

ϕ_3/γ measurement at Belle



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LLWI'08
Feb. 20th, 2008

Outline

Introduction

Overview of ϕ_3/γ measurements

New result on $B^- \rightarrow [K^+ \pi^-]_D K^-$

Introduction

- CKM (Cabbibo-Kobayashi-Maskawa) matrix
 - The quark mixing matrix, which is unitary.

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

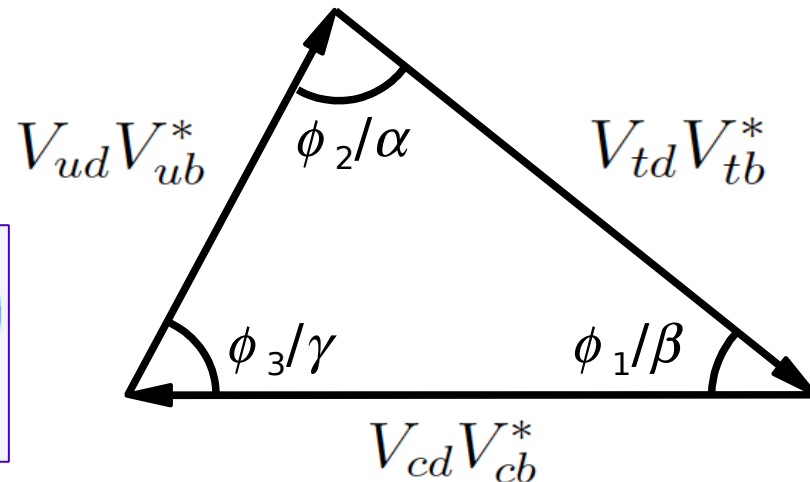
Complex phase

- The Unitarity Triangle

$$V_{ud}V_{ub}^* + V_{cd}V_{cb}^* + V_{td}V_{tb}^* = 0$$

$$\phi_3/\gamma \equiv \arg \left(\frac{V_{ud}V_{ub}^*}{-V_{cd}V_{cb}^*} \right)$$

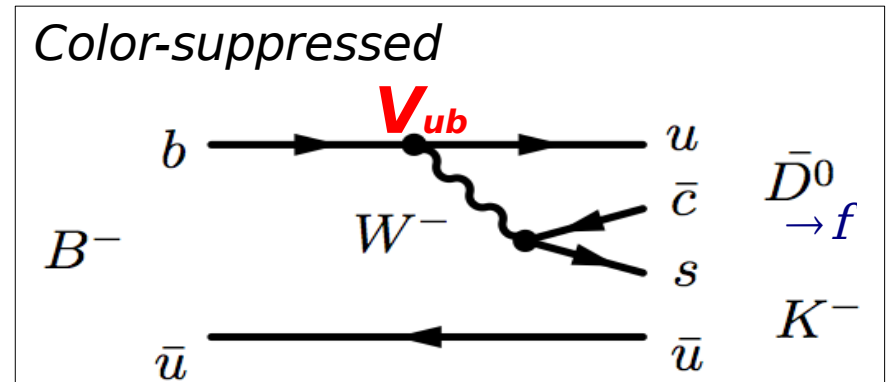
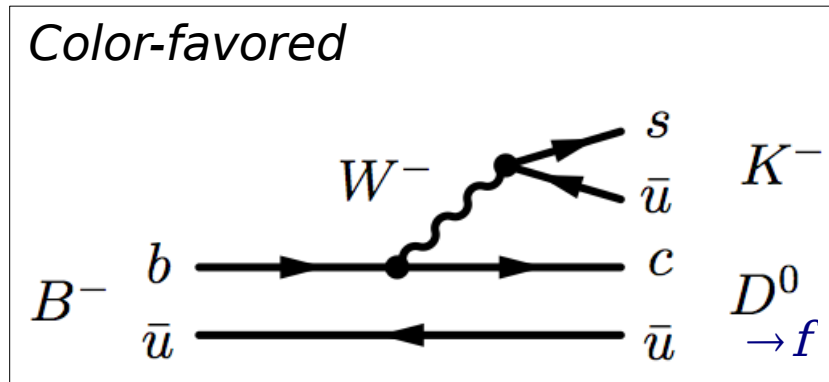
$$\sim -\arg(V_{ub})$$



Methods of ϕ_3/γ measurements

◦ $B^- \rightarrow D^{(*)} K^{(*)-}$

(No penguin)



- Access ϕ_3 using the same final state f of D^0 and \bar{D}^0 decays.
- Basically, we extract ϕ_3 with the ratio of the amplitudes

$$r_B \equiv \left| \frac{A(B^- \rightarrow \bar{D}^0 K^-)}{A(B^- \rightarrow D^0 K^-)} \right|$$

r_B is a crucial parameter in ϕ_3 measurement.

(Expected to be 0.1-0.2.)

◦ $B \rightarrow D^{(*)\pm} \pi^\mp, D^\pm \rho^\mp$

- Extract $\sin(2\phi_1 + \phi_3)$ by the studies of $B^0 - \bar{B}^0$ transitions.

Methods of ϕ_3/γ measurements

◦ $B^- \rightarrow D^{(*)} K^{(*)-}$

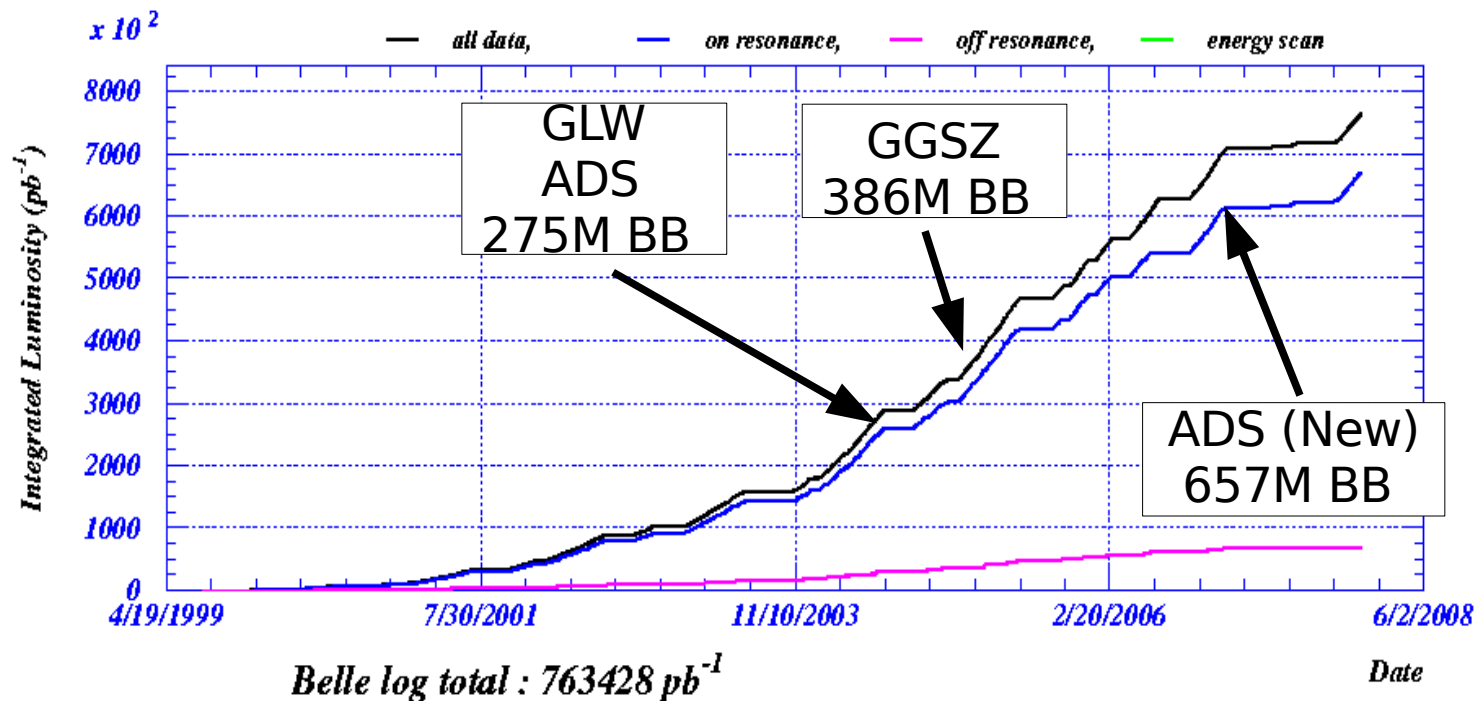
Three types of final state f of D^0 and \bar{D}^0 decays

GLW (Gronau-London-Wyler) : $f = K^+ K^- , \pi^+ \pi^- , K_S \pi^0 , \dots$

ADS (Atwood-Dunietz-Soni) : $f = K^+ \pi^- , K^+ \pi^- \pi^0 , \dots$

GGSZ (Giri-Grosman-Soffer-Zupan) : $f = K_S \pi^+ \pi^-$

◦ The Luminosity of KEKB/Belle with corresponding analyses



GLW

$f = \text{CP eigenstates}$
 $(K^+ K^-, \pi^+ \pi^-, K_S \pi^0, \dots)$

PRD(RC)73, 051106 (2006)

Belle: 275M BB

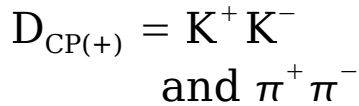
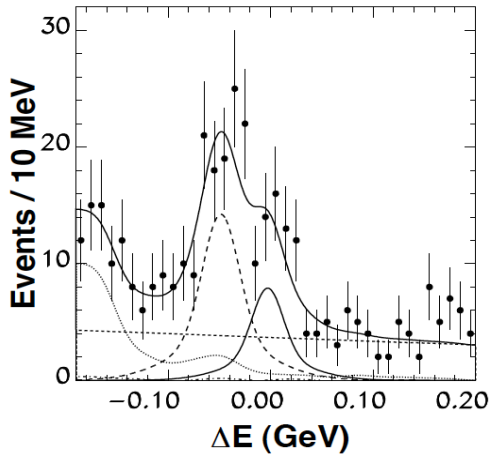
R_{CP} : Ratio to $B^- \rightarrow D^0 K^-$

$$R_{CP(\pm)} = 1 + r_B^2 \pm 2r_B \cos \delta_{CP} \cos \phi_3$$

\mathcal{A}_{CP} : Charge asymmetry

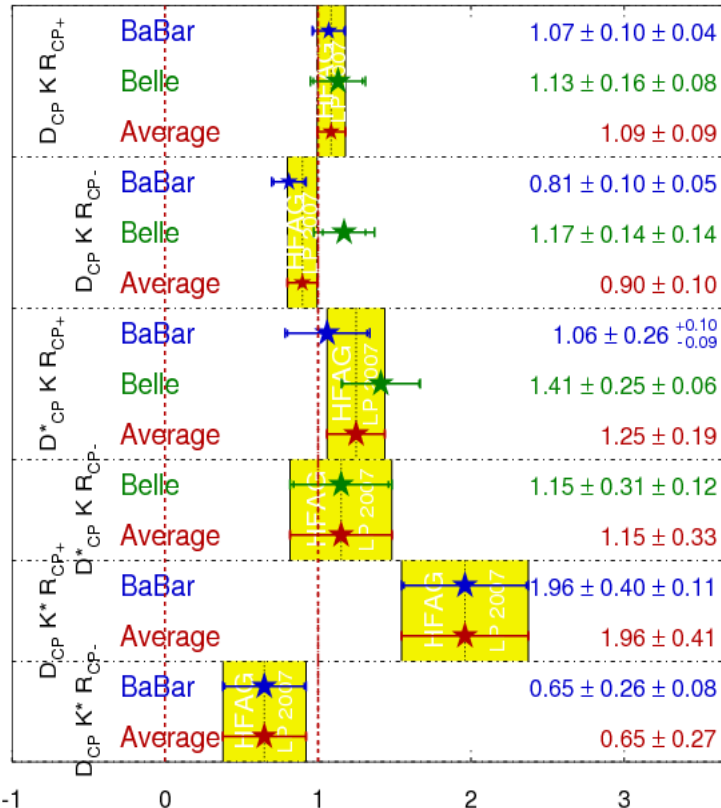
$$\mathcal{A}_{CP\pm} = \frac{\pm 2r_B \sin \delta \sin \phi_3}{1 + r_B^2 \pm 2r_B \cos \delta \cos \phi_3}$$

Signals are observed.



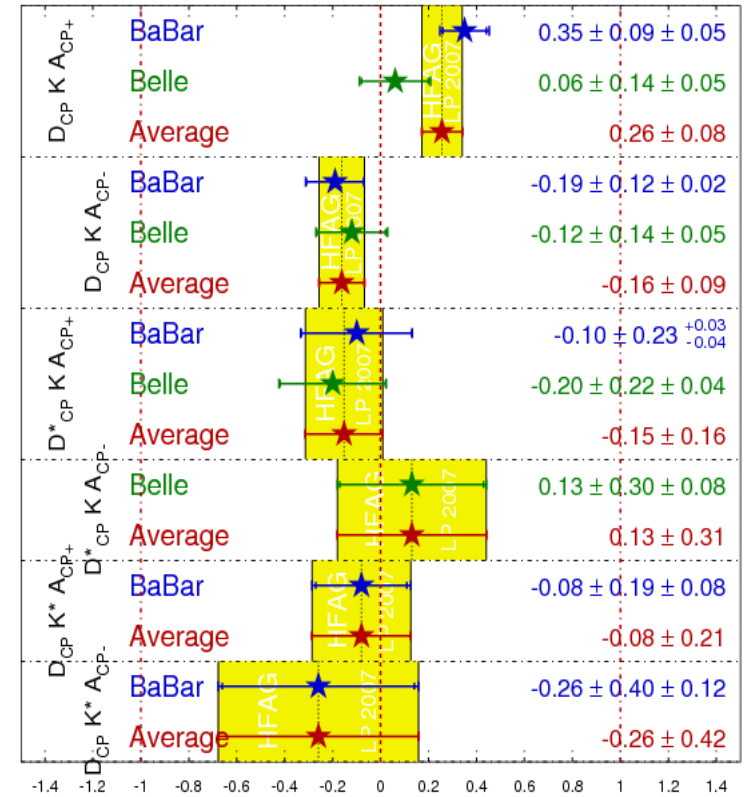
R_{CP} Averages

HFAG
LP 2007
PRELIMINARY



\mathcal{A}_{CP} Averages

HFAG
LP 2007
PRELIMINARY



Can be used to improve the constraint by GGSZ at present.

GGSZ

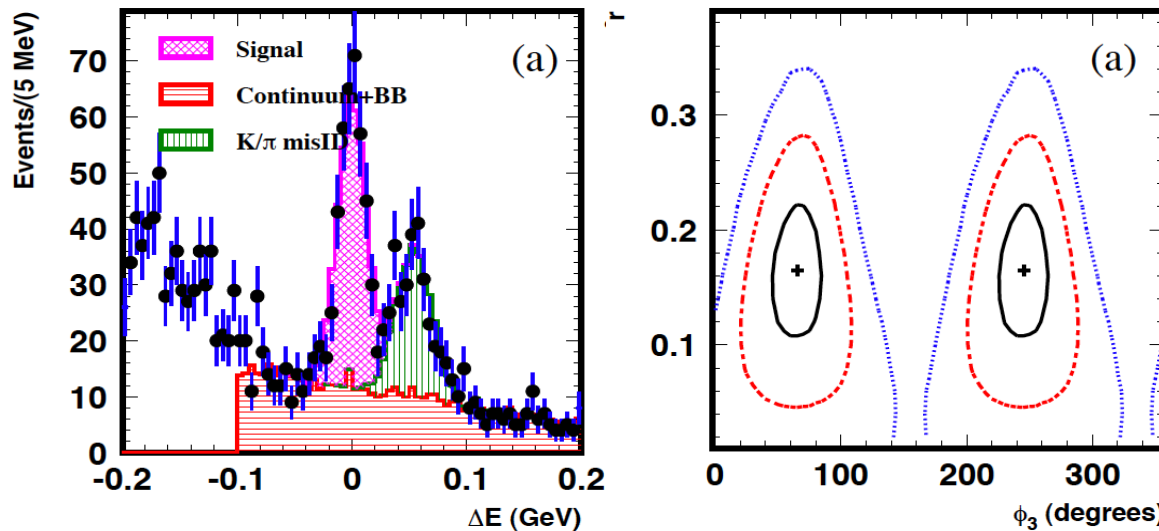
PRD73, 112009 (2006)

Belle: 386M BB

$$f = K_S \pi^+ \pi^-$$

The most precise determination of ϕ_3 comes from this method.

○ $B^- \rightarrow DK^-$



$$\phi_3 = 66^{+19}_{-20}(\text{stat})$$

○ Combining $B^- \rightarrow DK^-$, $B^- \rightarrow D^* K^-$, and $B^- \rightarrow DK^{*-}$,

$$\phi_3 = 53^{+15}_{-18}(\text{stat}) \pm 3^\circ(\text{syst}) \pm 9^\circ(\text{model})$$

$$r_B(DK) = 0.157^{+0.054}_{-0.050}$$

$$r_B(D^*K) = 0.175^{+0.108}_{-0.099}$$

$$r_B(DK^*) = 0.564^{+0.216}_{-0.155}$$

Analysis of $B^- \rightarrow [K^+ \pi^-]_D K^-$

ADS $f = K^+ \pi^-$

◦ Main decays

◦ $B^- \rightarrow [K^+ \pi^-]_D K^- : B^- \rightarrow D_{\text{sup}} K^-$

◦ $B^- \rightarrow [K^- \pi^+]_D K^- : B^- \rightarrow D_{\text{fav}} K^-$

$$R_{DK} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{\text{sup}} K^-) + \mathcal{B}(B^+ \rightarrow D_{\text{sup}} K^+)}{\mathcal{B}(B^- \rightarrow D_{\text{fav}} K^-) + \mathcal{B}(B^+ \rightarrow D_{\text{fav}} K^+)}$$

$$= r_B^2 + r_D^2 + 2r_B r_D \cos \phi_3 \cos \delta$$

$$r_D \equiv \left| \frac{A(D^0 \rightarrow K^+ \pi^-)}{A(D^0 \rightarrow K^- \pi^+)} \right|$$

$$\delta = \delta_B + \delta_D$$

(Strong phase difference)

◦ Reference decays: (parameterize PDF)

The charge asymmetry is expected to be very small.

◦ $B^- \rightarrow [K^+ \pi^-]_D \pi^- : B^- \rightarrow D_{\text{sup}} \pi^-$

◦ $B^- \rightarrow [K^- \pi^+]_D \pi^- : B^- \rightarrow D_{\text{fav}} \pi^-$

Large statistics

*We imply that the charge conjugate decay is included.
We use the same selection criteria whenever possible.*

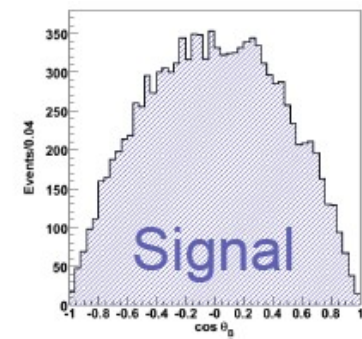
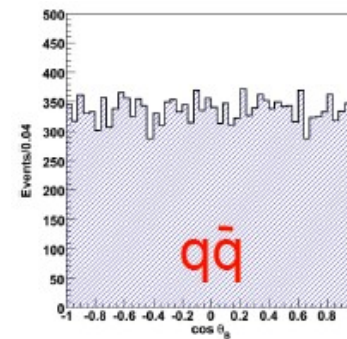
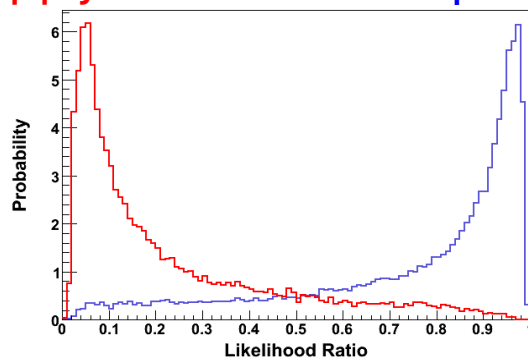
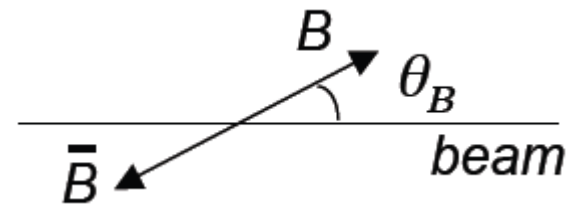
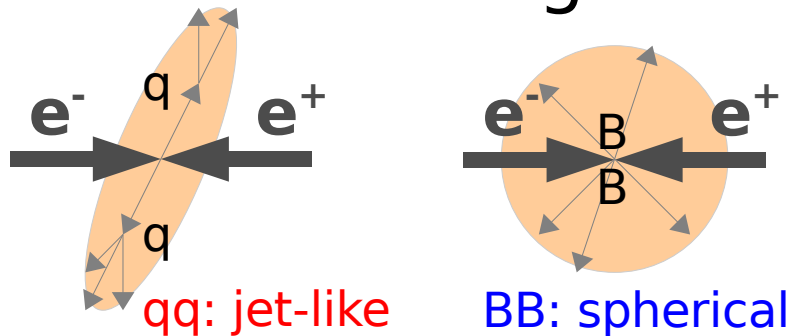
Reconstruction and $q\bar{q}$ suppression

- K/π identifications (Efficiency $\sim 90\%$, Fake rate $\sim 10\%$)
- D mass requirement: $|M(K^+\pi^-) - 1.865| < 0.015 \text{ GeV}/c^2$ (3σ)
- For B reconstruction, we use

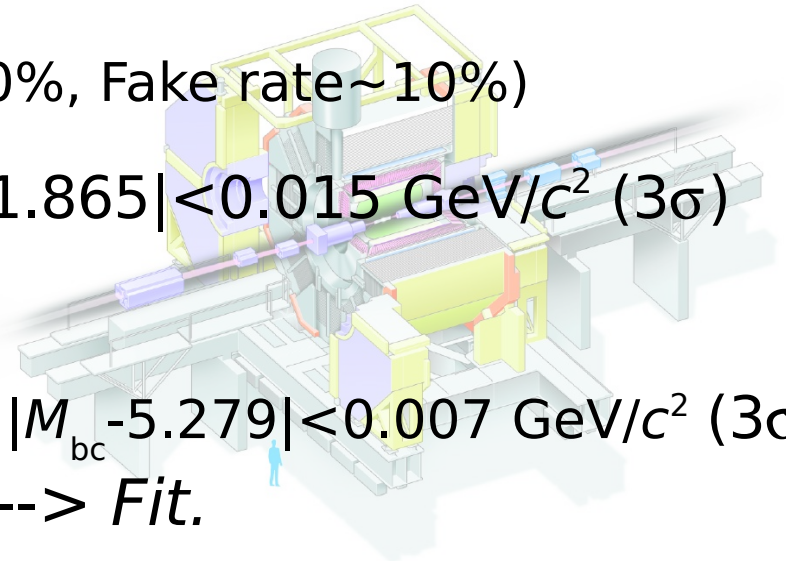
$$M_{bc} \equiv \sqrt{E_{\text{beam}}^2 - |\vec{p}_{K^+} + \vec{p}_{\pi^-} + \vec{p}_{K^-}|^2} : |M_{bc} - 5.279| < 0.007 \text{ GeV}/c^2 (3\sigma)$$

$$\Delta E \equiv E_{K^+} + E_{\pi^-} + E_{K^-} - E_{\text{beam}} \quad \rightarrow \text{Fit.}$$

- Continuum background ($e^+e^- \rightarrow q\bar{q}$) suppression $q=u,d,s,c$



$\cos \theta_B$



Background peaking in ΔE

– $B^- \rightarrow [K^+ K^-]_D \pi^-$ background

- Caused by the unfortunate condition: $M(K^+ \pi^-) \sim M_D$
- We veto events with $M(K^+ K^-) \sim M_D$
- After the veto, (0.22 ± 0.19) events will contribute *Subtract.*

– $B^- \rightarrow [K^- \pi^+]_D K^-$ (favored) background

- Caused by double misidentifications for candidates from D
- We veto events with $M(K^+ \pi^-) \sim M_D$ when IDs are swapped
- After the veto, (0.17 ± 0.13) events will contribute *Subtract.*

– $B^- \rightarrow K^+ K^- \pi^-$ background

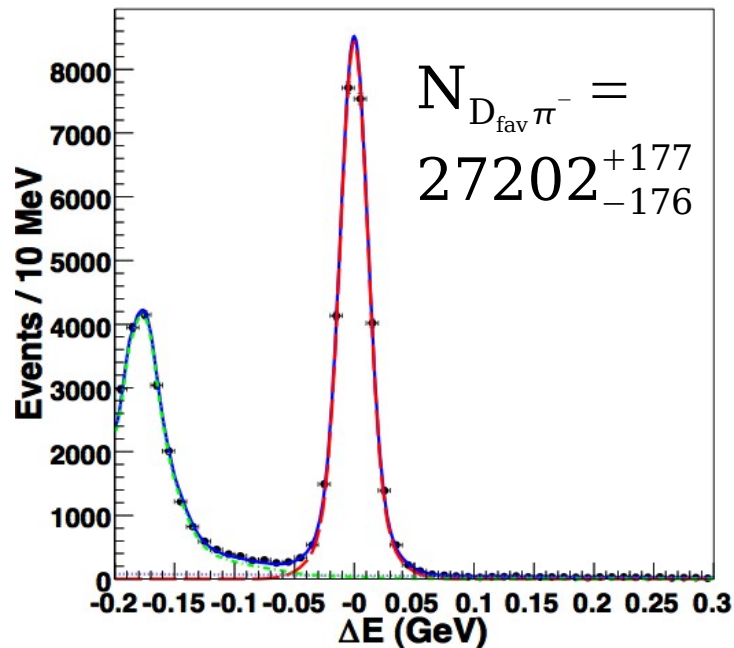
- We fit the data sample of $M(K^+ \pi^-)$ sideband, and estimate the yield contribute to the signal as (-2.3 ± 2.4) events
-->Syst. Err.

ΔE fit for Favored modes

(657M $B\bar{B}$)

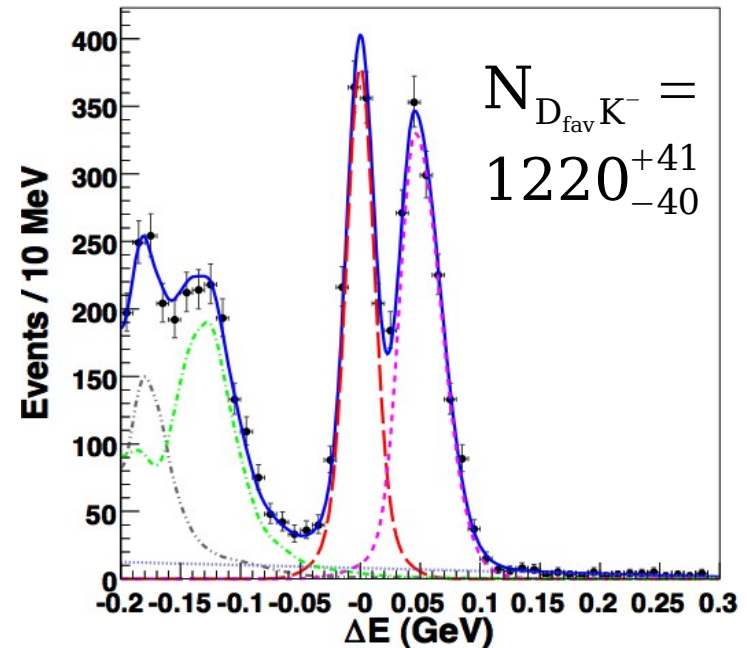
- Signal: Sum of two Gaussians
- $B^- \rightarrow X\pi^-$ BG (as $B^- \rightarrow D^*\pi^-$): Smoothed function
- $B^- \rightarrow XK^-$ BG (as $B^- \rightarrow D^*K^-$): Smoothed function
- $q\bar{q}$ BG: Linear function
- $B^- \rightarrow D\pi^-$ BG: A sum of asymmetric Gaussians

$$B^- \rightarrow D_{\text{fav}}\pi^-$$



pion mass assigned

$$B^- \rightarrow D_{\text{fav}}K^-$$

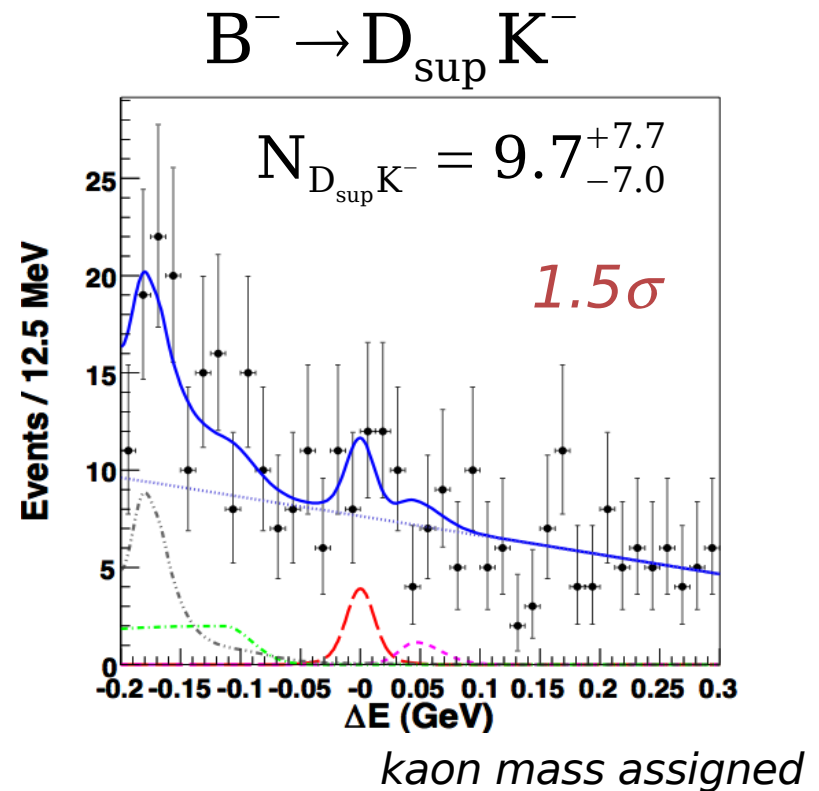
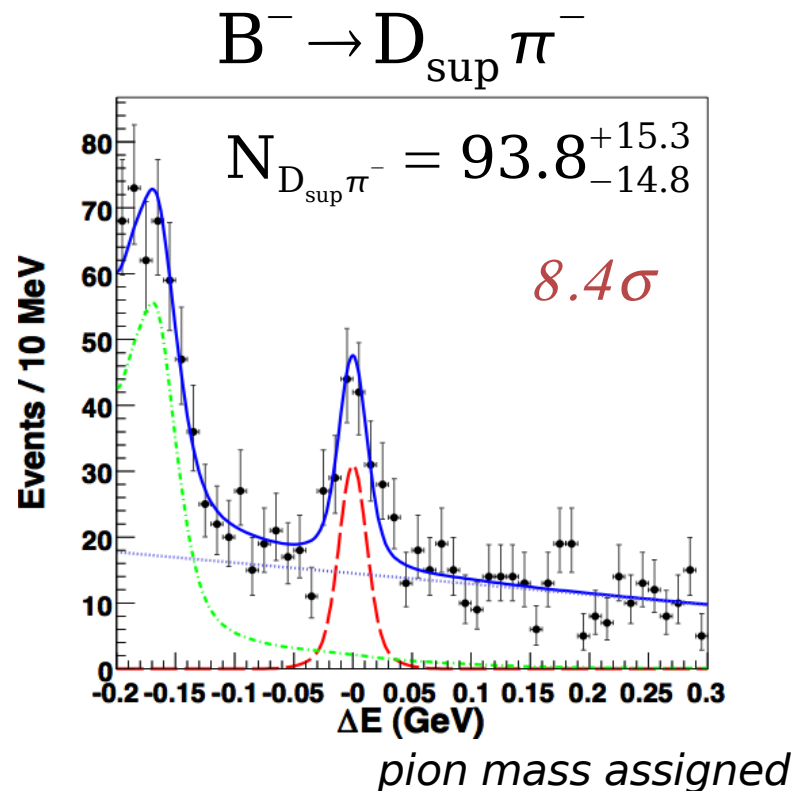


kaon mass assigned

ΔE fit for Suppressed modes

(657M $B\bar{B}$)

- Signal: Sum of two Gaussians
- $B^- \rightarrow X\pi^-$ BG (as $B^- \rightarrow D^*\pi^-$): Smoothed function
- $B^- \rightarrow XK^-$ BG (as $B^- \rightarrow D^*K^-$): Smoothed function
- $q\bar{q}$ BG: Linear function
- $B^- \rightarrow D\pi^-$ BG: A sum of asymmetric Gaussians



(657M $B\bar{B}$)

- We obtain the ratio of the branching fractions.

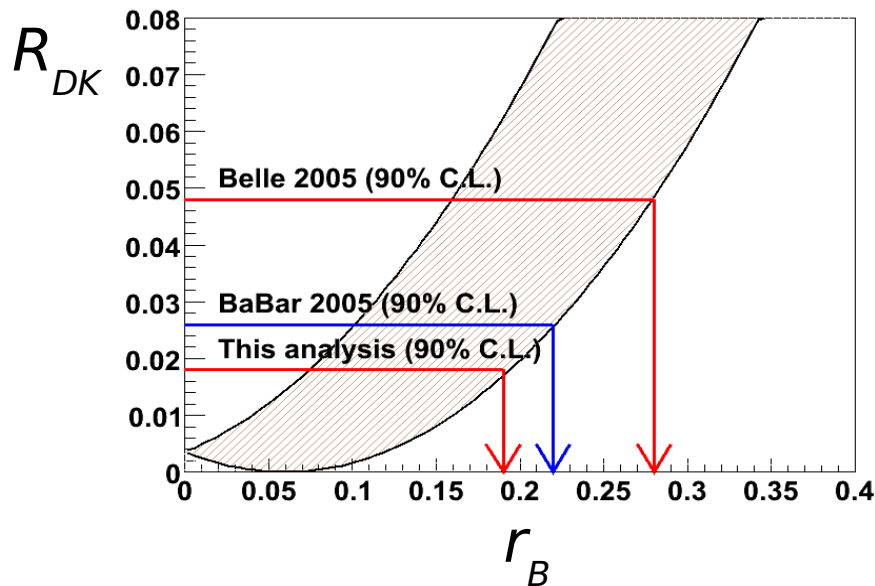
$$R_{Dh} \equiv \frac{\mathcal{B}(B^- \rightarrow D_{\text{sup}} h^-)}{\mathcal{B}(B^- \rightarrow D_{\text{fav}} h^-)} = \frac{N_{D_{\text{sup}} h^-} / \epsilon_{D_{\text{sup}} h^-}}{N_{D_{\text{fav}} h^-} / \epsilon_{D_{\text{fav}} h^-}} \quad (h = \pi, K)$$

ϵ : Detection efficiency

$$R_{D\pi} = [3.40^{+0.56}_{-0.54}(\text{stat})^{+0.13}_{-0.21}(\text{sys})] \times 10^{-3}$$
$$R_{DK} = [8.0^{+6.3}_{-5.7}(\text{stat})^{+2.0}_{-2.8}(\text{sys})] \times 10^{-3}$$

Signal is not significant for $DK \rightarrow$ $R_{DK} < 1.8 \times 10^{-2}$ (90% C.L.)

- We can then derive a limit on r_B .



$$R_{DK} = r_B^2 + r_D^2 + 2r_B r_D \cos \phi_3 \cos \delta$$

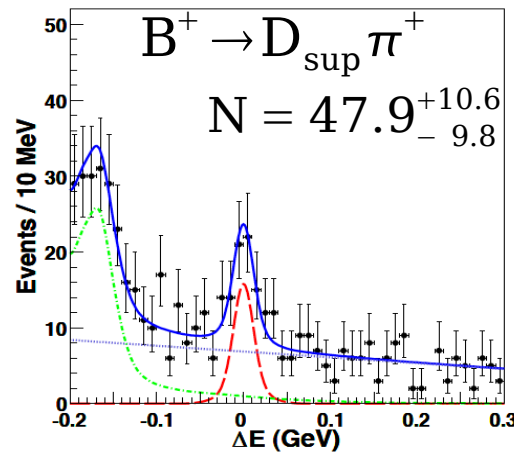
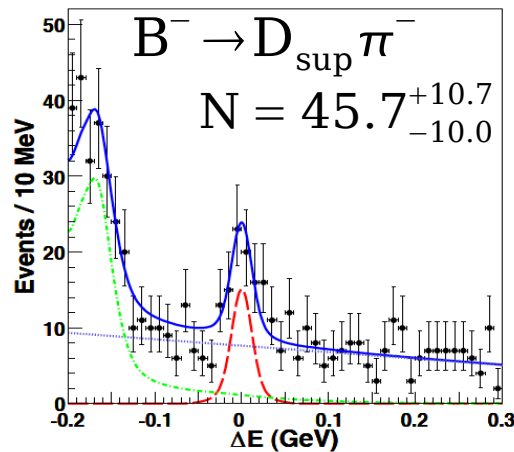
$$r_D = 0.0574^{+0.0012}_{-0.0010} \text{ [HFAG'07]}$$

$$r_B < 0.19 \text{ (90\% C.L.)}$$

(657M $B\bar{B}$)

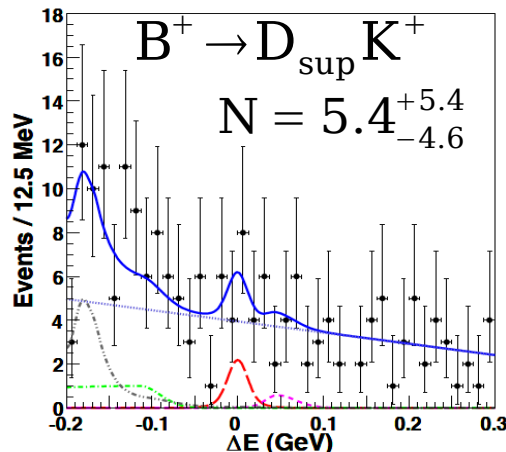
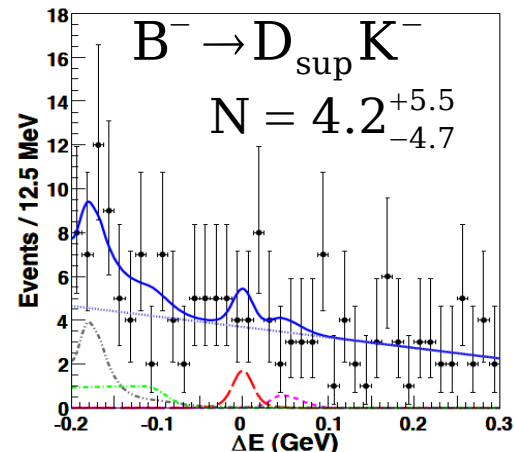
- We obtain the charge asymmetry.

$$\mathcal{A}_{Dh} \equiv \frac{\mathcal{B}(B^- \rightarrow Dh^-) - \mathcal{B}(B^+ \rightarrow Dh^+)}{\mathcal{B}(B^- \rightarrow Dh^-) + \mathcal{B}(B^+ \rightarrow Dh^+)} \quad (h = \pi, K)$$



– $A_{D\pi}$ is consistent with the expectation.

$$\mathcal{A}_{D\pi} = -0.023 \pm 0.218(stat) \pm 0.071(sys)$$



– Will need much more statistics to measure ϕ_3 with ADS method.

$$\mathcal{A}_{DK} = -0.13^{+0.97}_{-0.88}(stat) \pm 0.26(sys)$$

Summary

- The methods for extracting ϕ_3 are overviewed.
- New result on $B^- \rightarrow [K^+ \pi^-]_D h^-$ is reported.
 - For $D_{\text{sup}} \pi^-$, the asymmetry is measured to be consistent with zero as expected.
 - No significant signal is observed for $D_{\text{sup}} K^-$, and we set an upper limit of $r_B < \mathbf{0.19}$ at 90% C.L.

