

# $B \rightarrow D^* \pi$ 崩壊を用いたCP対称性の破れの測定

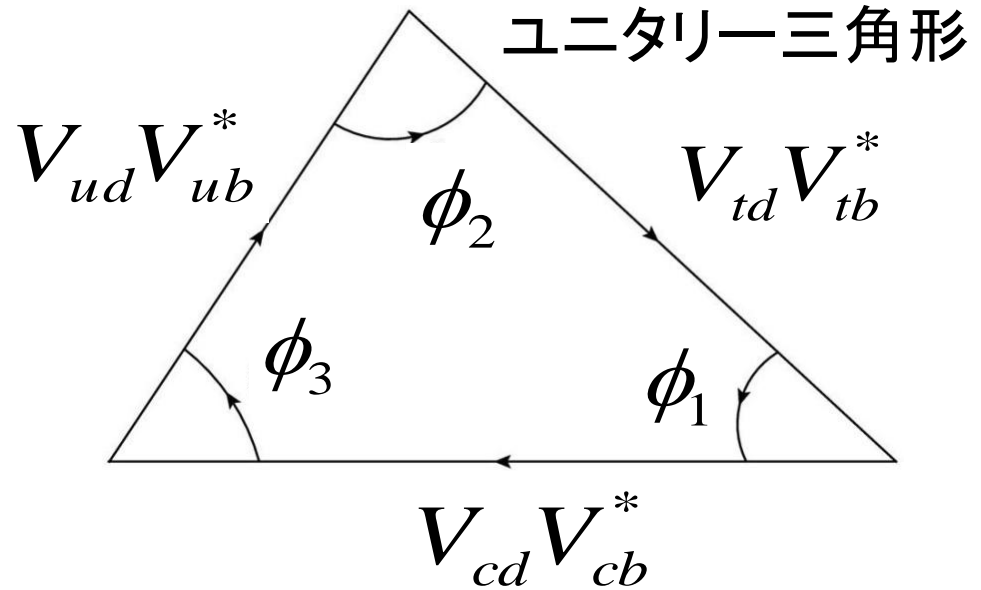
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# 内容

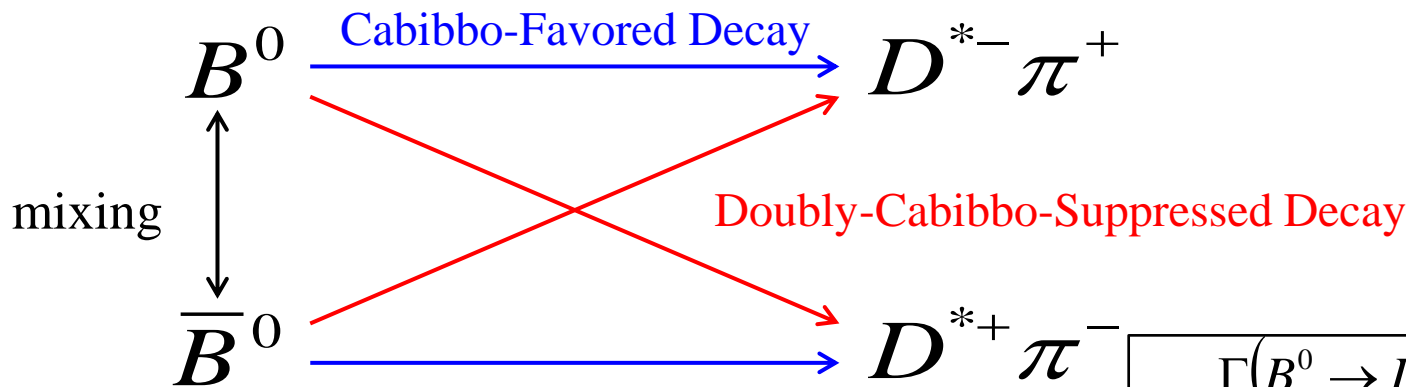
- 導入
- 再構成
  - Signal MC, Generic MC
- Generic MC を使用した Signal fraction の見積もり
- Generic MC の  $\Delta t$  fit
- まとめと計画

# 導入

- 動機:  $\phi_3$  の精密測定



- $B^0 \rightarrow D^* \pi$  崩壊

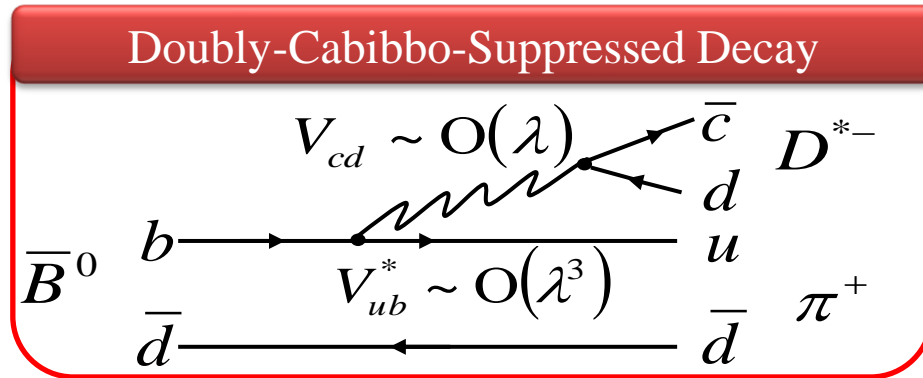
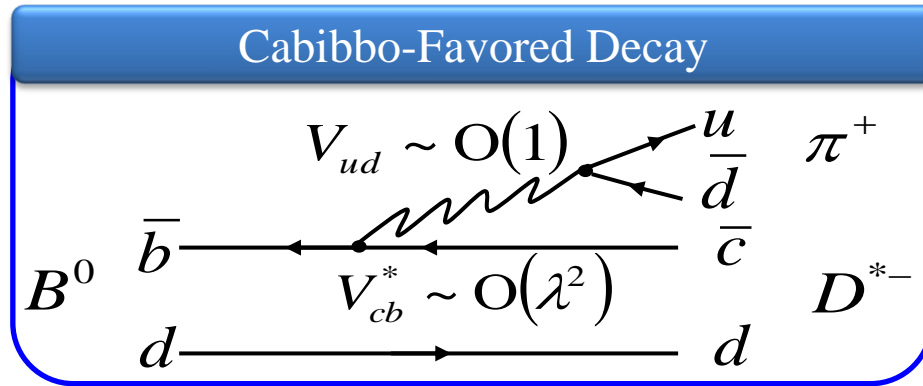
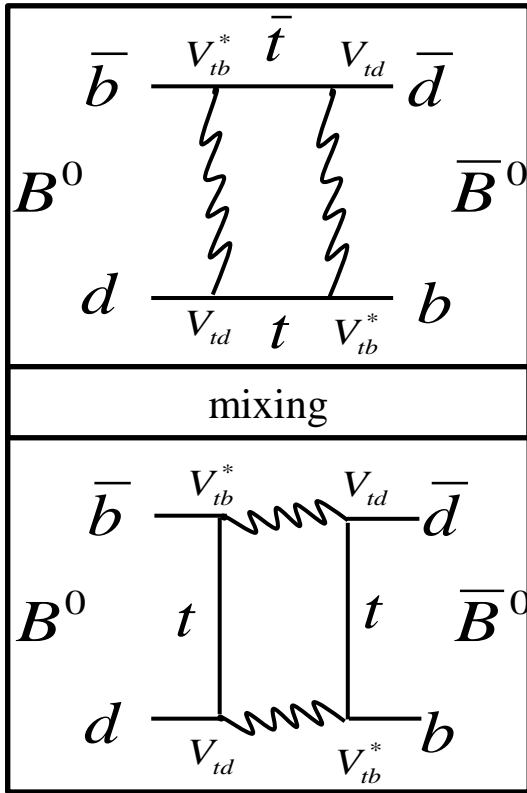


$$R = \frac{\Gamma(B^0 \rightarrow D^{*+} \pi^-)}{\Gamma(B^0 \rightarrow D^{*-} \pi^+)} \sim \frac{V_{cd} V_{ub}^*}{V_{cb} V_{ud}^*} \sim \mathcal{O}(\lambda^2)$$

$$\lambda \cong 0.23$$

二つの崩壊経路: 干渉  $\rightarrow$  CP対称性の破れ

# 導入: $B^0 \rightarrow D^* \pi$ 崩壊



## 干渉項の位相

$$\arg\left(-\frac{V_{td}^* V_{tb}}{V_{td} V_{tb}^*} \frac{V_{ub} V_{cd}^*}{V_{cb}^* V_{ud}}\right) = \arg\left(\frac{V_{cd} V_{cb}^*}{-V_{td} V_{tb}^*} \frac{V_{cd} V_{cb}^*}{-V_{td} V_{tb}^*} \frac{V_{ud} V_{ub}^*}{-V_{cd} V_{cb}^*}\right) = 2\phi_1 + \phi_3$$

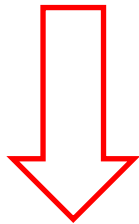
# 導入： $B^0 \rightarrow D^* \pi$ 崩壊

$B^0 \rightarrow D^* \pi$  の崩壊率

$$P(B^0 \rightarrow D^{*\mp} \pi^\pm) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{8\tau_{B^0}} \left[ 1 \pm C \cos(\Delta m \Delta t) - S^\mp \sin(\Delta m \Delta t) \right]$$

$$P(\bar{B}^0 \rightarrow D^{*\pm} \pi^\mp) = \frac{e^{-|\Delta t|/\tau_{B^0}}}{8\tau_{B^0}} \left[ 1 \pm C \cos(\Delta m \Delta t) + S^\pm \sin(\Delta m \Delta t) \right]$$

$$S^\pm = -\frac{2R}{1+R^2} \sin(2\phi_1 + \boxed{\phi_3} \pm \delta), \quad C = \frac{1-R^2}{1+R^2} \cong 1$$

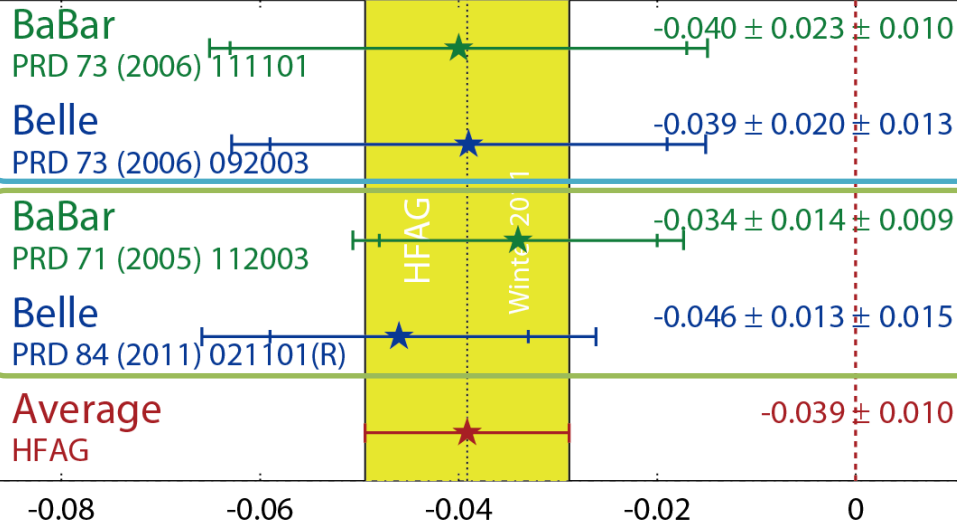


$B^0 \rightarrow D^* \pi$  の崩壊時間分布を測定する

# 導入：今までの結果

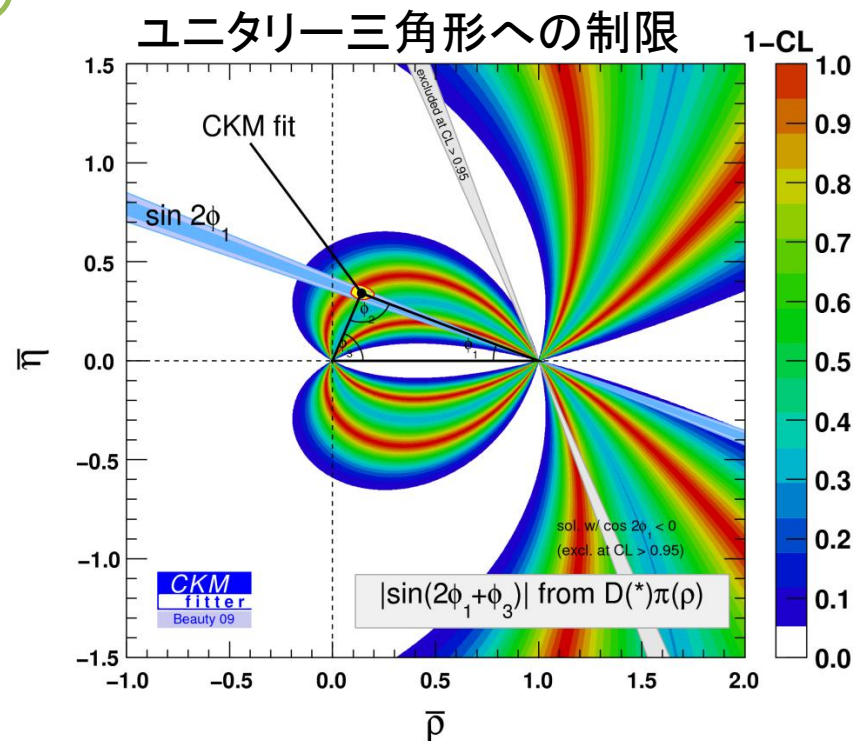
## Merged $D^*\pi a$

**HFAG**  
Winter 2011  
PRELIMINARY



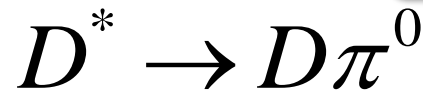
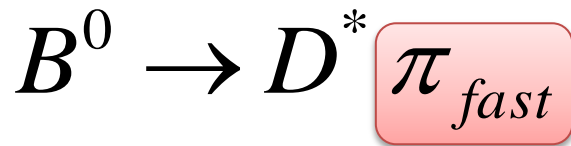
Full reconstruction

Partial reconstruction



# 導入

## partial reconstruction と full reconstruction



$B^0$  崩壊

$D^*$  崩壊

で生成される荷電 $\pi$ が特徴的

### 再構成方法

#### – Partial reconstruction

荷電 $\pi$ のみ観測

– 運動量、電荷、方向

- $D$  の下位崩壊によらないため、検出効率が良い

#### – Full reconstruction

$D$  を再構成

- 信号事象/背景事象 の比が良い

# 導入 : my analysis

- Belle 全データを使用した full reconstruction

- 使用する下位崩壊

$$D^* \rightarrow D^0 \pi$$

$$D^0 \rightarrow K\pi, K\pi\pi^0, K\pi\pi\pi, K_s\pi\pi$$

$$D^* \rightarrow D\pi^0$$

$$D \rightarrow K\pi\pi$$

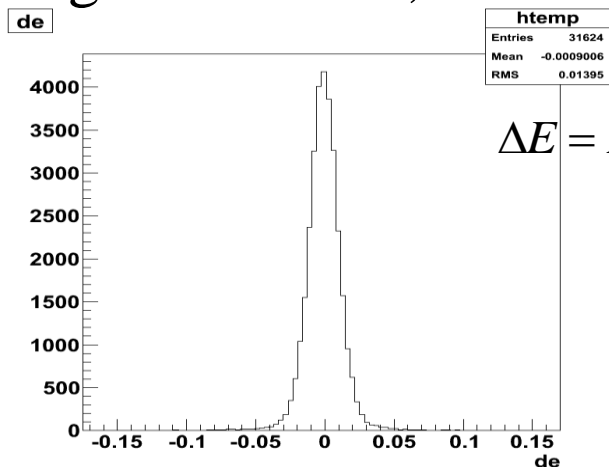
$D^* \rightarrow D^0 \pi, D^0 \rightarrow K\pi$  の進行状況  
についての talk



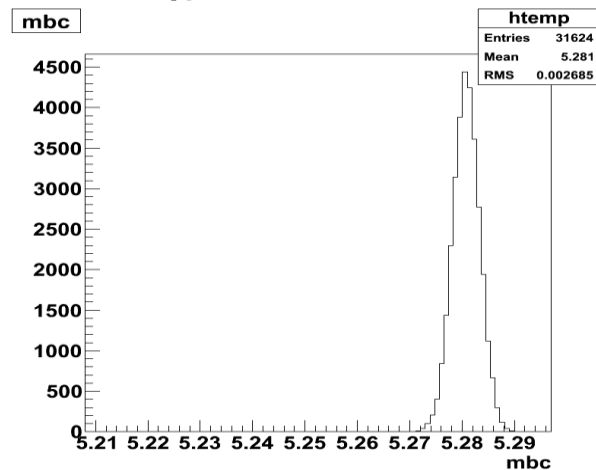


# 再構成

- Signal MC 100,000 events を生成、再構成

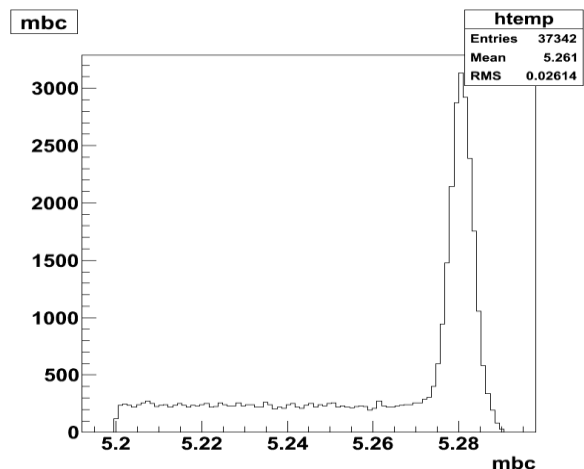
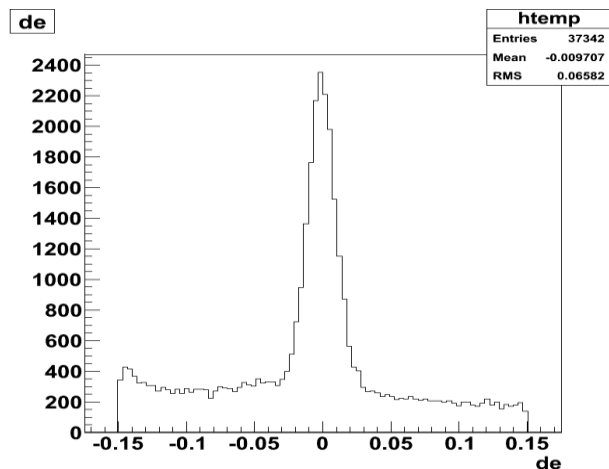


$$\Delta E = E_B - E_{Beam}$$



$$M_{bc} = \sqrt{E_{Beam}^2 - P_B^2}$$

- Generic MC の再構成



再構成数: 31,624 ~ 32%

— よく再構成できている

# $\Delta E$ PDF

- Signal fraction を計算するため、

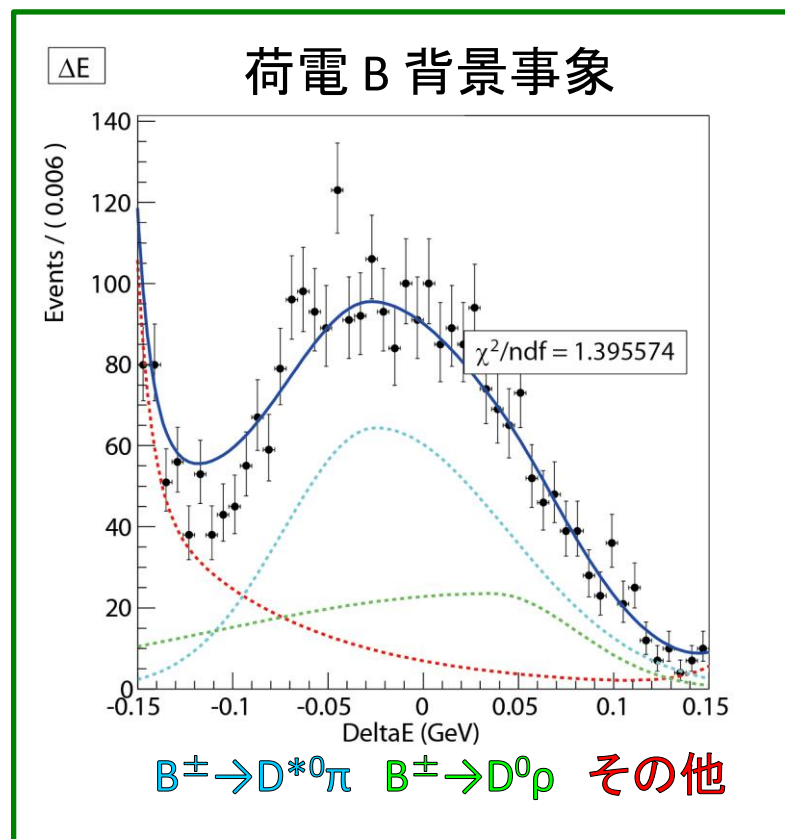
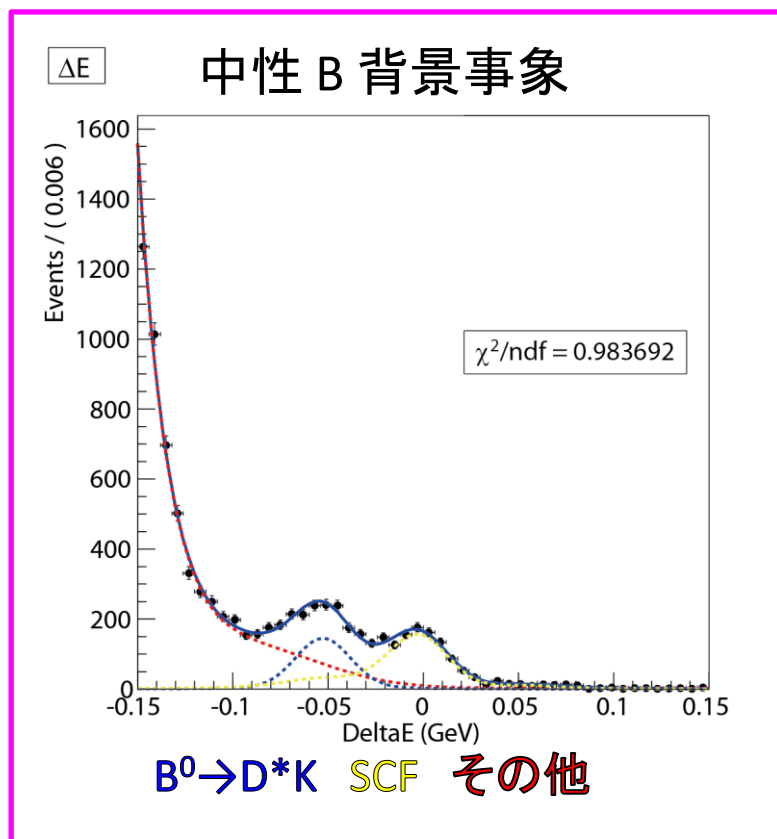
$\Delta E$  PDF を見積もった

実験データの 5 倍の統計量を使用

範囲 :  $5.27 \text{ GeV} < M_{bc} < 5.29 \text{ GeV}$

$-0.15 \text{ GeV} < \Delta E < 0.15 \text{ GeV}$

- 得られた 中性/荷電 B 背景事象の  $\Delta E$  PDF



# ΔE PDF

signal fraction を求めた

ΔE を fit し、

– flavor tag の信頼度ごと

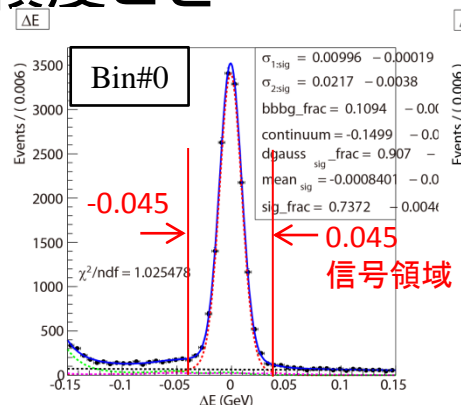
Bin#0 → Bin#6  
 信頼度高

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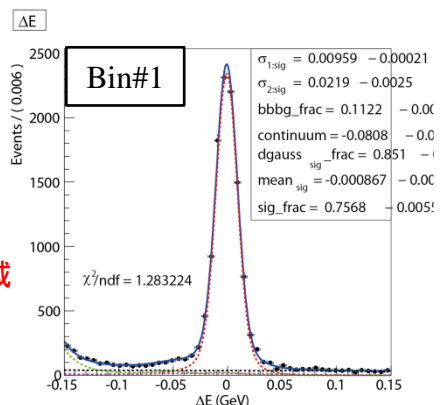
変数  
 信号事象: ダブルガウシアン  
 B以外の背景事象: 直線  
 Signal fraction

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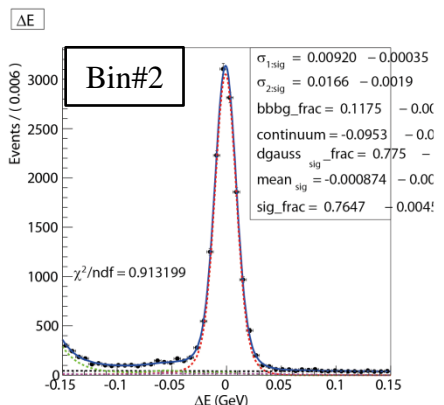
B 背景事象: 固定



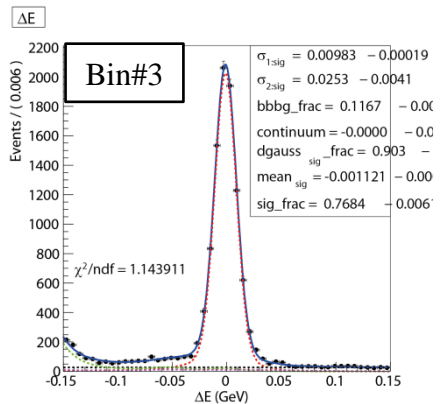
信号事象 ~ 90%  
 B<sup>0</sup> BG ~ 2%, B<sup>±</sup> BG ~ 2%  
 B 以外 ~ 6%



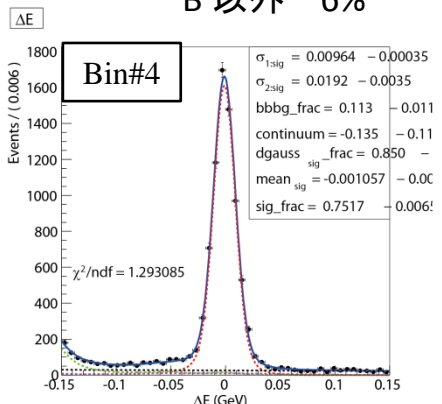
信号事象 ~ 91%  
 B<sup>0</sup> BG ~ 2%, B<sup>±</sup> BG ~ 2%  
 B 以外 ~ 5%



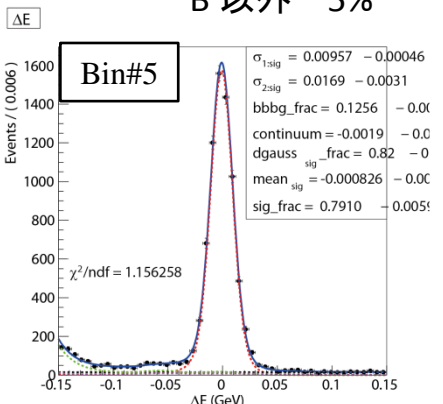
信号事象 ~ 92%  
 B<sup>0</sup> BG ~ 2%, B<sup>±</sup> BG ~ 2%  
 B 以外 ~ 4%



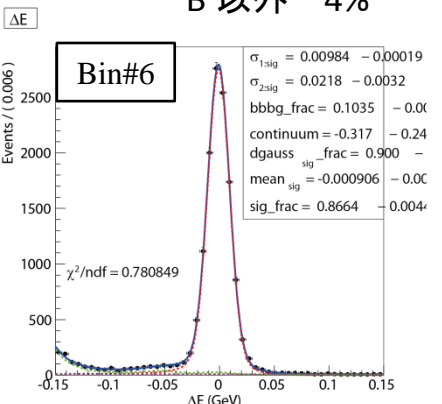
信号事象 ~ 92%  
 B<sup>0</sup> BG ~ 2%, B<sup>±</sup> BG ~ 2%  
 B 以外 ~ 4%



信号事象 ~ 91%  
 B<sup>0</sup> BG ~ 2%, B<sup>±</sup> BG ~ 2%  
 B 以外 ~ 5%



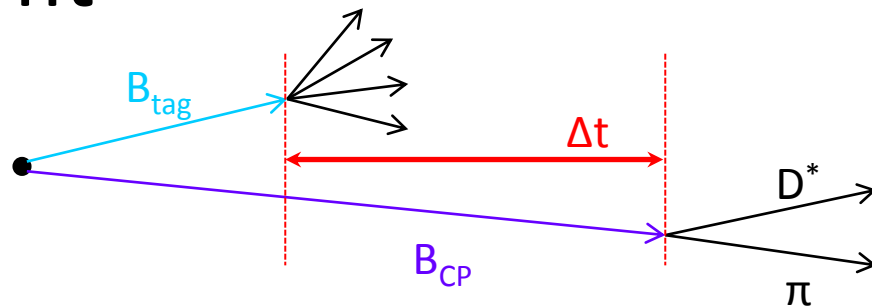
信号事象 ~ 93%  
 B<sup>0</sup> BG ~ 2%, B<sup>±</sup> BG ~ 2%  
 B 以外 ~ 3%



信号事象 ~ 96%  
 B<sup>0</sup> BG ~ 2%, B<sup>±</sup> BG ~ 1%  
 B 以外 ~ 1%

$\Delta t$  fit

- $\Delta t$ :  $B_{\text{tag}}$  と  $B_{\text{CP}}$  の崩壊時間差



- PDF

$$P(\Delta t) = (1 - f_{ol}) \left[ f_{sig} P_{sig} + (1 - f_{sig}) \left\{ f_{B^0\bar{B}^0} P_{B^0\bar{B}^0} + f_{B^+B^-} P_{B^+B^-} + (1 - f_{B^0\bar{B}^0} - f_{B^+B^-}) P_{con} \right\} \right] + f_{ol} P_{ol}$$

$P_{sig}$  :  $\phi_3$  を含む信号事象項

$P_{B^0\bar{B}^0}$  : 中性B中間子背景事象項

$P_{B^+B^-}$  : 荷電B中間子背景事象項

$P_{con}$  : B中間子以外の背景事象項

$P_{ol}$  : 検出器のresolutionの補正項

- Generic MC の  $\Delta t$  fit
  - Fitter program の挙動確認
  - B 背景事象項の決定

# 信号事象の $\Delta t$ fit

- $\tau, \Delta m$  を fit

$$P_{sig}(\Delta t, q_{tag}, q_{cp}) = \frac{1}{8\tau} e^{-|\Delta t|/\tau} \left\{ 1 - q_{tag} \Delta w_{rbin}^{official} - q_{tag} q_{cp} (1 - 2w_{rbin}^{official}) \cos(\Delta m \Delta t) \right\}$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*-} \pi^+ \text{ と } B_{tag} = B^0, f_{CP} = D^{*+} \pi^-$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*+} \pi^- \text{ と } B_{tag} = B^0, f_{CP} = D^{*-} \pi^+$$

を  $\delta = 0$  として統合  $\rightarrow$  sin 項を無視

$w, \Delta w$ : flavor tag の間違いを補正

$$w = \frac{w_{B^0} + w_{\bar{B}^0}}{2}, \Delta w = w_{B^0} - w_{\bar{B}^0}$$

Official wrong tag fraction を使用

R bin #	official wrong tag fraction	
Bin#0	w = 0.5	$\Delta w = 0.$
Bin#1	w = 0.412222	$\Delta w = 0.0569661$
Bin#2	w = 0.307838	$\Delta w = 0.0126192$
Bin#3	w = 0.212765	$\Delta w = 0.0147724$
Bin#4	w = 0.149933	$\Delta w = 0.000550289$
Bin#5	w = 0.0913264	$\Delta w = 0.00887704$
Bin#6	w = 0.0218754	$\Delta w = 0.00465683$

# 信号事象の $\Delta t$ fit

## Fit 結果

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*+} \pi^-$$

$$B_{tag} = B^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = B^0, f_{CP} = D^{*+} \pi^-$$

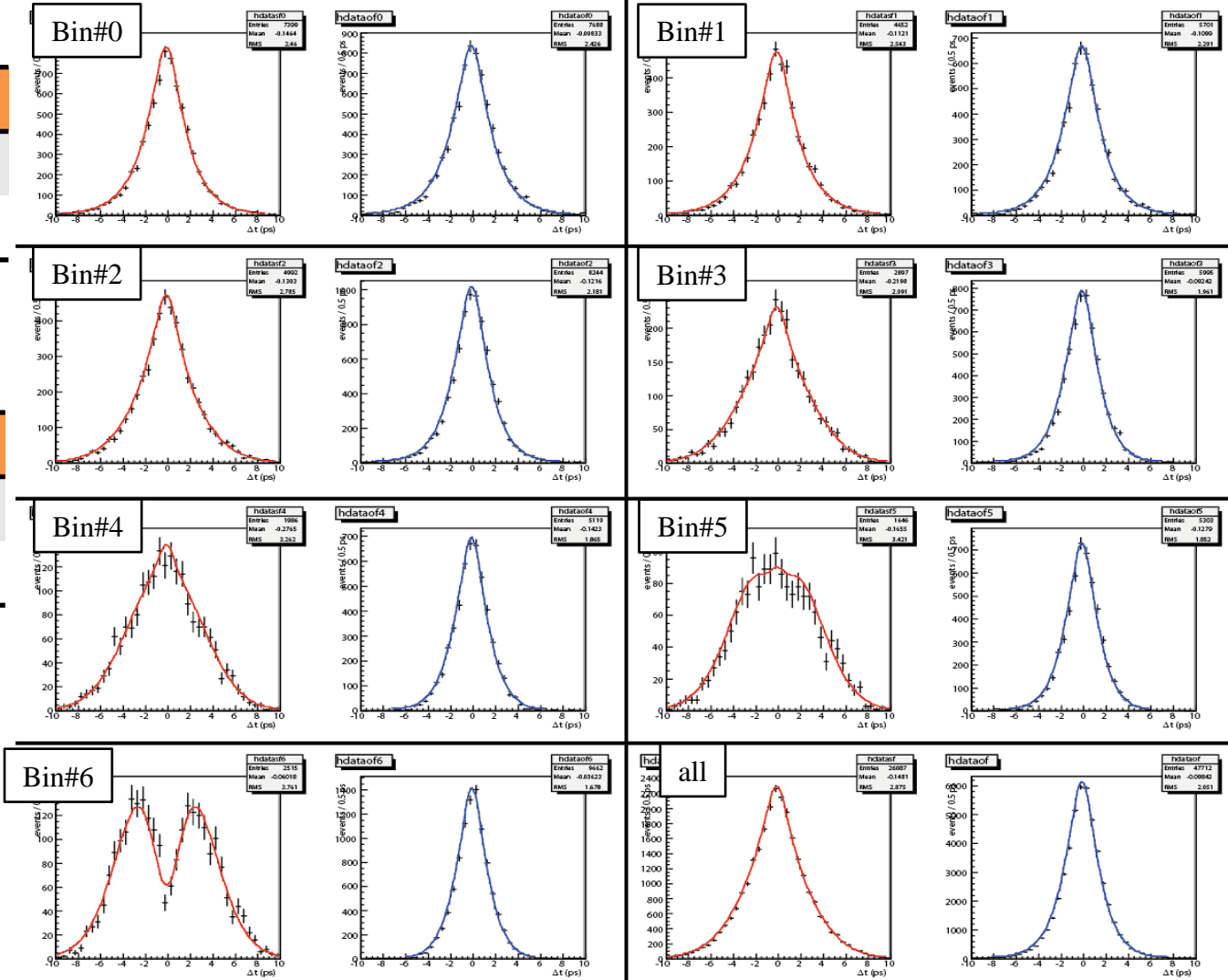
## MC 入力値

Name	Value
$\tau_{B0}$	1.534
$\Delta m$	0.507

## Fit 結果

Name	Value
$\tau_{B0}$	$1.533 \pm 0.006$ (ps)
$\Delta m$	$0.505 \pm 0.004$

Fit 結果は入力値と consistent



# 背景事象の $\Delta t$ fit

- 背景事象のPDFを得るため、各々を fit
- Fit 範囲 :  $-0.15 \text{ GeV} < \Delta E < 0.15 \text{ GeV}$ ,  $5.2 \text{ GeV} < M_{bc} < 5.3 \text{ GeV}$

## 中性B中間子背景事象 PDF

$$P_{B^0BG}(\Delta t, q_{tag}, q_{cp}) = \frac{1}{8\tau_{B^0BG}} e^{-|\Delta t|/\tau_{B^0BG}} \left\{ 1 - q_{tag} q_{cp} (1 - 2w_{rbin}) \cos(\Delta m \Delta t) \right\}$$

## 荷電B中間子背景事象 PDF

$$P_{chg}(\Delta t, q_{tag}, q_{cp}) = \frac{1}{8\tau_{chgB}} e^{-|\Delta t|/\tau_{chgB}} \left\{ 1 - q_{tag} q_{cp} (1 - 2w_{rbin}) \right\}$$

## B中間子以外からの背景事象 PDF

$$P_{con}(\Delta t) = \int P_{con}(\Delta t') \cdot R_{bkg}(\Delta t - \Delta t') \cdot d\Delta t'$$

$$P_{con}(\Delta t) = f_{\delta} \cdot \delta(\Delta t - \mu_{\delta}) + (1 - f_{\delta}) \cdot \exp\left(-\frac{|\Delta t - \mu_{\tau}|}{\tau_{con}}\right)$$

$$R_{con}(\Delta t) = (1 - f_{con}^{tail}) \cdot G(\Delta t; s_{con}^{main} \cdot \sigma_{vtx}) + f_{con}^{tail} \cdot G(\Delta t; s_{con}^{tail} \cdot \sigma_{vtx})$$

# 中性B中間子背景事象の $\Delta t$ fit

## Fit 結果

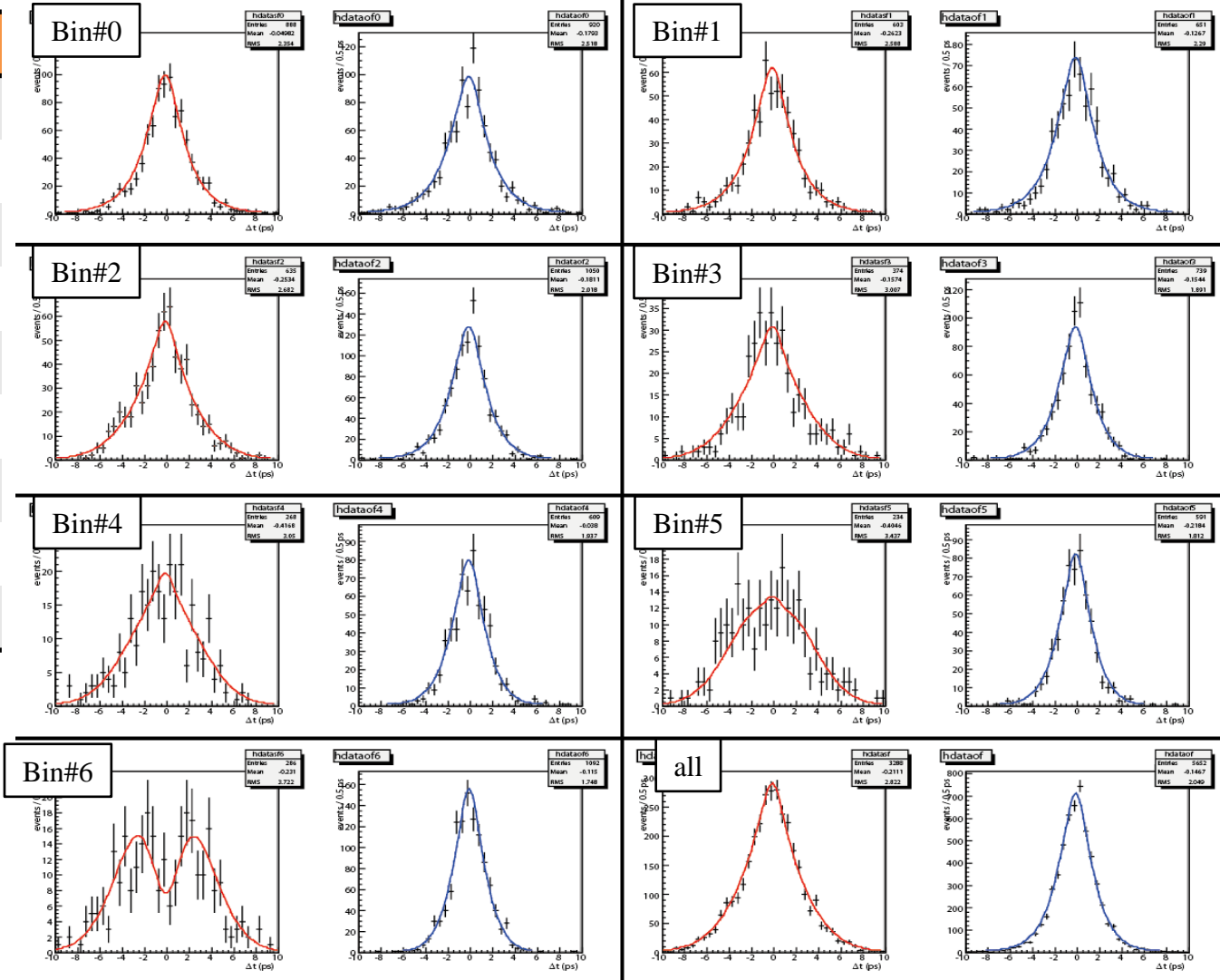
$$B_{tag} = \bar{B}^0, f_{CP} = D^{*+} \pi^-$$

$$B_{tag} = B^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = B^0, f_{CP} = D^{*+} \pi^-$$

Name	Value
$\tau_{B0BG}$	$1.525 \pm 0.019$ (ps)
$\Delta m$	$0.516 \pm 0.013$
$w_0$	0.50 (fixed)
$w_1$	$0.45 \pm 0.02$
$w_2$	$0.29 \pm 0.02$
$w_3$	$0.23 \pm 0.02$
$w_4$	$0.18 \pm 0.02$
$w_5$	$0.12 \pm 0.02$
$w_6$	$0.03 \pm 0.01$





# 荷電B中間子背景事象のΔt fit

## Fit 結果

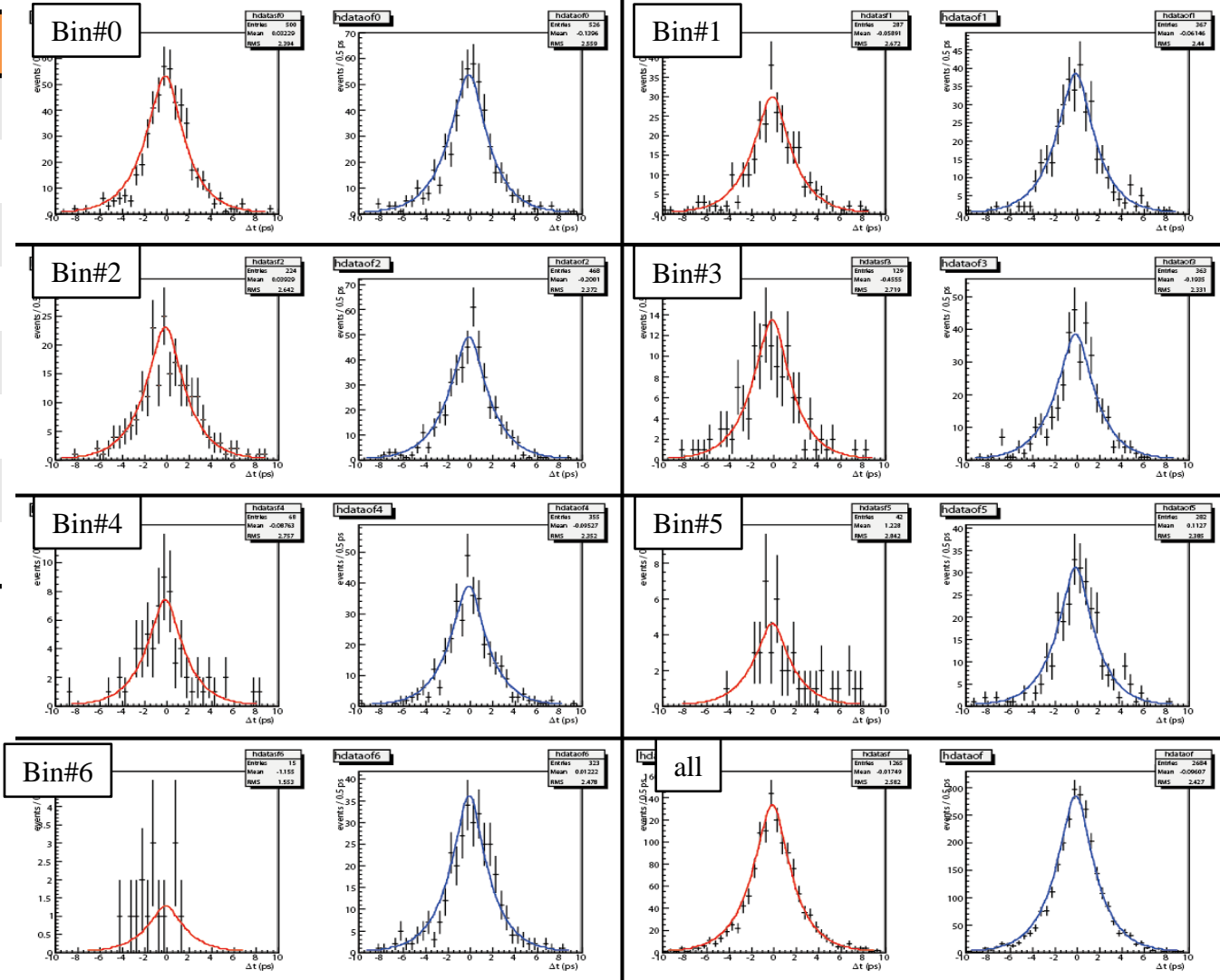
$$B_{tag} = \bar{B}^0, f_{CP} = D^{*+} \pi^-$$

$$B_{tag} = B^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = \bar{B}^0, f_{CP} = D^{*-} \pi^+$$

$$B_{tag} = B^0, f_{CP} = D^{*+} \pi^-$$

Name	Value
$\tau_{chgB}$	$1.599 \pm 0.029$ (ps)
$w_0$	0.50 (fixed)
$w_1$	$0.44 \pm 0.02$
$w_2$	$0.32 \pm 0.02$
$w_3$	$0.26 \pm 0.02$
$w_4$	$0.16 \pm 0.02$
$w_5$	$0.13 \pm 0.02$
$w_6$	$0.04 \pm 0.01$



# B以外の背景事象の $\Delta t$ fit

## Fit 結果

Single-track  
vertex  
Either CP or  
tag B

Multi-track  
vertex  
Both CP and  
tag B

$$f_d = 0.26 \pm 0.04 \quad 0.39 \pm 0.02$$

$$m_d = 0.046 \pm 0.007$$

$$m_\tau = 0.14 \pm 0.01$$

$$\tau_{\text{con}} = 0.58 \pm 0.02$$

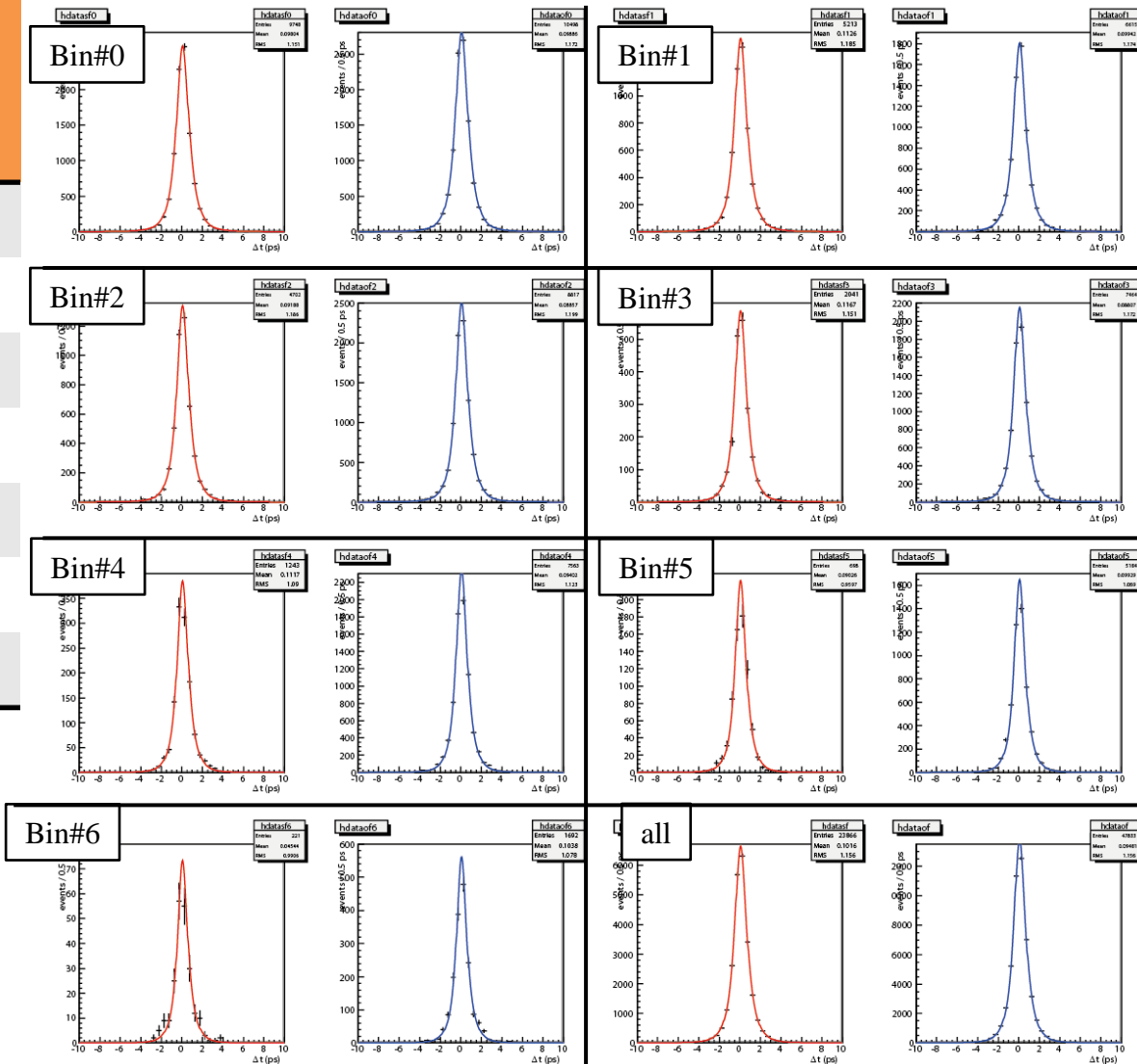
$$S_{\text{bkg}}^{\text{main}} = 1.07 \pm 0.03 \quad 1.34 \pm 0.02$$

$$S_{\text{bkg}}^{\text{tail}} = 5.40 \pm 0.42 \quad 4.87 \pm 0.26$$

$$f_{\text{bkg}}^{\text{tail}} = 0.088 \pm 0.010 \quad 0.047 \pm 0.007$$

$$\begin{aligned} B_{\text{tag}} &= \bar{B}^0, f_{CP} = D^{*+} \pi^- \\ B_{\text{tag}} &= B^0, f_{CP} = D^{*-} \pi^+ \end{aligned}$$

$$\begin{aligned} B_{\text{tag}} &= \bar{B}^0, f_{CP} = D^{*-} \pi^+ \\ B_{\text{tag}} &= B^0, f_{CP} = D^{*+} \pi^- \end{aligned}$$



# 信号事象 + 背景事象

- signal fraction に従って背景事象を加え、信号事象の  $\tau$ ,  $\Delta m$  を fit

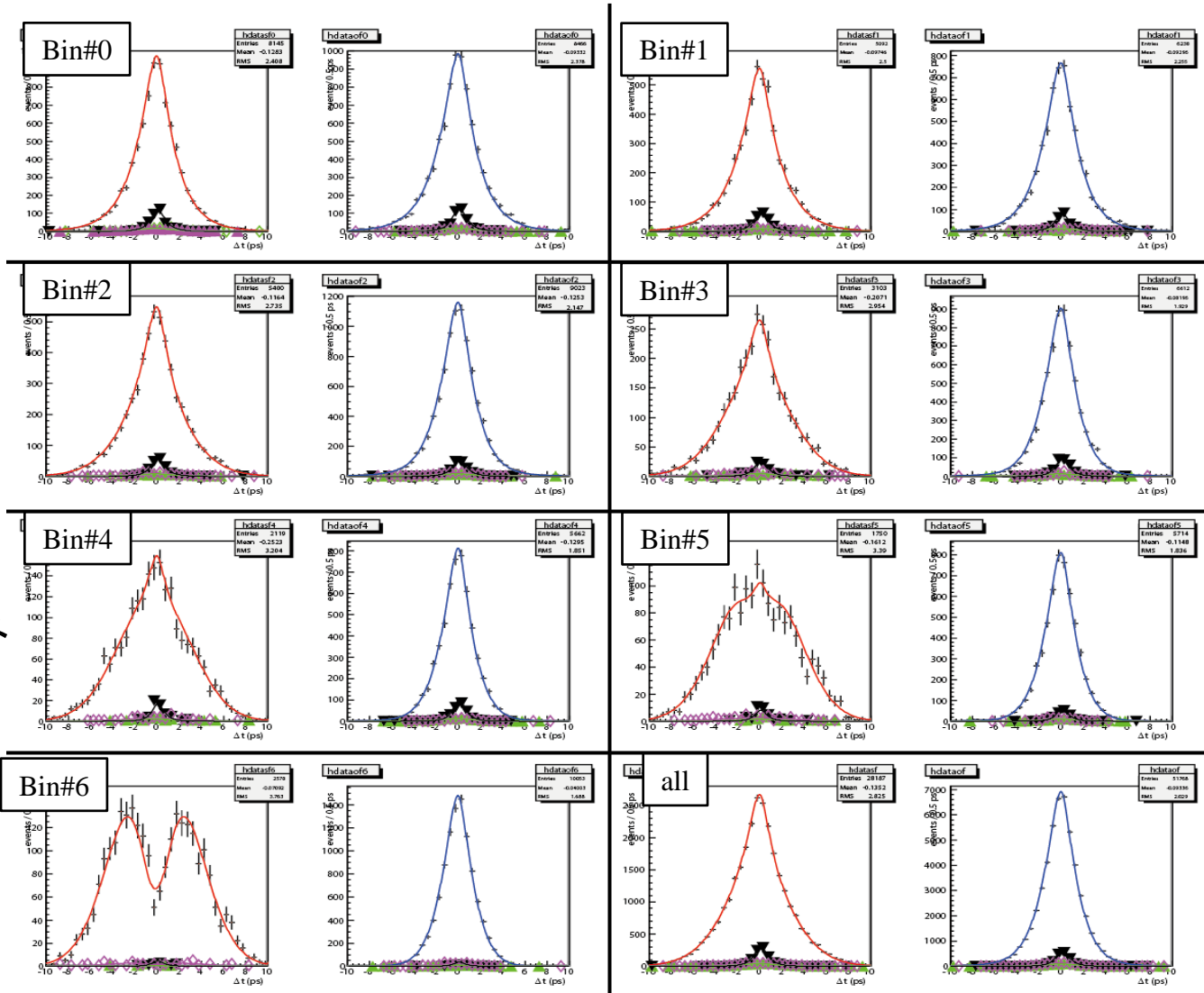
Name	Value	信号事象のみ
$\tau_{B0}$	$1.533 \pm 0.006$ (ps)	
$\Delta m$	$0.505 \pm 0.004$	

↓ + 背景事象

Name	Value
$\tau_{B0}$	$1.534 \pm 0.006$ (ps)
$\Delta m$	$0.506 \pm 0.004$

Fit 結果は信号事象のみと consistent.

背景事象 PDF が得られた



# まとめ

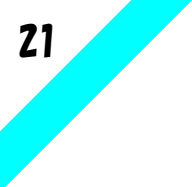
- $B \rightarrow D^* \pi$  解析を進行中.

## $\phi_3$ の測定

- $D^* \rightarrow D^0 \pi, D^0 \rightarrow K \pi$  を解析中
  - BG PDFs が MC から得られた

# 計画

- $S^\pm$  fit for MC
- 他の下位崩壊を加えての  $\Delta t$  fit



# Buck up

# Signal event selection

## ➤ 正確なvertex の決定のための Fast pion への要求

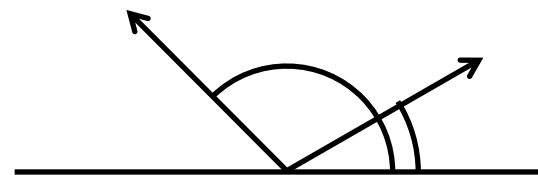
- Impact parameter

- radial :  $dr < 0.1 \text{ cm}$

- longitudinal :  $|dz| < 2.0 \text{ cm}$

- SVDにヒットをもつ

- Polar angle in the laboratory frame :  $30^\circ < \theta_{lab} < 135^\circ$



- The vertex positions are obtained by fits of the candidate tracks with the IP.

- Lepton, kaon hypothesis と一致しない

- Based on information from the CDC, TOF and ACC.

- Fast pion cms momentum :  $1.83 \text{ GeV}/c < p_{\pi_f} < 2.43 \text{ GeV}/c$

# Signal event selection

- Slow pion cms momentum :  $0.05 \text{ GeV}/c < p_{\pi_s} < 0.30 \text{ GeV}/c$
- Particle identification のとき、slow pion には何の条件も課さない
- Vertexing に使用しない
- IP から生じることのみ要求する
  
- fast pion とslow pion は逆の電荷をもつ

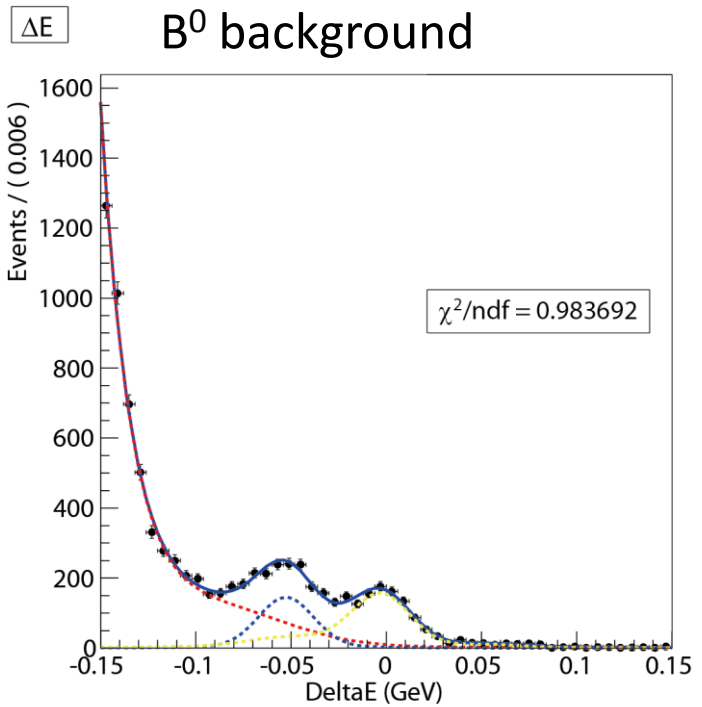
## 再構成

- $D^* \rightarrow D^0 \pi, D^0 \rightarrow K \pi$  信号選択

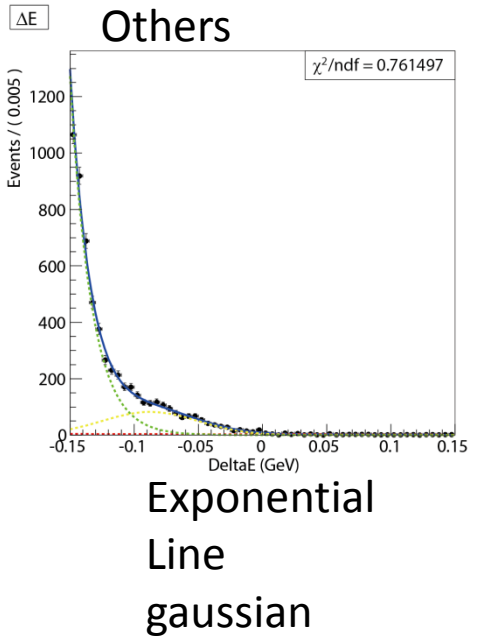
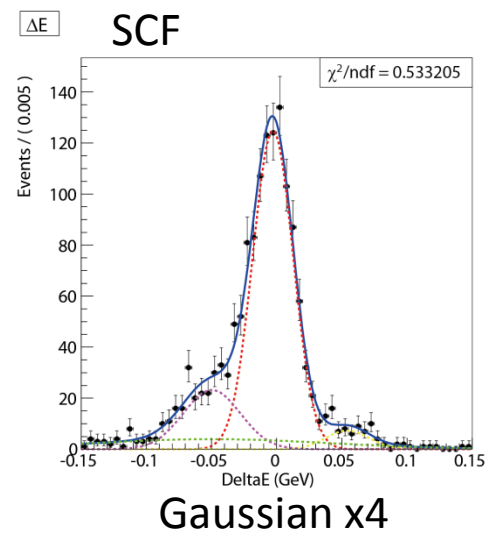
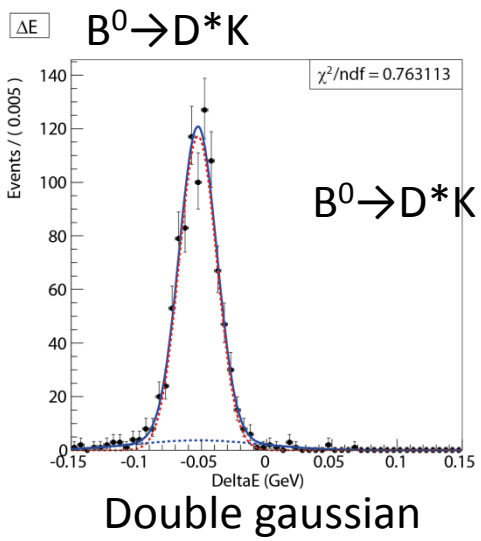
Slow $\pi$ 以外の $\pi$ SVD hit in $r\text{-}\phi \geq 1, z \geq 2$ $\text{Pid}(K/\pi) \leq 0.7$	$D^0$	$1.82 \text{ GeV} <  M_{K\pi}  < 1.92 \text{ GeV}$
	$D^*$	$0.143 \text{ GeV} < M_{D^*} - M_{D^0} < 0.148 \text{ GeV}$
K SVD hit : $\pi$ と同じ $\text{Pid}(K/\pi) \geq 0.3$	B	$5.2 \text{ GeV} < M_{bc} < 5.3 \text{ GeV}$ $-0.15 \text{ GeV} < \Delta E < 0.15 \text{ GeV}$ 最良候補選択 ( $M_{bc}, M_{D^*} - M_{D^0}$ )
	Slow $\pi$ 要求なし	



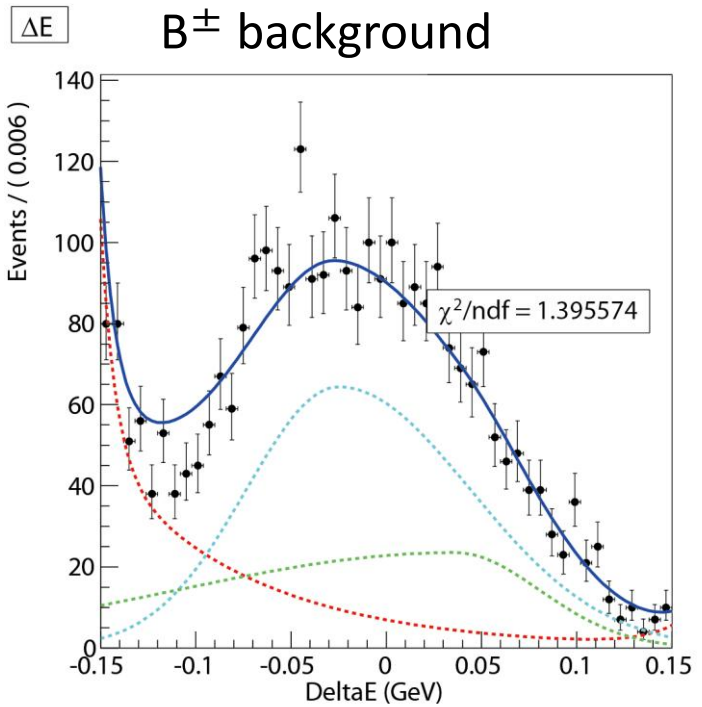
# Neutral B BG $\Delta E$ PDF



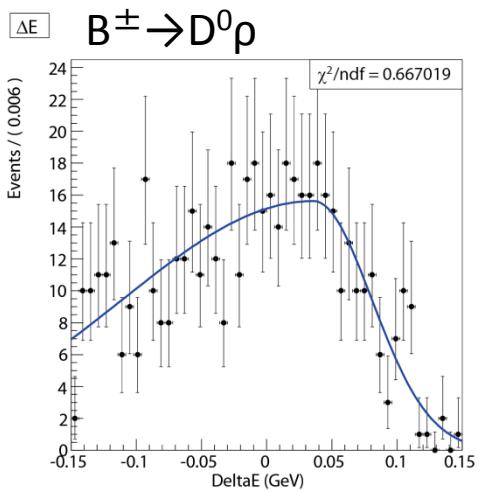
$B^0 \rightarrow D^*K$   
SCF  
Others



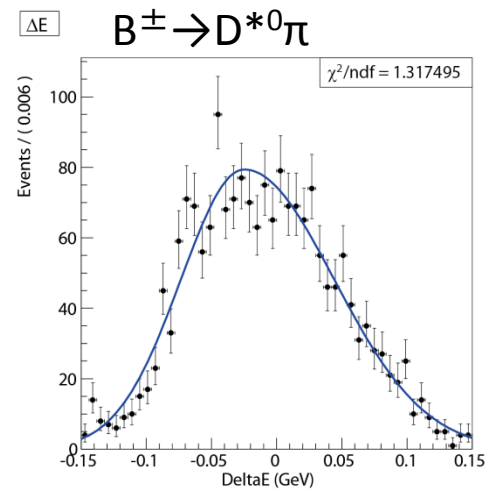
# Charged B BG $\Delta E$ PDF



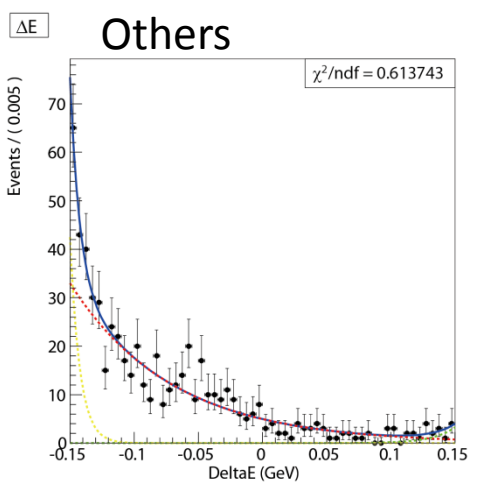
$B^\pm \rightarrow D^0 \pi$   
 $B^\pm \rightarrow D^0 \rho$   
 Others



Bifurcated gaussian



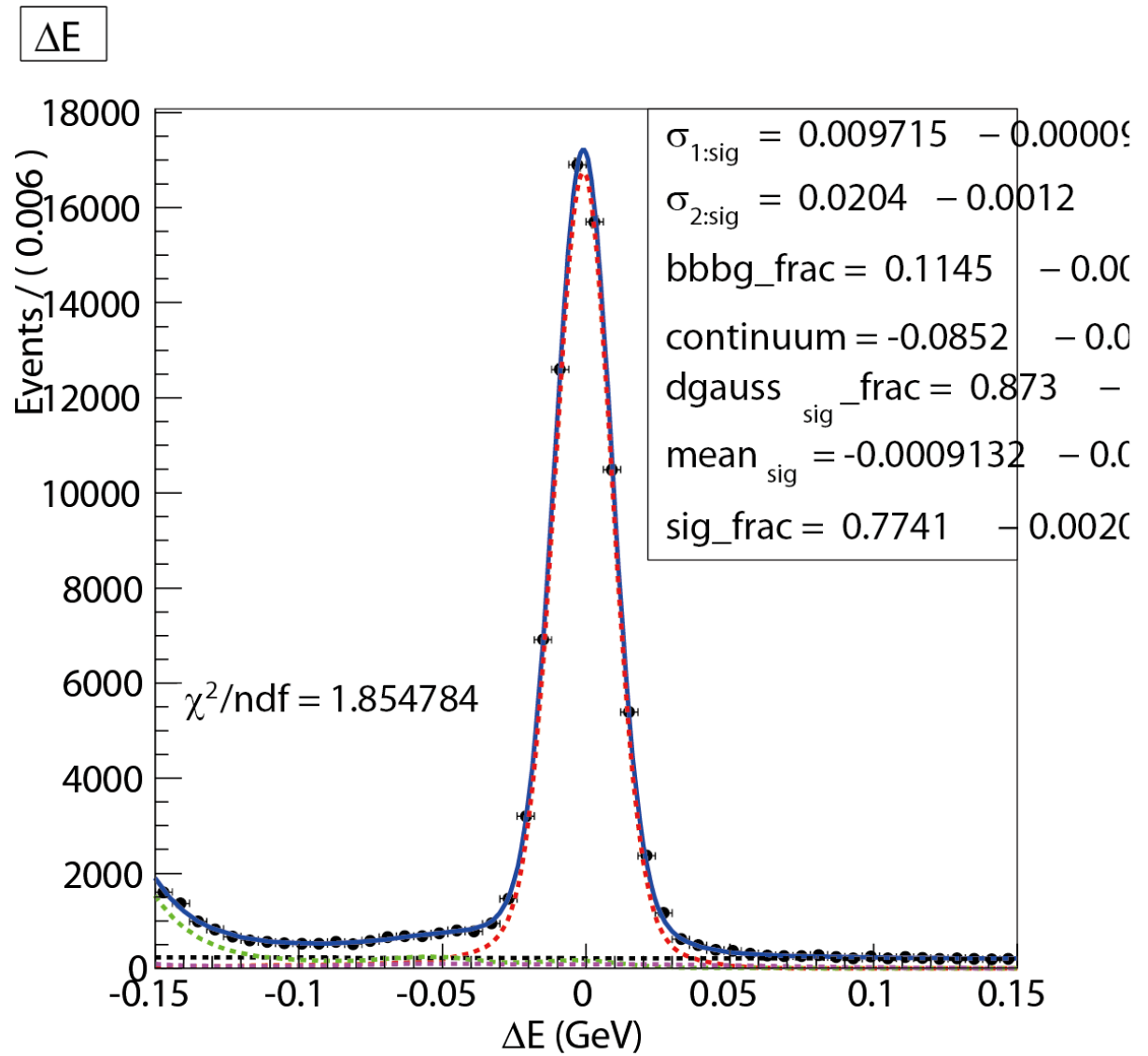
Bifurcated gaussian



Exponential x3

# B reconstruction

- Generic MC were reconstructed.
  - Case B
  - 5 streams



# r bin

- r bin : bin definition of the flavor tagging category

R bin #		wrong tag fraction for SVD2 MC	
Bin#0	$0 \leq  r  \leq 0.1$	$w = 0.5$	$\Delta w = 0.$
Bin#1	$0.1 <  r  \leq 0.25$	$w = 0.412222$	$\Delta w = 0.0569661$
Bin#2	$0.25 <  r  \leq 0.5$	$w = 0.307838$	$\Delta w = 0.0126192$
Bin#3	$0.5 <  r  \leq 0.625$	$w = 0.212765$	$\Delta w = 0.0147724$
Bin#4	$0.625 <  r  \leq 0.75$	$w = 0.149933$	$\Delta w = 0.000550289$
Bin#5	$0.75 <  r  \leq 0.875$	$w = 0.0913264$	$\Delta w = 0.00887704$
Bin#6	$0.875 <  r  \leq 1.0$	$w = 0.0218754$	$\Delta w = 0.00465683$

# Signal + $B^0\bar{B}^0$ Background

- To check the correctness of BG PDF, Signal +  $B^0\bar{B}^0$  BG was fitted.

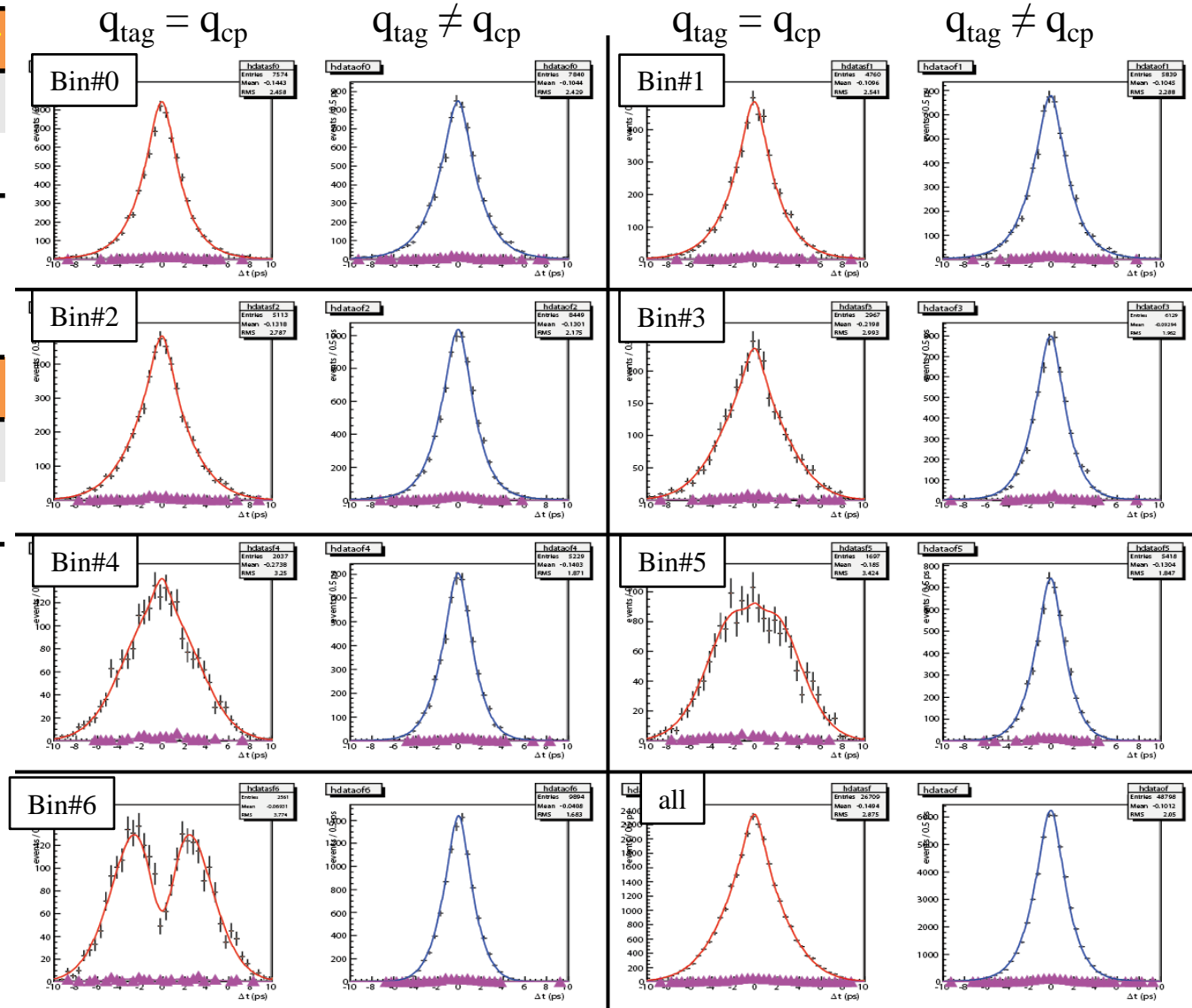
Name	Value	Signal Only
$\tau_{B^0}$	$1.533 \pm 0.006$ (ps)	
$\Delta m$	$0.505 \pm 0.004$	

↓

+  $B^0\bar{B}^0$  BG

Name	Value
$\tau_{B^0}$	$1.535 \pm 0.006$ (ps)
$\Delta m$	$0.505 \pm 0.004$

- Fit results for signal and signal +  $B^0\bar{B}^0$  BG are consistent.
- $B^0\bar{B}^0$  BG PDF were obtained.



# Signal + B<sup>+</sup>B<sup>-</sup> Background

- To check the correctness of BG PDF, Signal + B<sup>+</sup>B<sup>-</sup> BG was fitted.

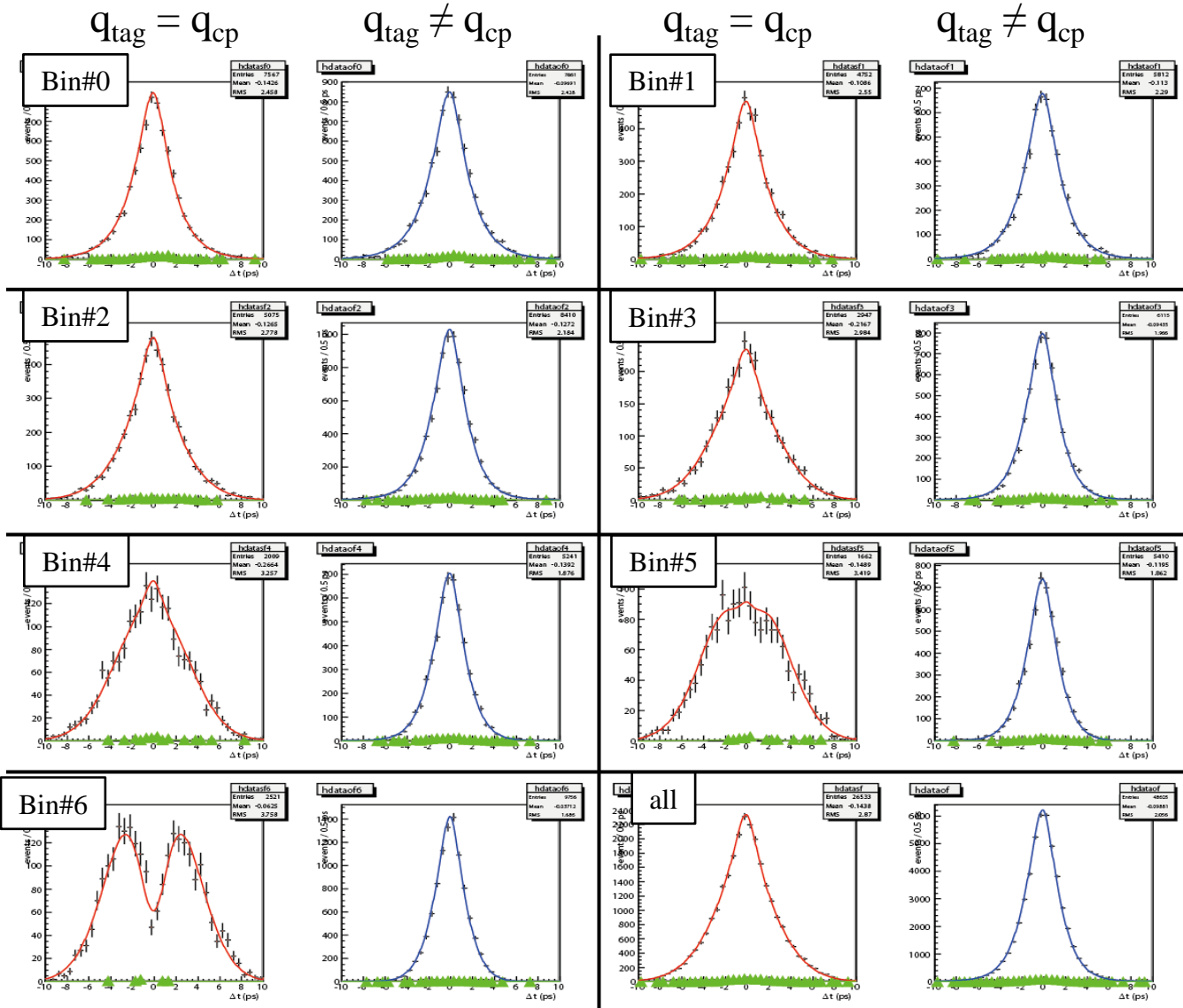
Name	Value	Signal Only
$\tau_{B0}$	$1.533 \pm 0.006$ (ps)	
$\Delta m$	$0.505 \pm 0.004$	



+ B<sup>+</sup>B<sup>-</sup> BG

Name	Value
$\tau_{B0}$	$1.535 \pm 0.006$ (ps)
$\Delta m$	$0.506 \pm 0.004$

- Fit results for signal and signal + B<sup>+</sup>B<sup>-</sup> BG are consistent.
- B<sup>+</sup>B<sup>-</sup> BG PDF were obtained.



# Signal + continuum Background

- To check the correctness of BG PDF, Signal + continuum BG was fitted.

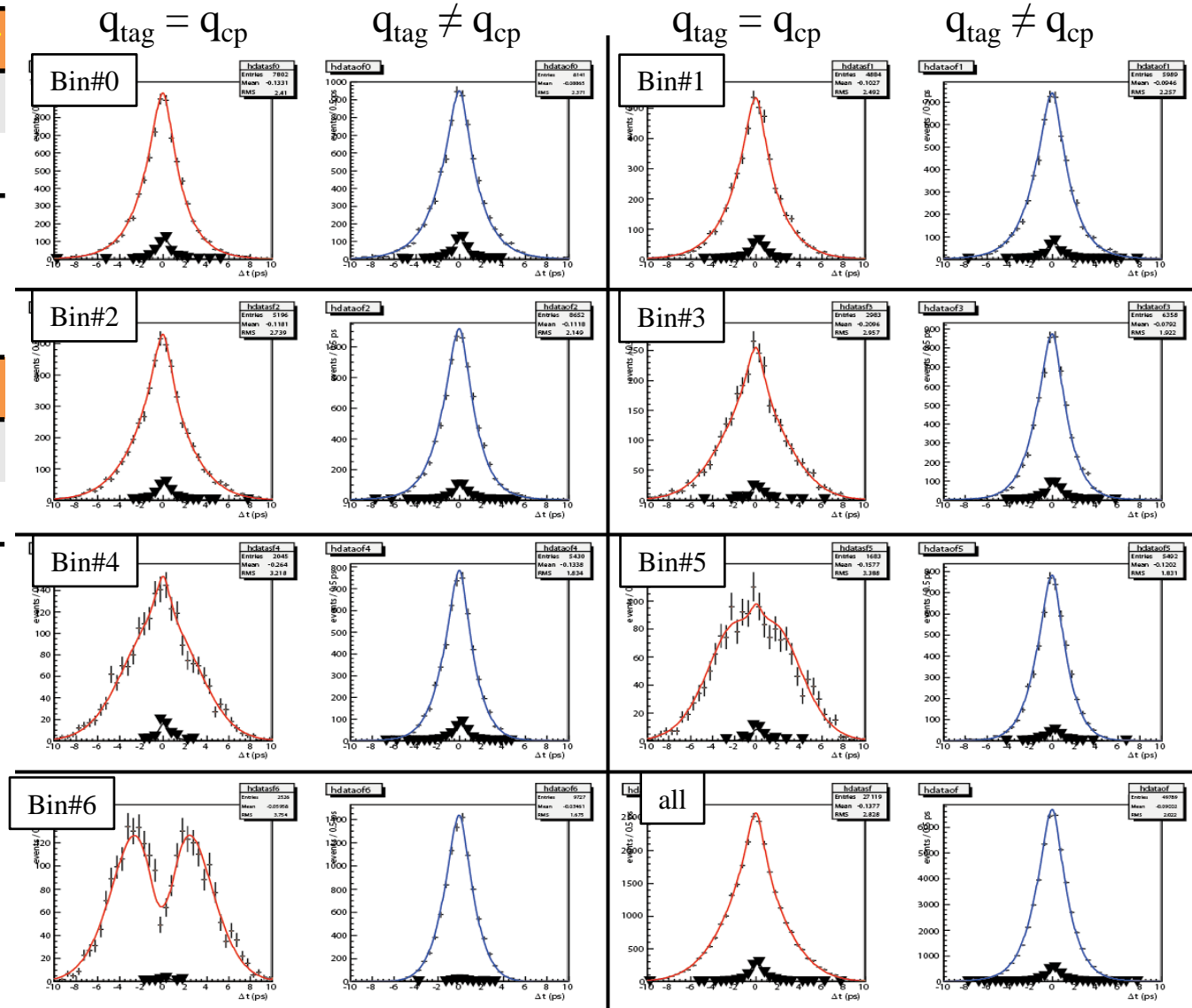
Name	Value	Signal Only
$\tau_{B0}$	$1.533 \pm 0.006$ (ps)	
$\Delta m$	$0.505 \pm 0.004$	

↓

+ continuum BG

Name	Value
$\tau_{B0}$	$1.534 \pm 0.006$ (ps)
$\Delta m$	$0.505 \pm 0.004$

- Fit results for signal and signal + continuum BG are consistent.
- **continuum BG PDF were obtained.**



# D\* $\pi$ 数

- $771.581 \times 10^6 \times 2.76 \times 10^{-3} = 2.13 \times 10^6$   
 –  $K\pi : \times 67.7 \times 10^{-2} \times 3.89 \times 10^{-2} = 56000$
- 使用する下位崩壊
  - D\*  $\rightarrow$  D<sup>0</sup> $\pi$  (67.7%)
    - D<sup>0</sup>  $\rightarrow$  K $\pi$  (3.89%), K $\pi\pi^0$  (13.9%), K $\pi\pi\pi$  (8.09%), K<sub>s</sub> $\pi\pi$  (2.94%)
  - D\*  $\rightarrow$  D $\pi^0$  (30.7%)
    - D  $\rightarrow$  K $\pi\pi$  (9.4%)