}^{+2.6} \pm 0.8 \pm 0.2) \times 10^{-7},$$

$$\mathcal{B}(B \rightarrow K \ell^+ \ell^-) = (4.8_{-0.9}^{+1.0} \pm 0.3 \pm 0.1) \times 10^{-7},$$

- @BABAR 2006 229*10⁶BB

$$\mathcal{B}(B \rightarrow K^* \ell^+ \ell^-) = (0.78_{-0.17}^{+0.19} \pm 0.11) \times 10^{-6}$$

$$\mathcal{B}(B \rightarrow K \ell^+ \ell^-) = (0.34 \pm 0.07 \pm 0.02) \times 10^{-6}$$

$$F_L(B \rightarrow K^* \ell^+ \ell^-)_{(a^2 > 0.1 \text{ GeV}^2/c^4)} = 0.63_{-0.19}^{+0.18} \pm 0.05$$

$$A_{\text{FB}}(B^+ \rightarrow K^+ \ell^+ \ell^-)_{(q^2 > 0.1 \text{ GeV}^2/c^4)} = 0.15_{-0.23}^{+0.21} \pm 0.08$$

$$A_{CP}(B \rightarrow K^* \ell^+ \ell^-) = +0.03 \pm 0.23 \pm 0.03$$

$$A_{CP}(B^+ \rightarrow K^+ \ell^+ \ell^-) = -0.07 \pm 0.22 \pm 0.02$$

$$R_{K^*} = 0.91 \pm 0.45 \pm 0.06$$

$$R_K = 1.06 \pm 0.48 \pm 0.08$$

$$A_I^{K^*} = -0.64_{-0.14}^{+0.15} \pm 0.03 \quad 3.9\sigma$$