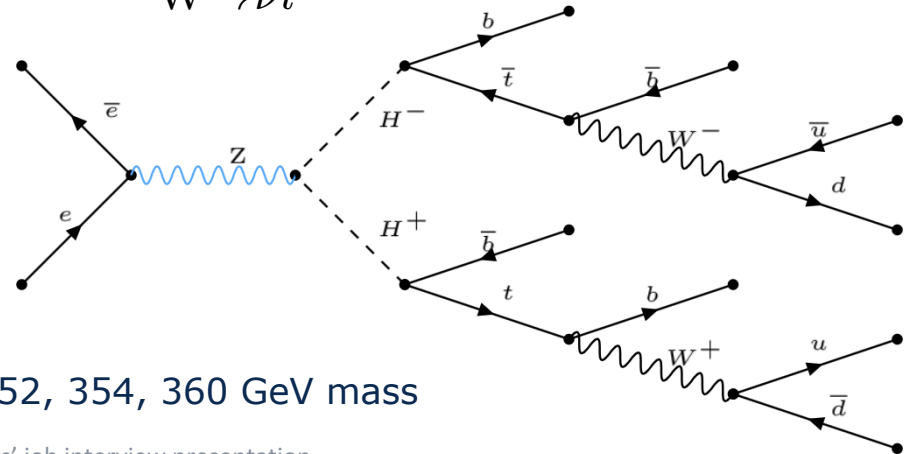


Overview

- Full simulation study of ILC/ILD
- $m_{H^\pm} = 350 \text{ GeV}$ cross section = 9 fb BR($H^\pm \rightarrow bt$) = 90%
- $E^+e^- \rightarrow H^+H^- \rightarrow tb \bar{t}b \rightarrow Wbb \bar{W}bb \xrightarrow{W \rightarrow 2 \text{ jets}} 8 \text{ jets}$ (hadronic)
- $Wbb \bar{W}bb \xrightarrow{W \rightarrow 2 \text{ jets}} 6 \text{ jets} + \text{lepton}$ (semi-lep.)
 $\xrightarrow{W \rightarrow \nu l}$
- Major background:
 - $ttH/ttZ/tt\gamma \rightarrow ttbb$
 - $tt \rightarrow bWbW$
 - $H/A \rightarrow bbbb$ (SUSY)
 - $H/A \rightarrow tt$ at resonance
 - Ignoring SUSY background
- Goal: m_{H^\pm} measurement
 - Samples with 340, 346, 348, 350, 352, 354, 360 GeV mass

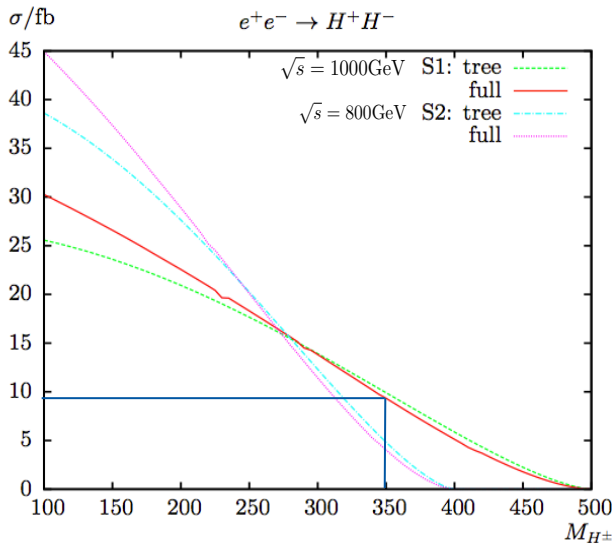


Cross section

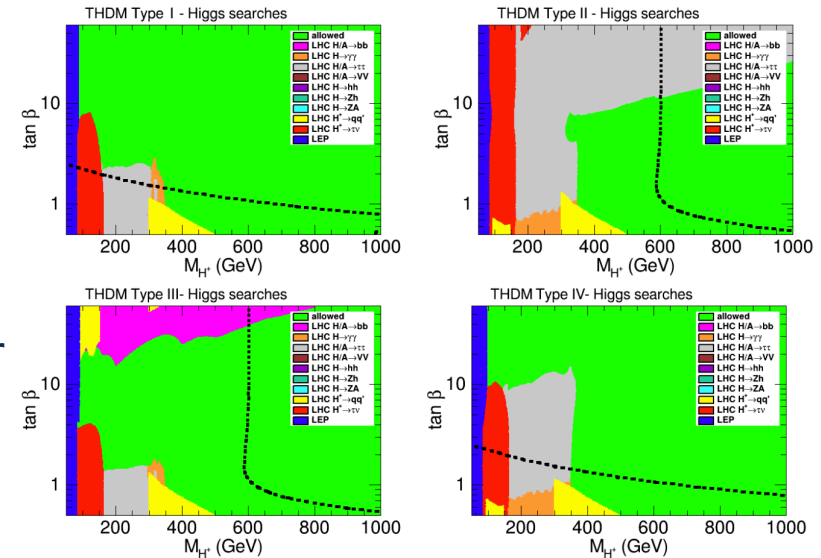
- $\sigma \approx 9 \text{ fb}$ with $P = (-80\%, 20\%)$ 10.4 fb
- $\mathcal{L} = 1000 \text{ 1/fb}$
- Hadronic: 5100 events
- Semileptonic: 3200 events

Allowed parameter space

Source: A. Arbey et al. "Status of the Charged Higgs Boson in Two Higgs Doublet Models." In: (2017). arXiv: 1706.07414 [hep-ph].

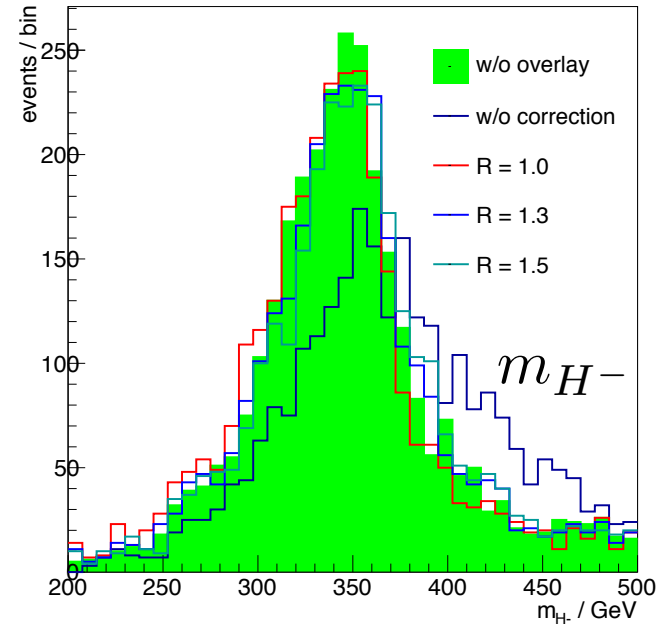
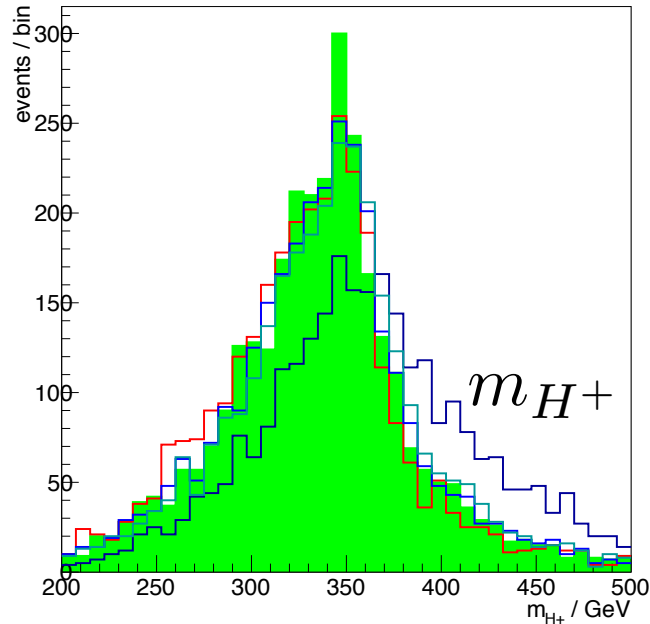


- MSSM excluded
- Brought parameter space allowed



Source: *Charged Higgs Boson production at ee colliders in the complex MSSM: a full one-loop analysis* Heinemeyer, S. and Schappacher, C. Eur. Phys. J. (2016)

Beam background reduction with kt-Algorithm



Reconstructed H^+ and H^- mass with realistic clustering and pairing with generator information



R chosen to be 1.3

Jet pairing

- Jet pairing with chi squared minimization
 - j_1, j_2, j_3 and j_4 – jets with highest b-tag
 - For semi-leptonic: j_7 and j_8 are neutrino and lepton

$$\chi^2 = \left| \frac{(m_{j_1 j_2 j_3 j_4})^2 - (m_{j_5 j_6 j_7 j_8})^2}{2\sigma_{H^+}^2} \right| + \left(\frac{m_{j_2 j_3 j_4} - M_t}{\sigma_t} \right)^2 + \left(\frac{m_{j_6 j_7 j_8} - M_t}{\sigma_t} \right)^2 + \left(\frac{m_{j_3 j_4} - M_W}{\sigma_W} \right)^2 + \left(\frac{m_{j_7 j_8} - M_W}{\sigma_W} \right)^2$$

	w/o overlay	R: 1.3	with overlay	
B-tag efficiency	44.6	42.5	38.0	the 4 b-jets have highest b-tag in the event
Clustering works well	50.7	49.4	40.2	For every color singlet there are 2 jets with a major fraction from this singlet
Pairing works	27.8	25.0	17.2	Jet pairing agrees with major color singlet fraction in jet

Neutrino four momentum

- Missing-Energy-Method (MEM)

$$p_{\text{vis}} = \sum_{i=1}^{N_{\text{PFO}}} p_i \quad p_{\text{CMS}} = (1000, 0, 0, 1000 \cdot \sin(0.014/2))$$

$$p_{\nu, \text{MEM}} = (p_{\text{CMS}} - p_{\text{vis}})$$

- Standard for most studies
- Missing-Direction-Method (MDM)
 - Using the Direction of Missing-Energy-Method and calculation the Energy by fixing W-Mass

$$E_{\nu, \text{NDM}} = \frac{m_W^2}{E_l(1 - \alpha)} \quad \alpha = \frac{\vec{p}_{\nu, \text{MEM}} \cdot \vec{p}_l}{|\vec{p}_{\nu, \text{MEM}}| |\vec{p}_l|}$$

$$p_{\nu, \text{NDM}} = \left(E_{\nu, \text{NDM}}, E_{\nu, \text{NDM}} \frac{\vec{p}_{\nu, \text{MEM}}}{|\vec{p}_{\nu, \text{MEM}}|} \right)$$

Neutrino four momentum

- Missing Momentum Method (MMM)
 - Using momentum from MEM for energy estimation

$$p_{\nu, \text{MMM}} = (|\vec{p}_{\nu, \text{MEM}}|, \vec{p}_{\nu, \text{MEM}})$$

- Missing Transversal Momentum Method (MTMM)
 - Using only the momentum in transversal momentum

$$\frac{m_W^2}{2} = E_\nu E_\ell - \vec{p}_\nu \vec{p}_\ell = E_\ell \sqrt{p_{\nu x}^2 + p_{\nu y}^2 + p_{\nu z}^2} - p_{\nu x} p_{\ell x} - p_{\nu y} p_{\ell y} - p_{\nu z} p_{\ell z}$$

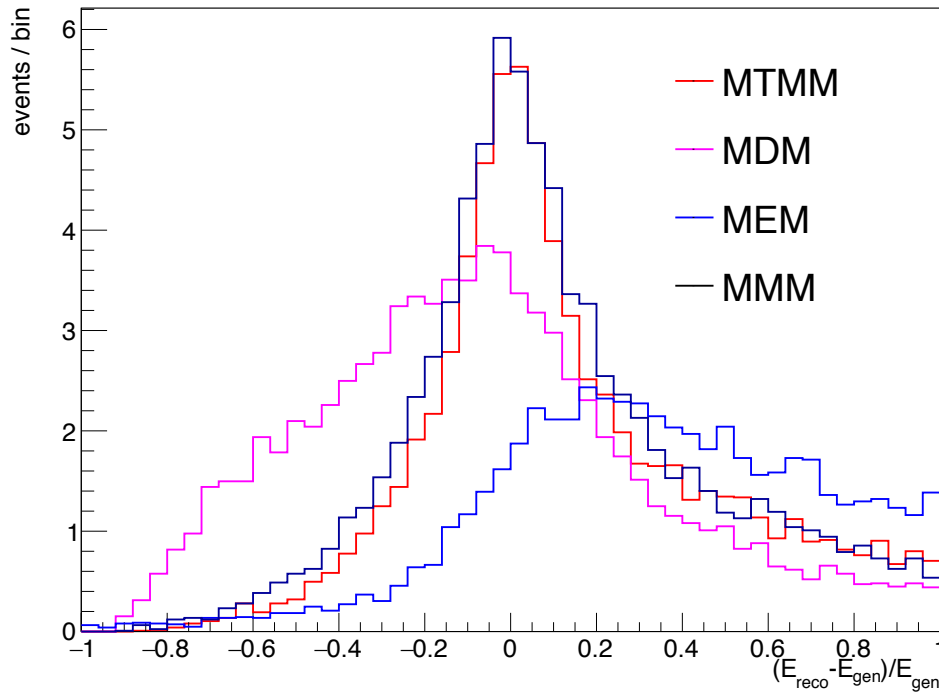
has two solutions

$$p_{\nu z} = \frac{\pm K + p_{\ell z} [2(p_{\ell y} p_{\nu y} + p_{\ell x} p_{\nu x}) + m_W^2]}{2(p_{\ell x}^2 + p_{\ell y}^2)}$$

$$K = E_\ell \sqrt{4[(2p_{\ell x} p_{\nu x} + m_W^2) p_{\ell y} p_{\nu y} - p_{\ell x}^2 p_{\nu y}^2 - p_{\ell y}^2 p_{\nu x}^2 + m_W^2 p_{\ell x} p_{\nu x}] + m_W^4}$$

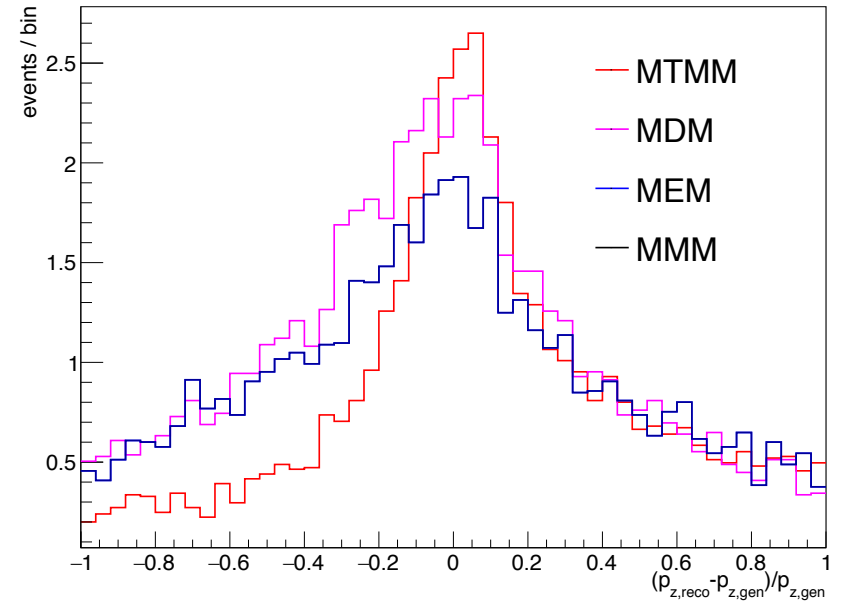
Neutrino reconstruction

Neutrino energy



MTMM	Transversal momentum
MDM	Direction
MEM	Standard with missing energy
MMM	Only using momentum

Neutrino momentum in z-direction



Event selection

- Different event selections were used
 - Static cuts
 - BDT
- Optimizations
 - Signal significance
 - Significance for correctly paired signal (BDT + separate BDTG)

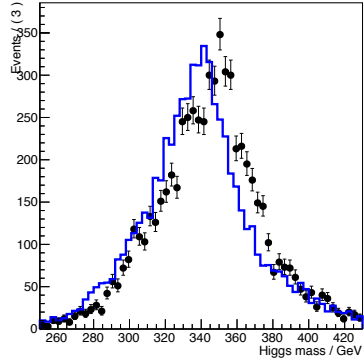
Cut type	Optim. type	Mode	Sig	o. Sig	Z(h)	$t\bar{t}Z$	$t\bar{t}b\bar{b}$	$t\bar{t}(sl)$	$t\bar{t}(h)$	$t\bar{t}h(sl)$	$t\bar{t}h(h)$	other
Static cuts		(h)	1982	46	0	138	106	454	16	200	12	0
Static cuts		(sl)	3090	586	139	208	181	95	678	53	327	26
Static cuts	corr. paired	(h)	579	699	0	50	61	112	2	103	4	0
Static cuts	corr. paired	(sl)	721	1154	0	46	54	12	122	12	121	0
BDT		(h)	2156	59	0	136	104	363	12	206	18	5
BDT		(sl)	3495	519	139	215	161	59	640	39	373	23
BDT	corr. paired	(h)	671	483	0	24	27	65	2	54	2	0
BDT	corr. paired	(sl)	865	936	0	18	30	5	63	4	69	0

Table 2.10: Remaining background after the event selections; (h) stands for hadronic and (sl) stands for semi-leptonic

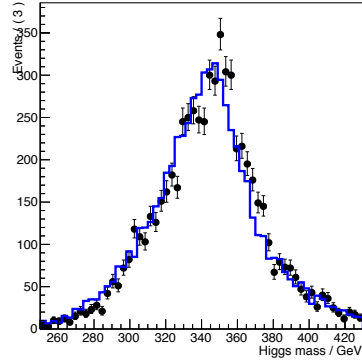
Mass measurement

- Template method
 - Compare mass distribution shape -> calculation χ^2
 - Get uncertainty from χ^2 parabola
- Shape method
 - Get shape of BG, correctly paired signal and false paired signal
 - Calibrate fitted mean to Higgs mass
- Combined method
 - Reduce fitting variables to Higgs mass from cor. and false paired signal

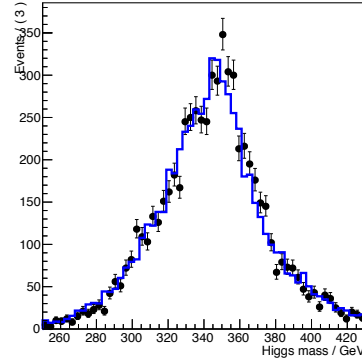
Template fit for $m_{H^\pm} = 340$ GeV



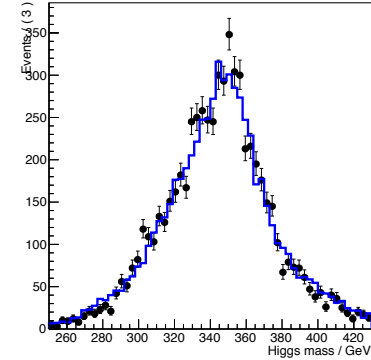
Template fit for $m_{H^\pm} = 346$ GeV



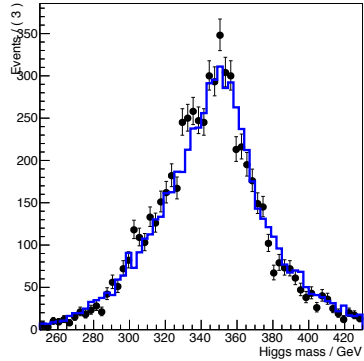
Template fit for $m_{H^\pm} = 348$ GeV



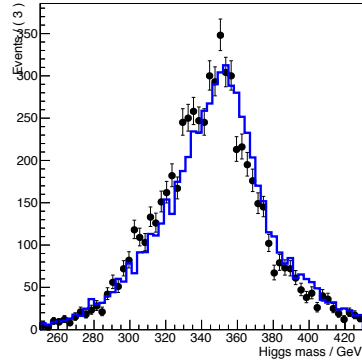
Template fit for $m_{H^\pm} = 350$ GeV



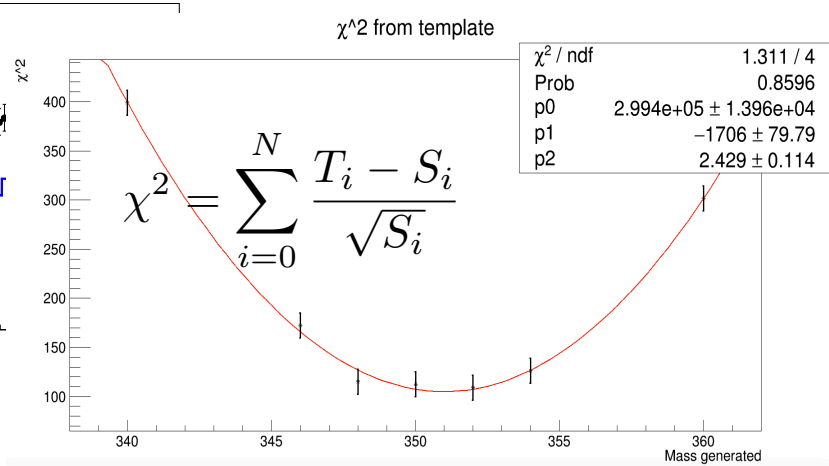
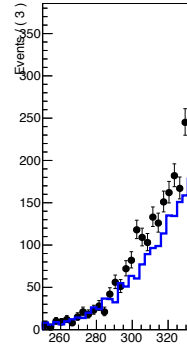
Template fit for $m_{H^\pm} = 352$ GeV



Template fit for $m_{H^\pm} = 354$ GeV

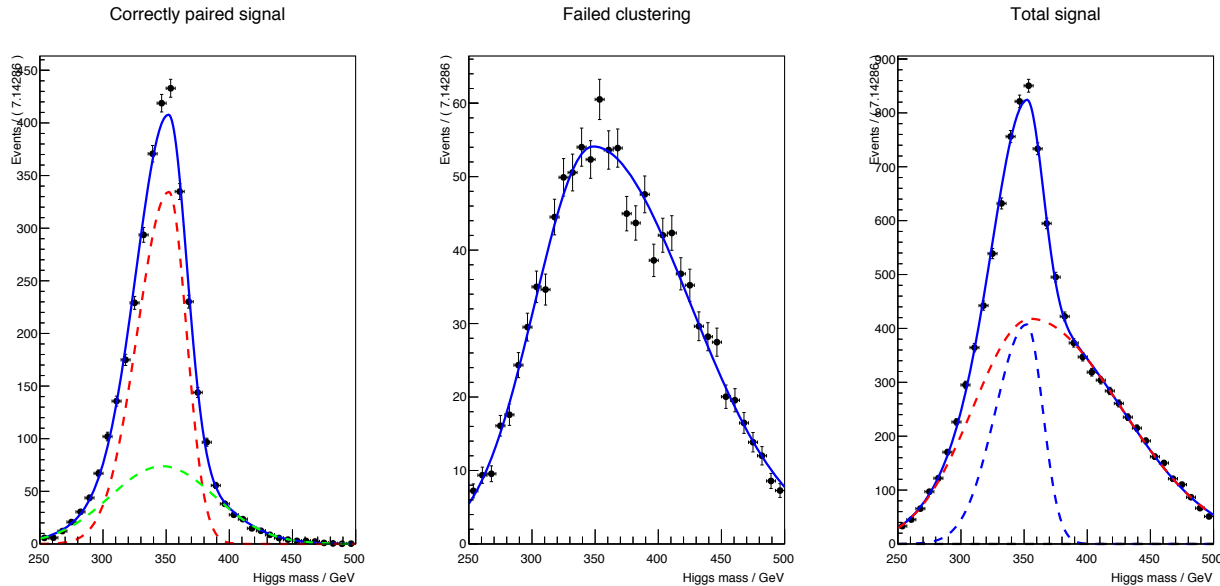


Template fit for $m_{H^\pm} = 360$ GeV



Shape method

- Get signal shape (Static Cuts)



Static cuts

N_s (exp.) = 5491

Correctly paired (24.5%):

- μ : 352.1 GeV
- σ_L : 24.8 GeV
- σ_R : 12.8 GeV

Wrong paired (75.5%):

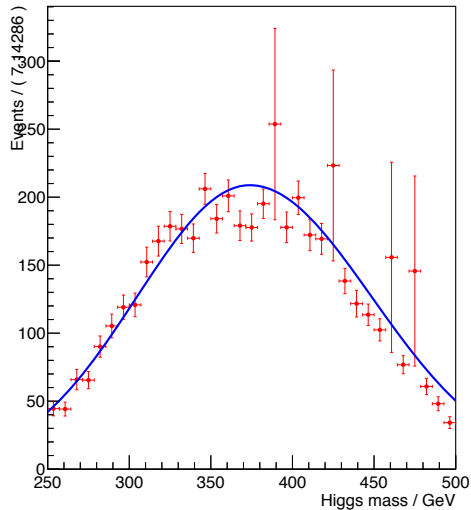
- μ : 355.1 GeV
- σ_L : 45.6 GeV
- σ_R : 71.5 GeV

red. $\chi^2 = 2.05$

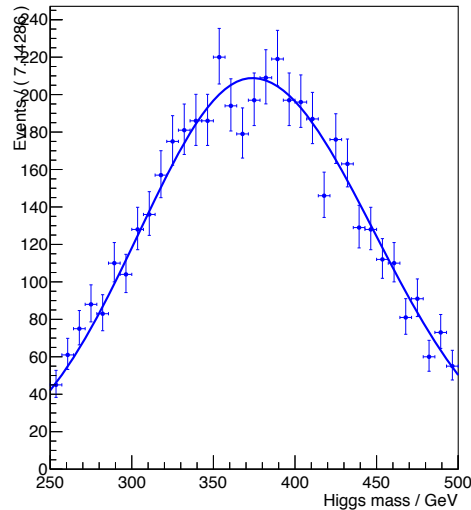
Shape method

- Get background shape (Static Cuts)

Background fit to BiGauss (original)



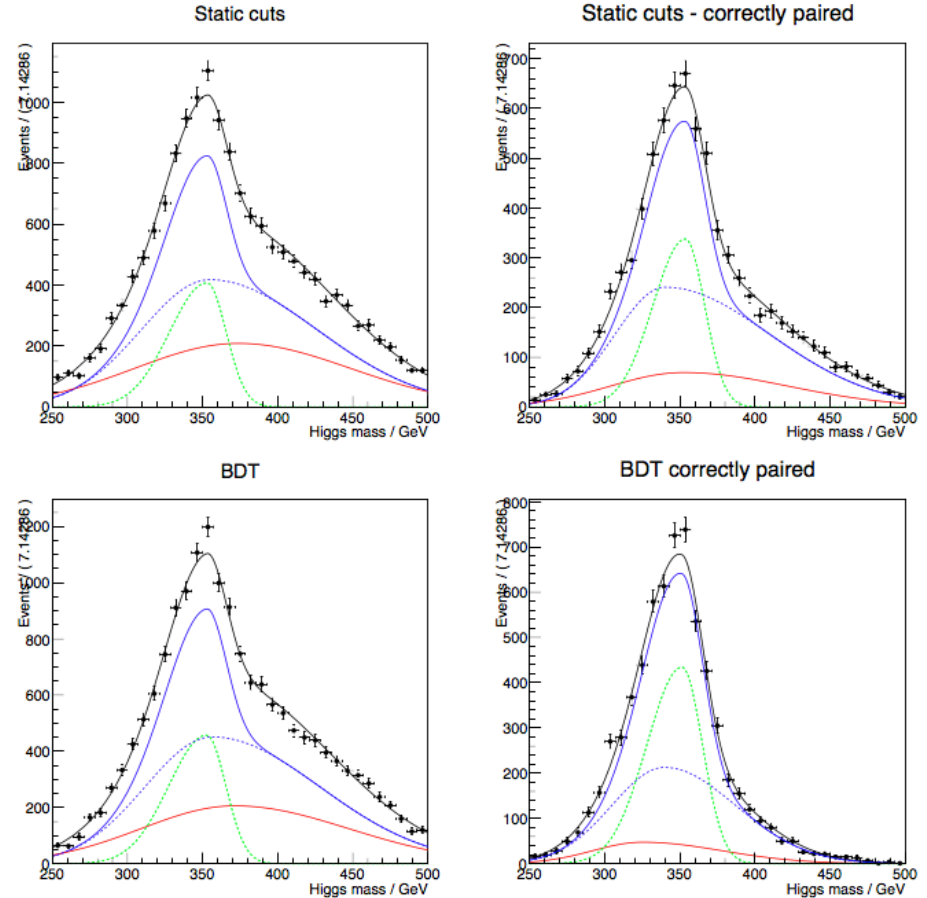
Background p.d.f. and generated data set



Static cuts
 N_B (exp.) = 2418
 μ = 373.8 GeV
 σ_L : 69.2 GeV
 σ_R : 74.8 GeV
 red. χ^2 (original BG) = 3.06
 red. χ^2 (gen BG) = 0.96

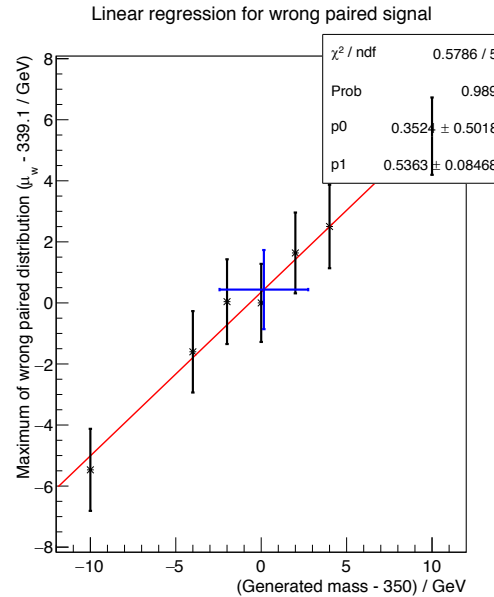
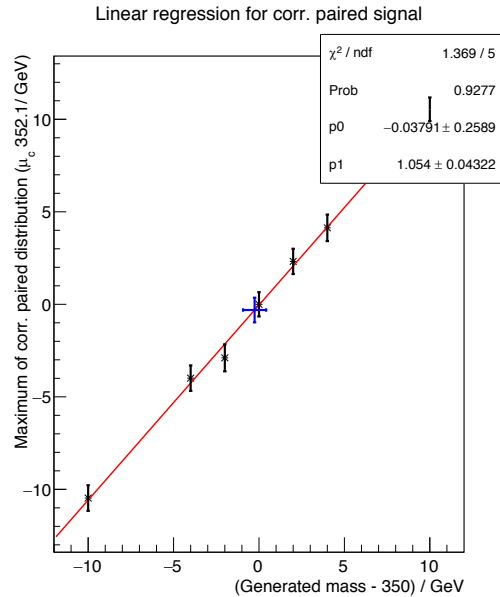
Added fit

- Added fit for different event selections for shape method
- All fit parameter fixed except mean of signal distributions
- **Background**
- **Signal (solid)**
 - Wrong paired signal (dashed)
 - Correctly paired signal



Shape method – mass estimation (BDT – correctly paired)

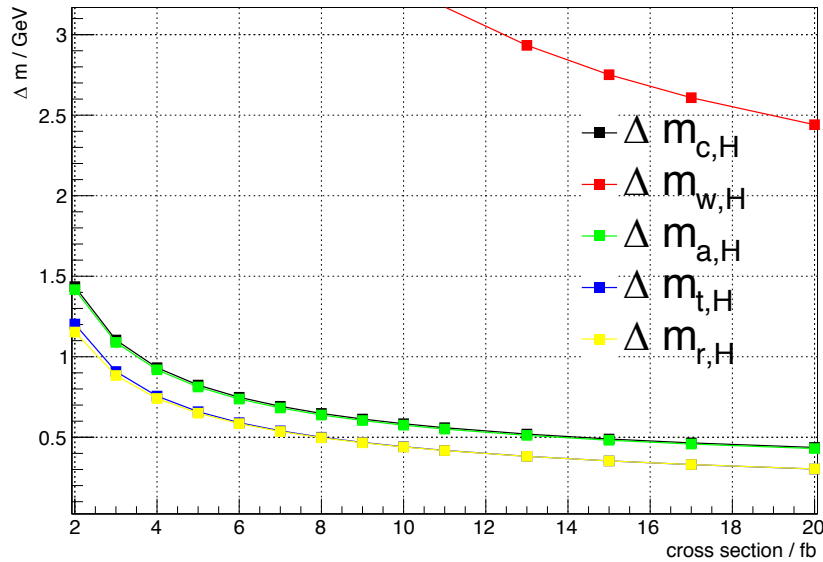
- Linear regression for signal distribution maximum and generated mass
- Test data set (blue)



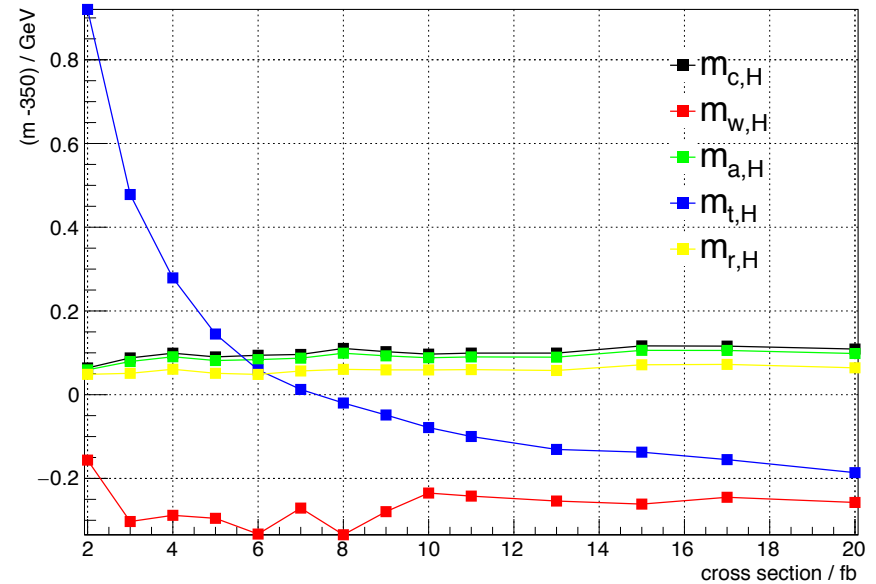
BDT correctly paired	
$m_{c,H}/\text{GeV}$	$= 349.74 \pm 0.68$ (Corr. pairing)
$m_{w,H}/\text{GeV}$	$= 350.16 \pm 2.59$ (Wrong pairing)
$m_{a,H}/\text{GeV}$	$= 349.77 \pm 0.66$ (combined)
$m_{r,H}/\text{GeV}$	$= 349.83 \pm 0.46$ (reduced)
$\Delta_{c,\text{const}}$	$: 0.2456$
$\Delta_{c,\text{linear}}$	$: -0.012$
$\Delta_{c,\text{fit}}$	$: 0.6319$
$m_{c,H}/\text{GeV}$	$= (1.05 \pm 0.04) \mu_c + (352.1 \pm 0.26)$
$m_{w,H}/\text{GeV}$	$= (0.54 \pm 0.08) \mu_w + (339.09 \pm 0.5)$

MC toy with varied cross section (BDT – correctly paired)

Mass uncertainty with TMVA correctly paired optimized



Mass deviation with TMVA correctly paired optimized

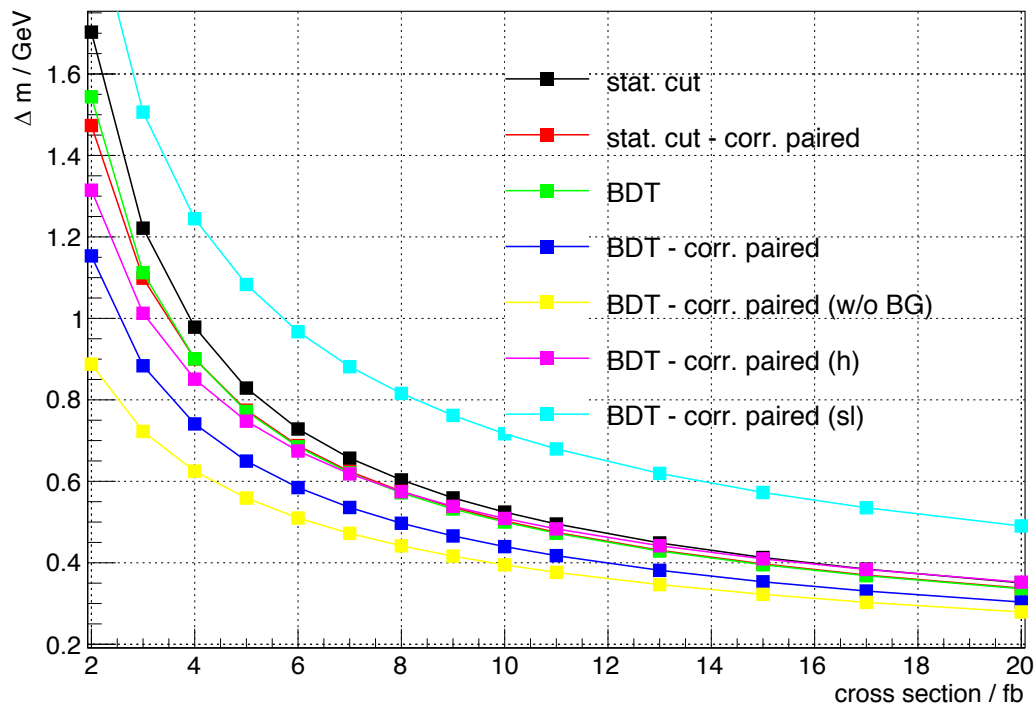


- Result from 10 000 toy MC

MC toy with varied cross section (BDT – correctly paired)

Mass uncertainty with reduced shape method

- Result from 10 000 toy MC samples
- 0.5 GeV mass precision
- Optimization for correctly paired signal beneficial



Result

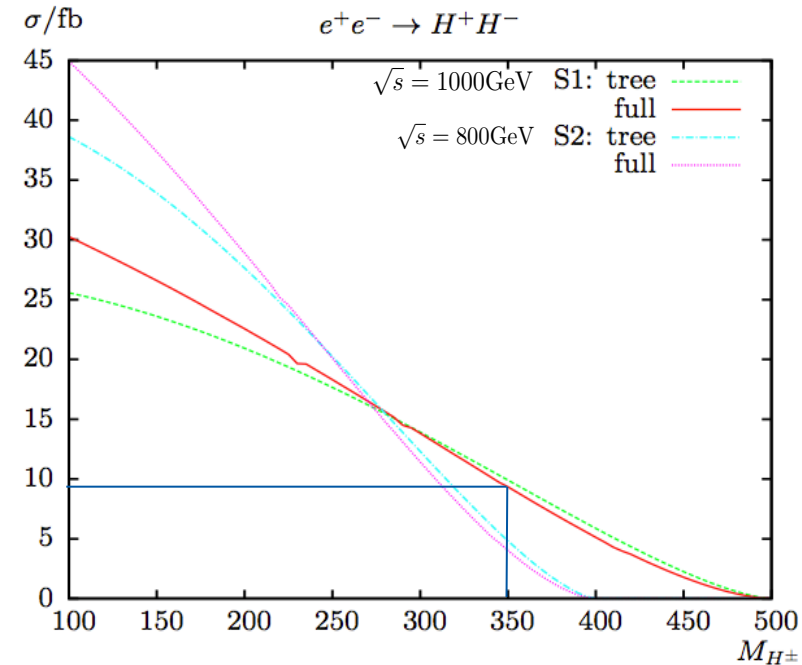
- 0.5 GeV mass precision
- Neutrino four momentum reconstruction with Missing Momentum Method was used
- Missing Transversal Momentum Method has great potential

Cut type	Optim. type	Mode	Corr. pair				mass precision with $\sigma = 9$ fb
			Signif.	Signif.	Effi.	Purity	
Static cuts		hadronic	44.6	17.9	65 %	64 %	0.56 GeV
Static cuts		semi-lep.	36.5	17.3	43 %	67 %	
Static cuts	corr. paired	hadronic	37.2	21.9	62 %	66 %	0.54 GeV
Static cuts	corr. paired	semi-lep.	31.5	19.0	55 %	63 %	
BDT		hadronic	49.1	20.9	73 %	67 %	0.53 GeV
BDT		semi-lep.	38.6	19.4	46 %	71 %	
BDT	corr. paired	hadronic	38.5	26.6	74 %	82 %	0.47 GeV
BDT	corr. paired	semi-lep.	31.5	23.0	64 %	79 %	

Backup

Cross section

- $\sigma \approx 9 \text{ fb}$ with $P = (-80\%, 20\%)$ 10.4 fb
- $\mathcal{L} = 1000 \text{ 1/fb}$
- $N = 10400 \text{ H}^\pm \text{ events}$
- Assuming $\text{BR}(\text{H}^\pm \rightarrow \text{tb}) = 90\%$
- $\text{BR}(\text{t} \rightarrow \text{bW}) = 100\%$
- $\text{BR}(\text{W} \rightarrow 2\text{jets}) = 67.6\%$
- $\text{BR}(\text{W} \rightarrow \text{ev}) = 10.75$
- $\text{BR}(\text{W} \rightarrow \text{ev}) = 10.57$
- Hadronic: 5100 events
- Semileptonic: 3200 events



Source: ***Charged Higgs Boson production at ee colliders in the complex MSSM: a full one-loop analysis***

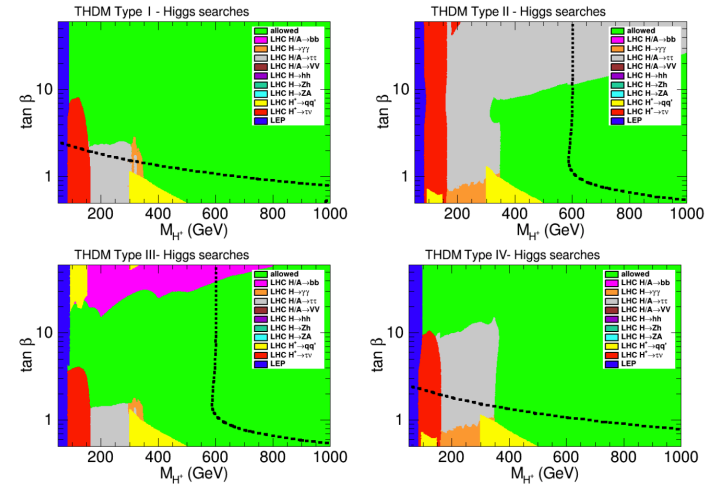
Heinemeyer, S. and Schappacher, C. Eur. Phys. J. (2016)

Allowed parameter space

Source: A. Arbey et al. “Status of the Charged Higgs Boson in Two Higgs Doublet Models.” In: (2017). arXiv: 1706.07414 [hep-ph].

Type	U_R	D_R	L_R	λ_{UU}	λ_{DD}	λ_{LL}
I	+	+	+	$\cot \beta$	$\cot \beta$	$\cot \beta$
II	+	-	-	$\cot \beta$	$-\tan \beta$	$-\tan \beta$
III	+	-	+	$\cot \beta$	$-\tan \beta$	$\cot \beta$
IV	+	+	-	$\cot \beta$	$\cot \beta$	$-\tan \beta$

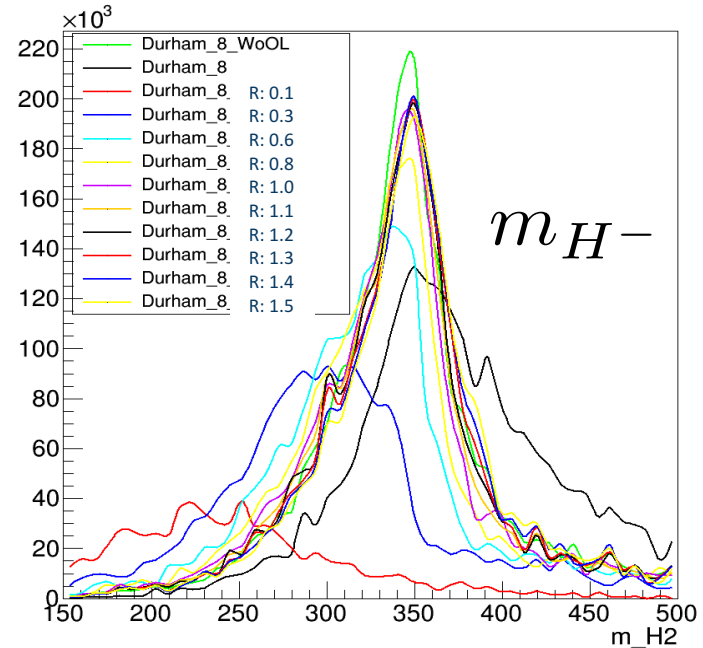
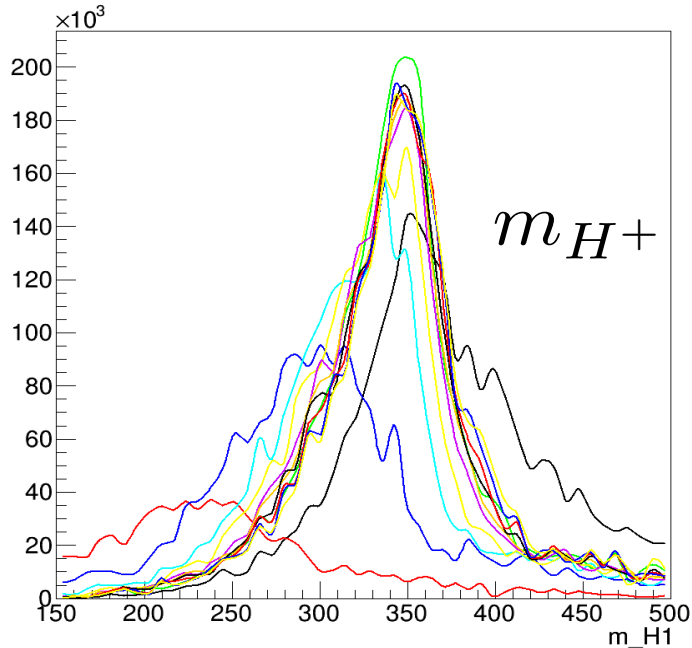
Table 1. Assignment of Z_2 charges for the right-handed fermions, and the resulting relations among Yukawa coupling matrices in the Z_2 -symmetric types of 2HDM Yukawa sectors. The Higgs doublets Φ_1 and Φ_2 have Z_2 quantum numbers $-$ and $+$, respectively.



Analysis Overview


- Isolated Lepton selection
- Reduce beam background by kt-Algorithm
- Jet-clustering and flavor tagging (LCFIplus)
- Calculating neutrino four-momentum (only semi-leptonic)
- Jet-pairing
- Extracting signal and background mass shape
- Added fit to find Higgs-mass

Find R for kt-Algorithm



Reconstructed H^+ and H^- mass with realistic clustering and pairing with generator information

Chi² - Jet Pairing (hadronic)

	w/o overlay	R: 1.3	with overlay	
B-tag efficiency 	44.6	42.5	38.0	the 4 b-jets have highest b-tag in the event
Clustering works well	50.7	49.4	40.2	For every color singlet there are 2 jets with a major fraction from this singlet
Pairing works	27.8	25.0	17.2	Jet pairing agrees with major color singlet fraction in jet

$$\chi^2 = \left| \frac{(m_{j_1 j_2 j_3 j_4})^2 - (m_{j_5 j_6 j_7 j_8})^2}{2\sigma_{H^+}^2} \right| + \left(\frac{m_{j_2 j_3 j_4} - M_t}{\sigma_t} \right)^2$$

$$+ \left(\frac{m_{j_6 j_7 j_8} - M_t}{\sigma_t} \right)^2 + \left(\frac{m_{j_3 j_4} - M_W}{\sigma_W} \right)^2 + \left(\frac{m_{j_7 j_8} - M_W}{\sigma_W} \right)^2$$

Lepton Selection

- Using the IsolatedLeptonTaggingProcessor
 - From MarilnReco
 - Based on MVA
- Open task: reduce false Lepton Tag in hadronic Channel
 - With event shape or b-tag
 - But actually the pairing efficiency is not effected

	Total (%)	w/o tau (%)
Lepton Tag	60.3	90.4
Correct Tag	60.0	90.0
False Lepton Tagged	0.3	0.4
Electron	29.5	89.4 (w/o tau and myon)
Myon	30.3	90.5 (w/o tau and electron)
False Lepton Tag in hadronic	2.1	