

Precision measurements of Little Higgs with T-parity parameters @ ILC

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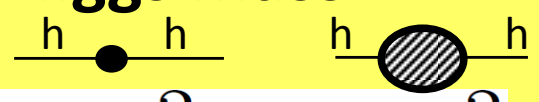
Keisuke Fujii, Shigeki Matsumoto, Hitoshi Yamamoto

- Little Higgs Model
- Analysis
- Summary

Little Hierarchy problem

There are 2 predictions on where the energy scale of new physics should emerge.

1. Fine tuning of Higgs mass

$$m_{Higgs}^2 = m_0^2 + \delta m^2$$
The diagram shows two Feynman diagrams for Higgs mass corrections. The first diagram is a tadpole diagram with a central Higgs line and a loop of Higgs particles, with 'h' labels above the loop. The second diagram is a self-energy diagram with a central Higgs line and a loop of Higgs particles, with 'h' labels above the loop and a shaded circle representing the loop.

Measured Higgs mass Bare mass Correction term

Λ : Energy scale $\delta m^2 \approx (0.27\Lambda)^2$

$\Lambda < 1 \text{ TeV}$

2. Electroweak precision measurement $\Lambda > 10 \text{ TeV}$

➡ Conflict between the 2 energy scales.

➡ Little Higgs model was proposed!

Little Higgs model

<Little Higgs mechanism>

Global Symmetry : $SU(5)$ $f \sim 1 \text{ TeV}$ $SO(5)$ $v \sim \langle h \rangle$
 subgroup : $[SU(2)_L \times U(1)_Y]^2$ \rightarrow $SU(2)_L \times U(1)_Y$ \rightarrow $U(1)_Y$

<Higgs mass contribution>

$$\begin{aligned}
 & \text{---} \overline{H} \text{---} \text{---} \text{---} + \text{---} H \text{---} \text{---} \text{---} + \text{---} \overline{H} \text{---} \text{---} \text{---} = 0\Lambda^2 \\
 & \text{---} H \text{---} \text{---} \text{---} + \text{---} H \text{---} \text{---} \text{---} = 0\Lambda^2
 \end{aligned}$$

Quadratic divergent terms cancel at 1-loop order

Solves Little hierarchy problem

Littlest Higgs with T-Parity model

Standard model

Quarks	u up	c charm	t top	γ photon
	d down	s strange	b bottom	Z Z boson
Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson
	e electron	μ muon	τ tau	g gluon
	Higgs boson			T_+

T -parity \longleftrightarrow

Little Higgs partner

Quarks	u_- up	c_- charm	t_- top	γ_H photon
	d_- down	s_- strange	b_- bottom	Z_H Z boson
Leptons	ν_{e-} electron neutrino	$\nu_{\mu-}$ muon neutrino	$\nu_{\tau-}$ tau neutrino	W_H W boson
	e_- electron	μ_- muon	τ_- tau	
	Triplet Higgs boson			T_-

A_H : dark matter candidate

$$m_{A_H} \approx \sqrt{0.2} g' f$$

$$m_{Z_H} \approx g f$$

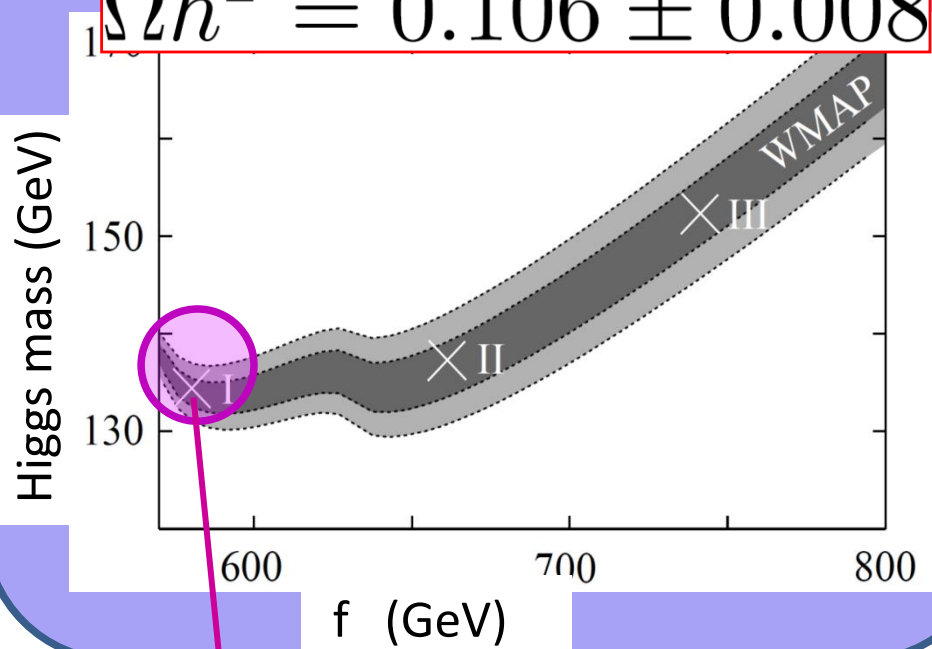
- Heavy gauge bosons acquire mass through global symmetry breaking
- $A_H Z_H W_H$ masses are proportional to f .
- f can be determined through $A_H Z_H W_H$ mass precision measurements.

Mass measurement of heavy gauge bosons extremely important !!

Selection of model parameters

<constraints from WMAP>

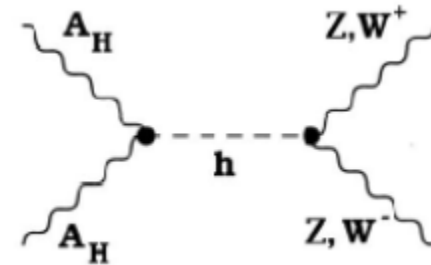
$$\Omega h^2 = 0.106 \pm 0.008$$



Model parameter

Used relic density measurement from WMAP.

Main annihilation mode



Cross section depends on m_{A_H} and m_H

f	m_H	m_{A_H}	m_{Z_H}	m_{W_H}
580(GeV)	134(GeV)	81.9(GeV)	369(GeV)	368(GeV)

$A_H Z_H W_H$ can be produced under CM energy 1TeV.

LHT heavy gauge bosons @LHC

Boson pair production cross section

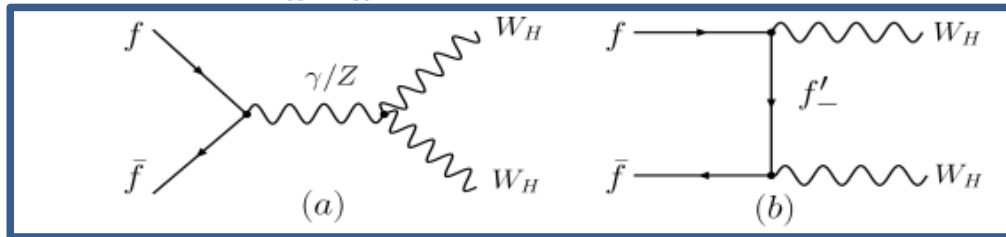
Largest cross section: $W_H W_H \sim 100 \text{fb}$

Signal: llE ($\sim 5 \text{fb}$)

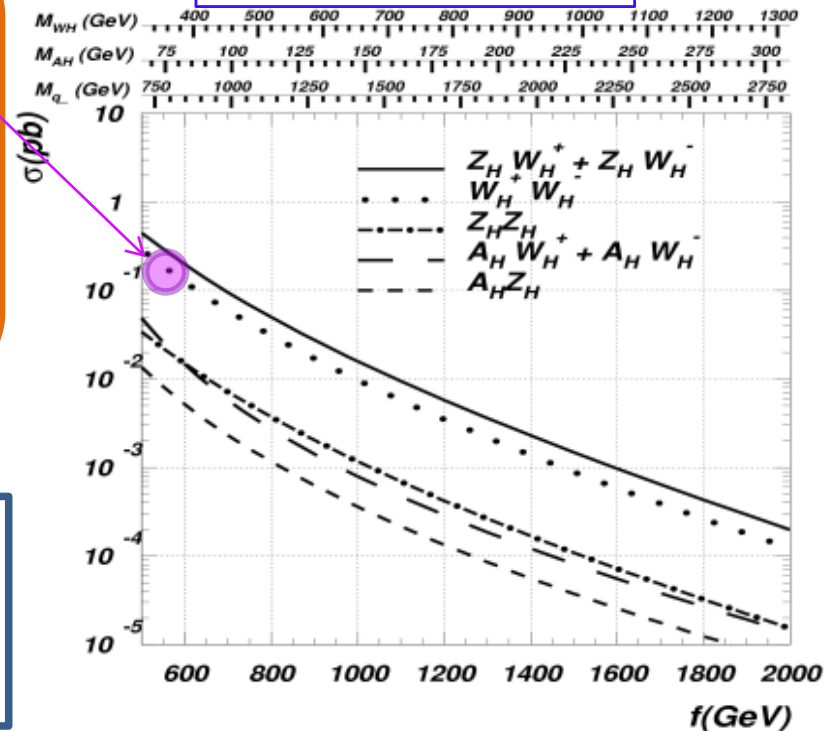
Large background: SM gauge boson
tt production

Extremely difficult to see.

Production of $W_H W_H$



VEV vs Cross section



Reference: Alexander Belyaev, Chuan-ren Chen et al Phys Rev D74,115020

simulation

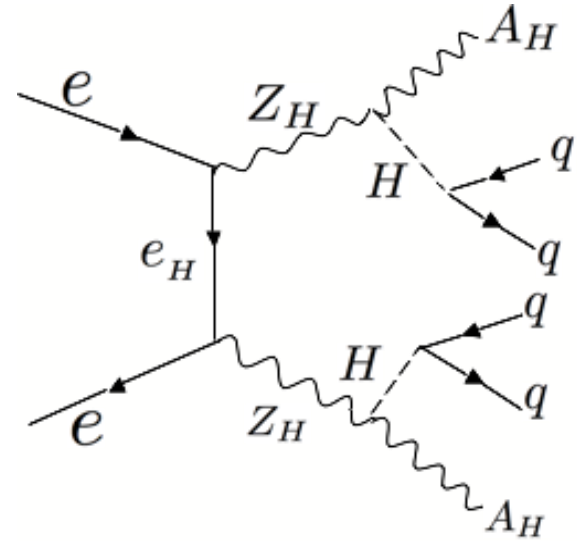
<simulation environment>

Fast simulator

Center mass energy :1TeV

Beam polarization 0%

Integrated luminosity :500fb⁻¹



<Signal event>

- $e^+e^- \rightarrow Z_H Z_H (99.52\text{fb})$
 - $Z_H \rightarrow A_H H$ (branching ratio 100%)
 - A_H is a **dark matter** candidate
 - Higgs decays mostly to $H \rightarrow bb$ (42%)
 - used **4 jet final state** as signal.

<background event (4 jet)>

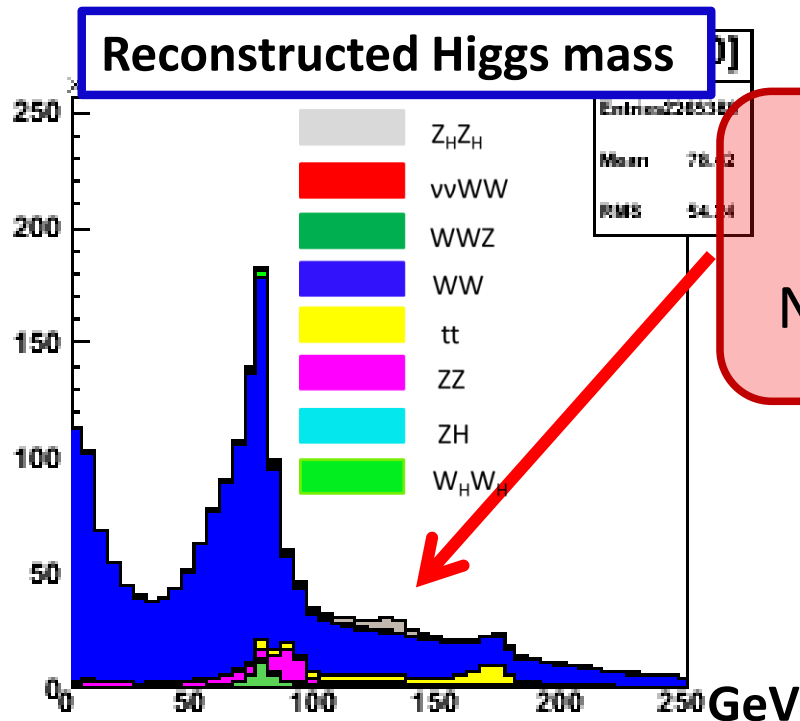
- WW (3069fb)
- tt (192.9fb)
- WWZ (63.86fb)
- $\nu\nu WW$ (14.67fb)
- ZZ (202.2fb)
- ZH (17.98fb)
- $W_H W_H$ (108.6fb)

Event reconstruction

- Reconstruct by forcing every event to be a 4 jet event.
- Select reconstructed pair that minimizes χ^2 .

$$\chi_H^2 = \left(\frac{M_{H1} - M_H}{\sigma_{M_H}} \right)^2 + \left(\frac{M_{H2} - M_H}{\sigma_{M_H}} \right)^2$$

$$M_H = 134.0(\text{GeV})$$

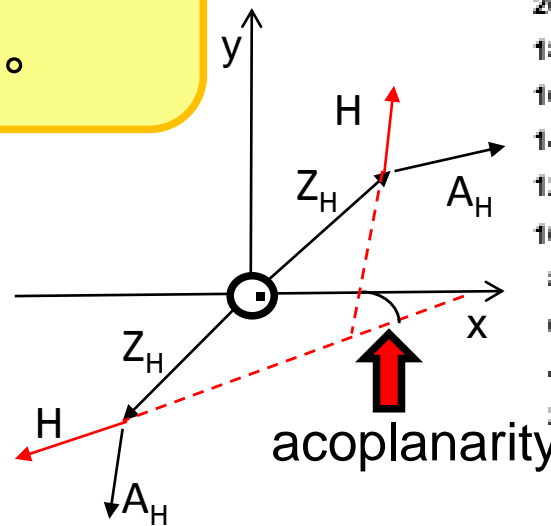
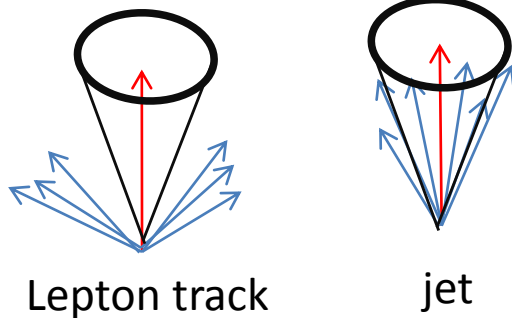


Buried signal

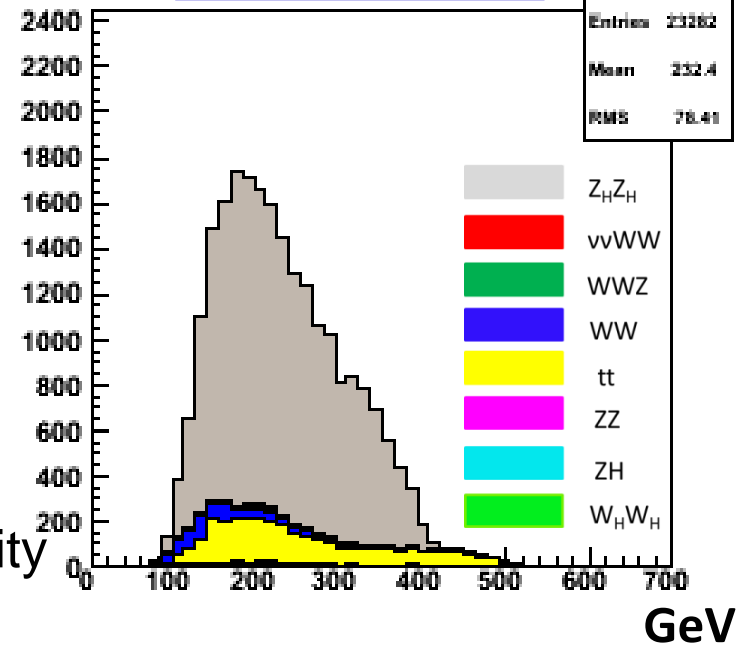
Need of background rejection

Selection criteria

- $\chi^2 < 60$
- Lepton track rejection
- # b-tag jets > 1
- Acoplanarity > 20°



Higgs energy



# event	Pre-cut	Post-cut
Signal event(Z _H Z _H)	49760	18989
Background event (SM)	2193232	3217
(background W _H W _H)	54343	87

Success in effectively rejecting background

$Z_H A_H$ mass extraction

The edge of Higgs energy possesses information of $Z_H A_H$ mass



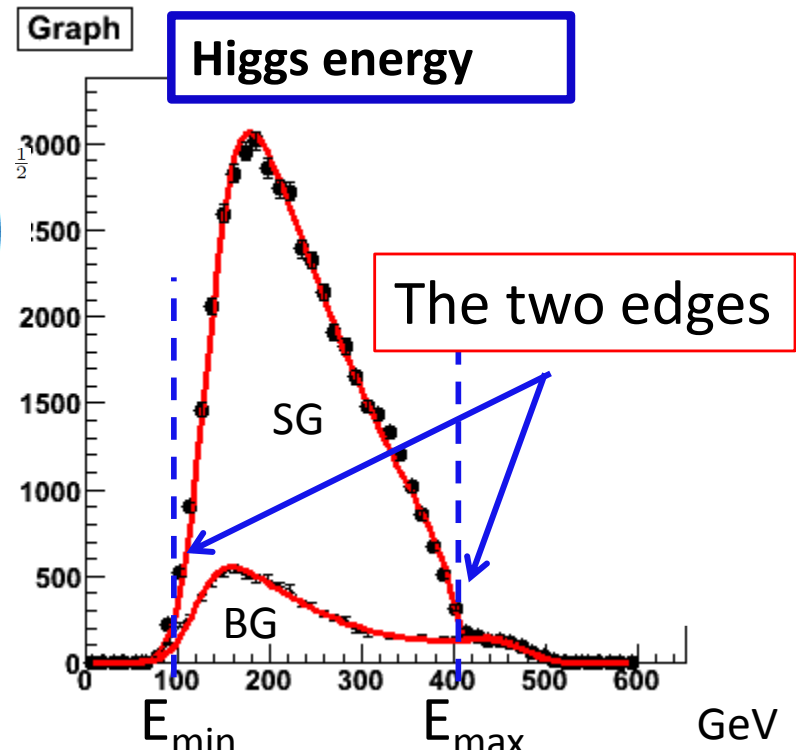
Fit energy and derive mass

<relation between edge and mass>

$$m_{Z_H} = \sqrt{s} \left(\frac{(E_+^2 - E_-^2 + m_H^2) \pm \sqrt{(E_+^2 - E_-^2 + m_H^2)^2 - 4E_+^2 m_H^2}}{8E_+^2} \right)$$

$$m_{A_H} = \left(m_H^2 + \left(1 - \frac{4E_+}{\sqrt{s}} \right) m_{Z_H}^2 \right)^{\frac{1}{2}}$$

$$\left(\begin{array}{l} E_- \equiv \frac{E_{max} - E_{min}}{2} \\ E_+ \equiv \frac{E_{max} + E_{min}}{2} \end{array} \right)$$



Contour plot of Z_H & A_H

< Z_H A_H mass solution>

2 mass solutions appear
if we select the true solution ...

A_H : 82.7 ± 3.5 GeV (True value 81.9 GeV)

Z_H : 366.1 ± 4.7 GeV (True value 369.0 GeV)

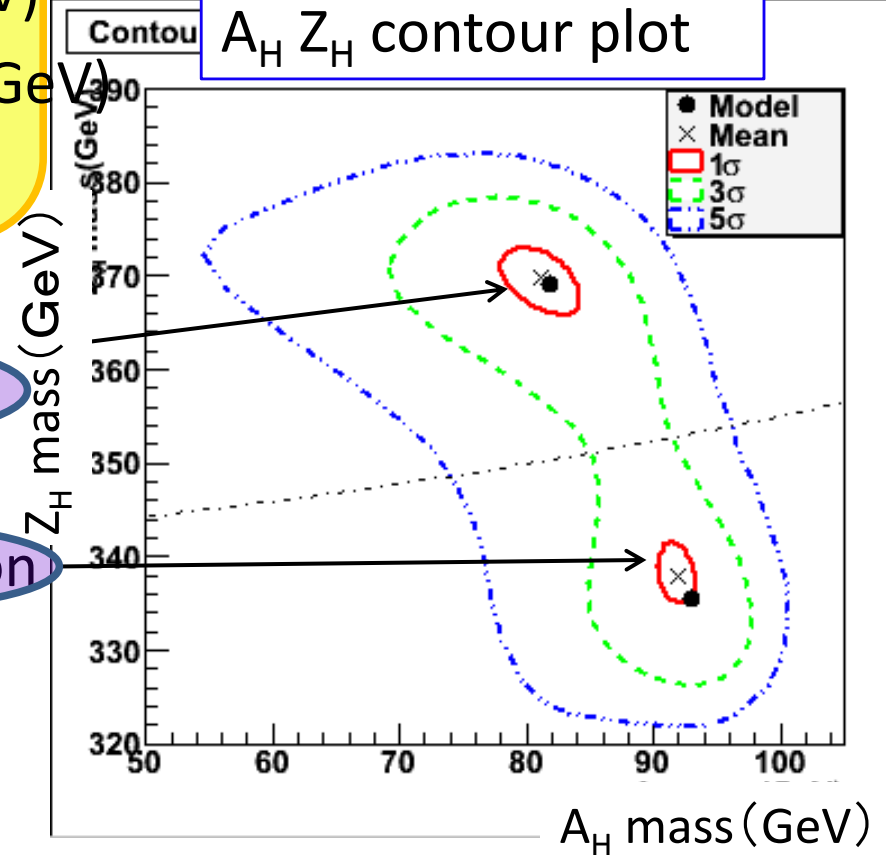
Mass resolution A_H 4.2% Z_H 1.3%



True solution

False solution

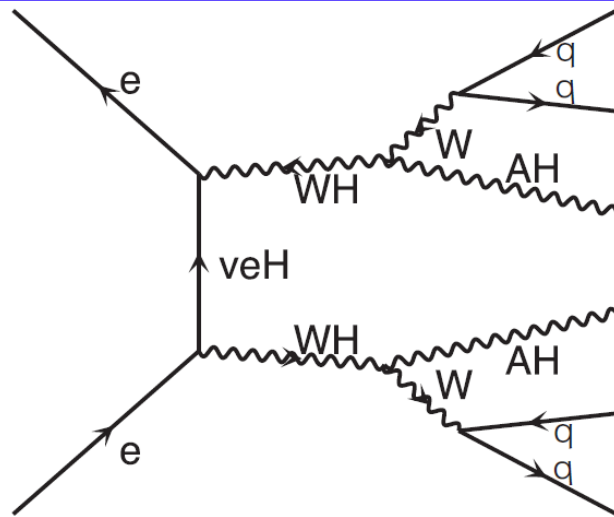
We can select the
true solution
By using **other modes**



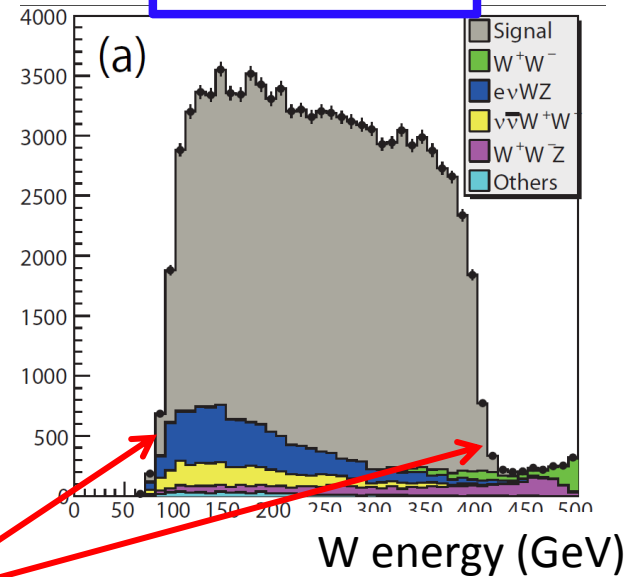
$e^+e^- \rightarrow W_H W_H$ mode

Used $e^+e^- \rightarrow W_H W_H$ mode to select true mass solution

1TeV : $e^+e^- \rightarrow W_H W_H$



W^\pm energy



Can determine $A_H W_H$ mass from W^\pm energy distribution

True solution

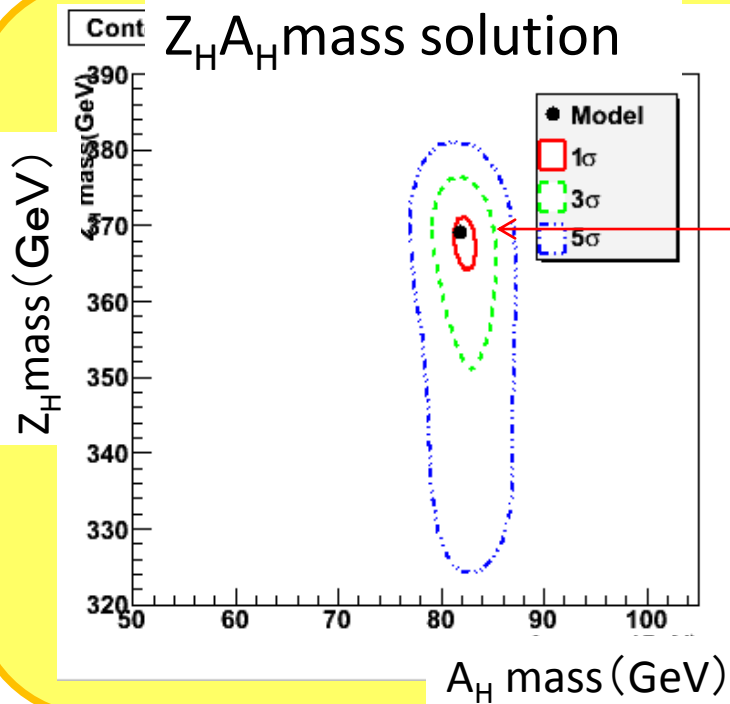
This analysis also produces 2 mass solutions.

$$m_{AH} = 81.6 \text{ GeV} , 81.0 \text{ GeV} \quad 1.3\%$$

$$m_{WH} = 368.3 \text{ GeV} , 218.0 \text{ GeV} \quad 0.2\% \text{ (phys. Rev D79.075013)}$$

Selected true solution by analyzing both $W_H W_H$ & $Z_H Z_H$

Result of simultaneous fit



Result of $Z_H Z_H$ & $W_H W_H$ simultaneous fit

$$A_H \text{ mass } 81.7 \pm 1.1 \text{ GeV}$$
$$Z_H \text{ mass } 367.3 \pm 4.1 \text{ GeV}$$

able to select 1 solution

<mass resolution>

$$A_H : 1.3\%$$

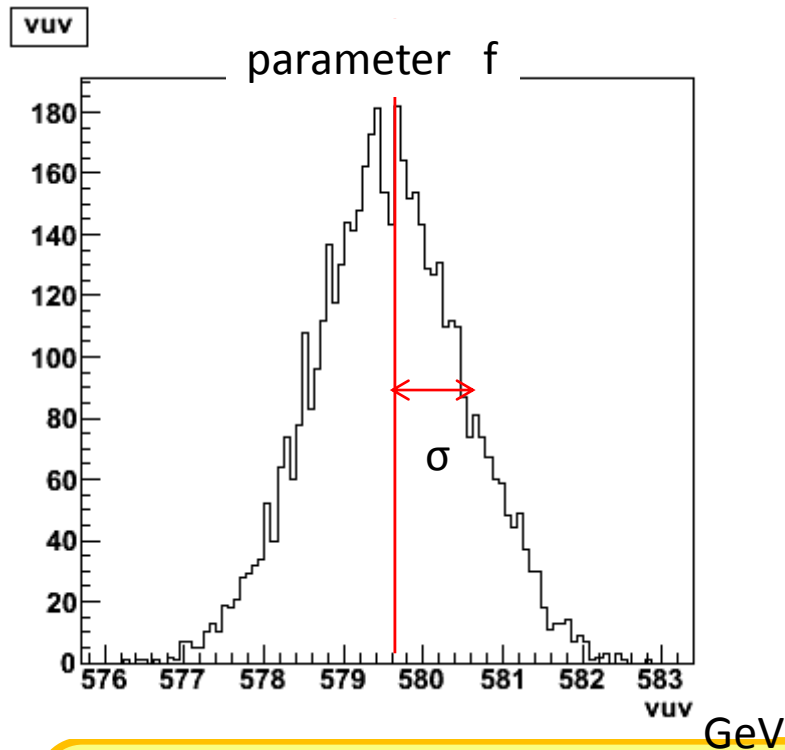
$$Z_H : 1.1\%$$

$$W_H : 0.20\%$$

**All heavy gauge boson mass resolutions
improved through simultaneous fit**

Model parameter f

Evaluated the measurement accuracy of f



Because A_H , Z_H masses depends on f , we can determine f through simultaneous fitting.

$$m_{A_H} \approx \sqrt{0.2} g' f$$

$$m_{Z_H} \approx g f$$

Measurement accuracy : **f resolution : 0.16%**

ILC can measure f with high resolution

Summary

The Little Higgs with T-Parity model is a new physics model that solves the **little hierarchy problem** and the **dark matter problem**.

$\langle \sqrt{s}=1\text{TeV}: e^+e^- \rightarrow Z_H Z_H \text{ analysis} \rangle$

2 neighboring mass solutions (A_H, Z_H) were obtained.
Necessary to select true solution.

$\langle \sqrt{s}=1\text{TeV}: e^+e^- \rightarrow Z_H Z_H \text{ \& } W_H W_H \text{ simultaneous fit} \rangle$

Able to select one true mass solution.
Through simultaneous fit all mass resolution improved.
Mass resolution A_H **1.3%** Z_H **1.1%** W_H **0.20%**
Vacuum expectation value: **f 0.16%**