

# The precise measurement of Higgs mass and cross section by recoil method

**Shun Watanuki<sup>A</sup>**

H.Yamamoto<sup>A</sup>, A.Ishikawa<sup>A</sup>, J.Strube<sup>A</sup>, T.Suehara<sup>B</sup>, K.Fujii<sup>C</sup>

(A : Tohoku University, B : Kyushu University, C : KEK)

# Target

One of the advantages of the ILC is **model independent (MI)** analysis of Higgs properties by **recoil method**.



- How precise can we measure Higgs **mass** and **cross section** by this method? The considered situations are ...

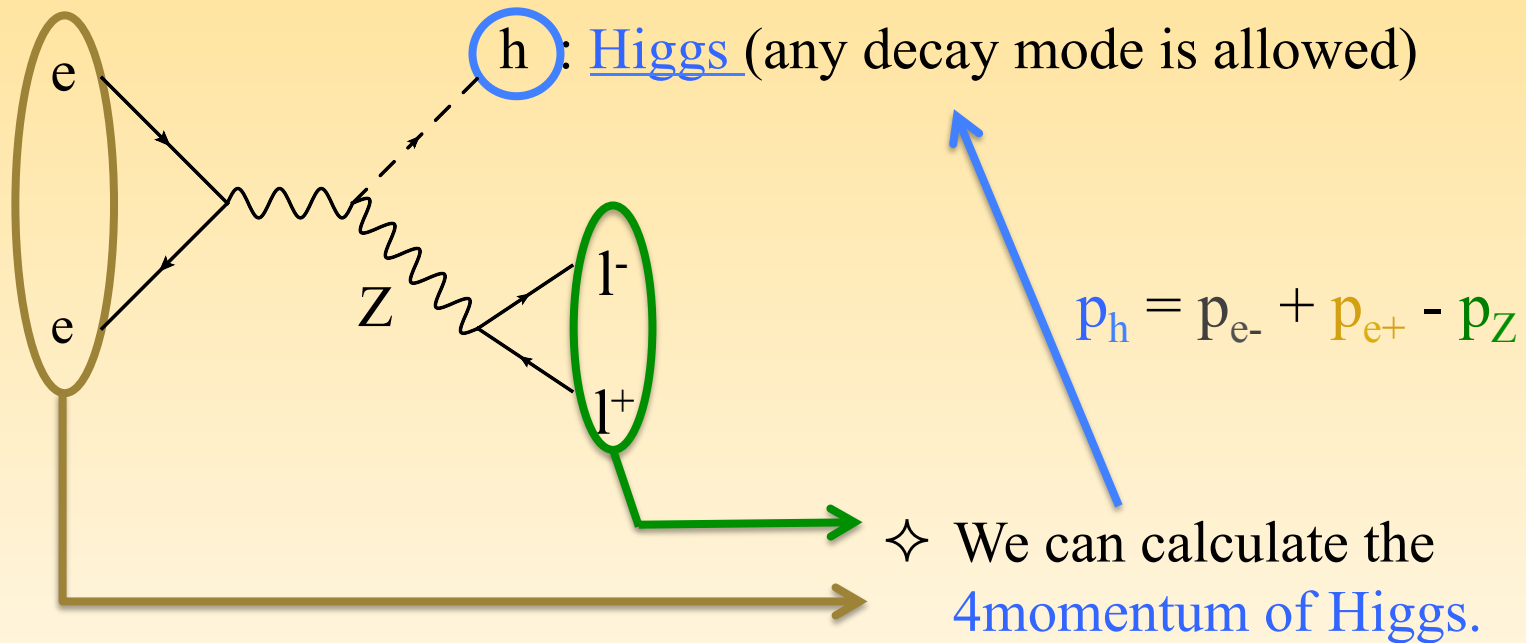
Production Mode	Higgs mass (GeV)	$E_{\text{CM}}$ (GeV)	Integrated Luminosity	Spin Polarization	Detector Simulation
$e^+e^- \rightarrow Zh \rightarrow \mu\mu h, eeh$	125	250	250 fb <sup>-1</sup>	$P(e^-, e^+) = (\mp 0.8, \pm 0.3)$	ILD_01_v05 (DBD ver.)

- Using only  $Zh \rightarrow llh$  ( $l = \mu, \text{ or } e$ ) signal event.



# What's the Recoil Method?

- ILC is a **lepton collider**  
= We already know initial state 4 momentum



Aim for Higgs  $\sigma$  measurement

Directly

It depends on the model of Higgs decay

Recoil method

We can measure Higgs **model independently**

# Keywords of the Study

## 1. Model independent analysis

- This means unbiased selections should be used  
= The bias of signal efficiency for each major Higgs decay must be suppressed at least within uncertainty of  $\sigma$  measurement

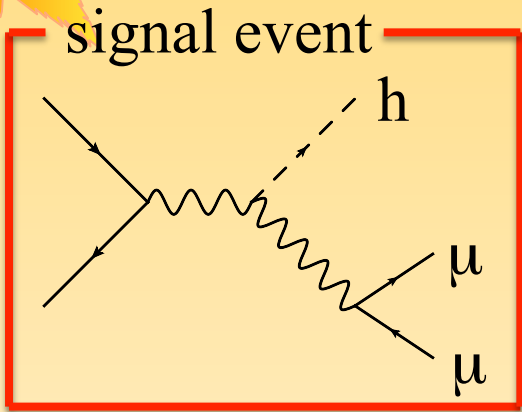
## 2. Precise measurement

- Maximize precision while staying model independent
- Comparison between different polarization cases

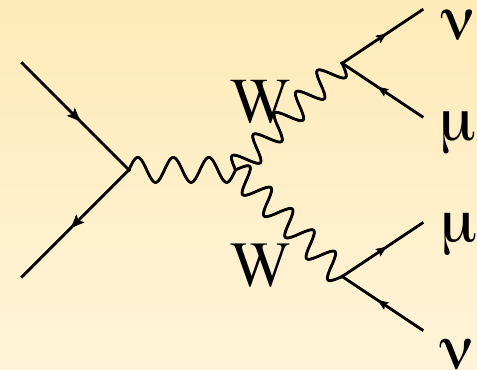
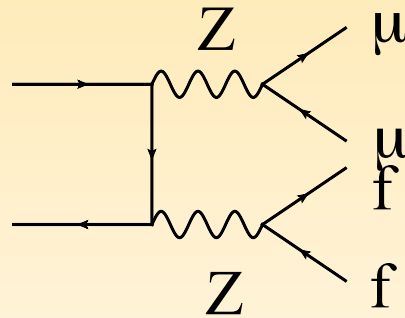
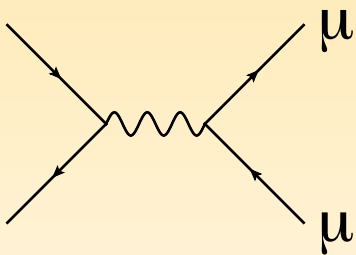
## 3. Mass template method

- This method is tried in order to estimate Higgs mass ignoring systematic uncertainty

# Signal and Background Events



- These are  $\mu\mu h$  channel signal & BGs.
- For  $e e h$  channel study, character of “ $\mu$ ” and “ $\nu$ ” are altered appropriately.



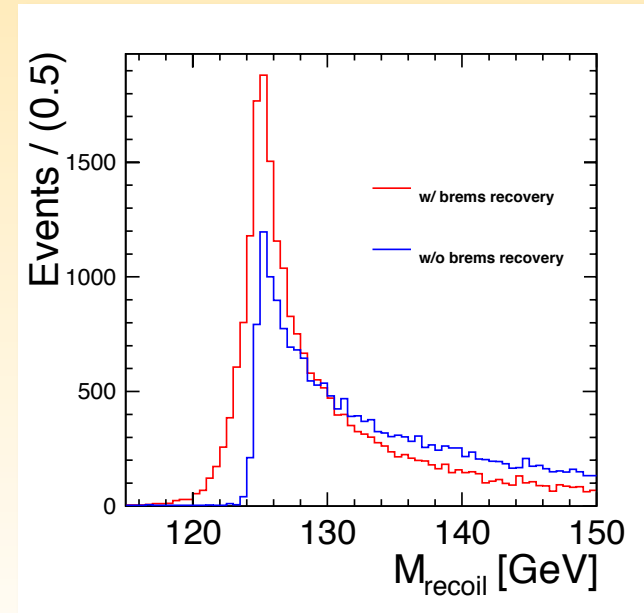
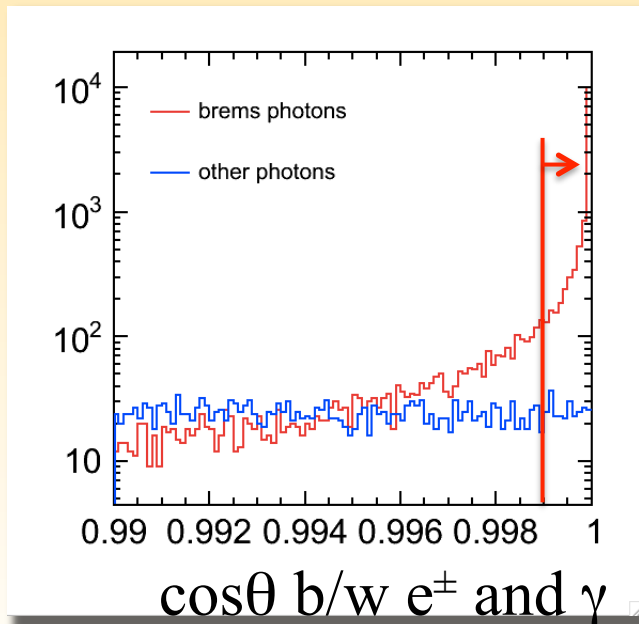
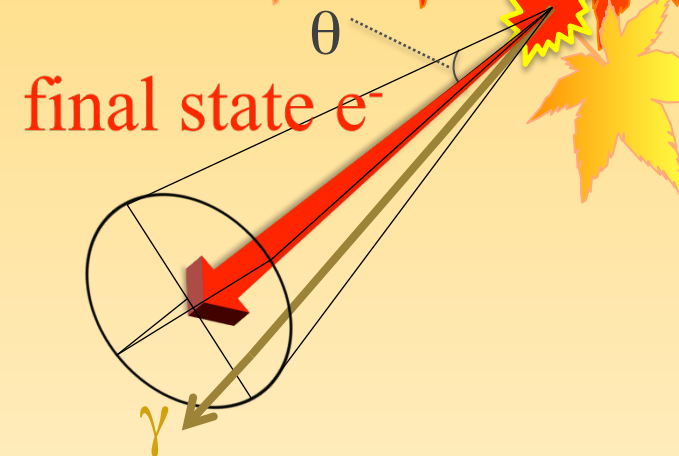
- Dominant Background is “ $\mu\mu$ ”, “ $\mu\mu\nu\nu$ ”, “ $\mu\mu f f$ ” events, and other BG is rejected significantly.

# Lepton Selection

- Muon (electron) selection
  - based on deposited energy in calorimeter
- Good track selection
  - based on error in forward / barrel
- Impact parameter (only for muon)
  - To suppress muons from tau decays
- Bremsstrahlung recovery (only for electron)
  - Photons emitted from electron are recovered.

# Bremsstrahlung Recovery

- Only for eeh channel, momentum of photon around **final state electron** is added to the electron.
  - $\cos\theta > 0.9995$
  - $\cos\theta > 0.999 \ \&\& \ E_{\text{photon}}/E_{\text{electron}} > 0.03$
  - not split photon
- This process contributes to the distribution of recoil mass significantly.



✘ For mass analysis, it is effective not to perform the recovery.



# BG Rejection

$p_{Tdl} > 20 \text{ GeV}$

$M_{dl} \in (80, 100) [\text{GeV}]$

$a_{\text{cop}} \in (0.2, 3.0)$

$\delta p_{Tbal} \notin (-10, 10) [\text{GeV}]$

$\cos \theta_{\text{missing}} < 0.99$

$M_{\text{recoil}} \in (115, 150) [\text{GeV}]$

Likelihood

$\mu\mu$

$\mu\mu\nu\nu$

$\mu\mu$

$\mu\mu\gamma$

$\mu\mu\gamma$

$\mu\mu$   
 $\mu\mu\nu\nu$   
 $\mu\mu ff$

$\mu\mu$   
 $\mu\mu\nu\nu$   
 $\mu\mu ff$



## Left Handed Case

$\mu\mu h$	signal	ll	llvv	llff	others
No Cut	2603	3.2M	507166	390041	7.1M
After Cut	1386	322	1479	1054	3
eeh	signal	ll	llvv	llff	others
No Cut	2729	7.8M	520624	404279	2.5M
After Cut	1190	1496	2203	937	4

## Right Handed Case

$\mu\mu h$	signal	ll	llvv	llff	others
No Cut	1756	2.6M	51768	330876	6.3M
After Cut	1113	287	323	650	3
eeh	signal	ll	llvv	llff	others
No Cut	1844	7.3M	52853	358595	1.5M
After Cut	742	927	230	393	1

**BG with neutrino is suppressed significantly**

# Unbiased Selection

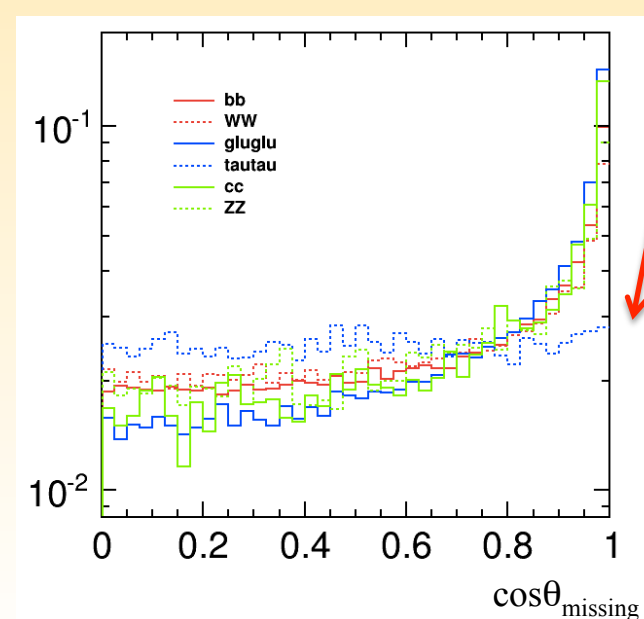
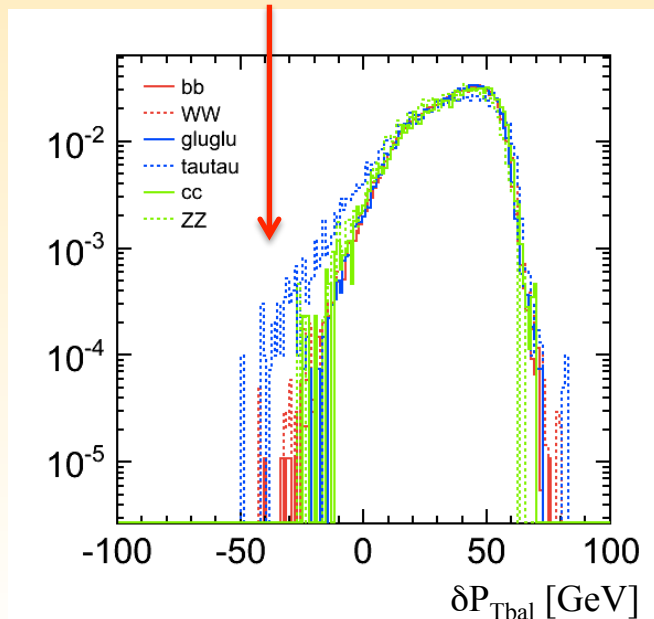
- Signal efficiencies should be same for each Higgs decay modes, but  $h \rightarrow \tau\tau$  mode tends to have a bias

$$\delta P_{T_{\text{bal}}}$$

$$\cos\theta_{\text{missing}}$$

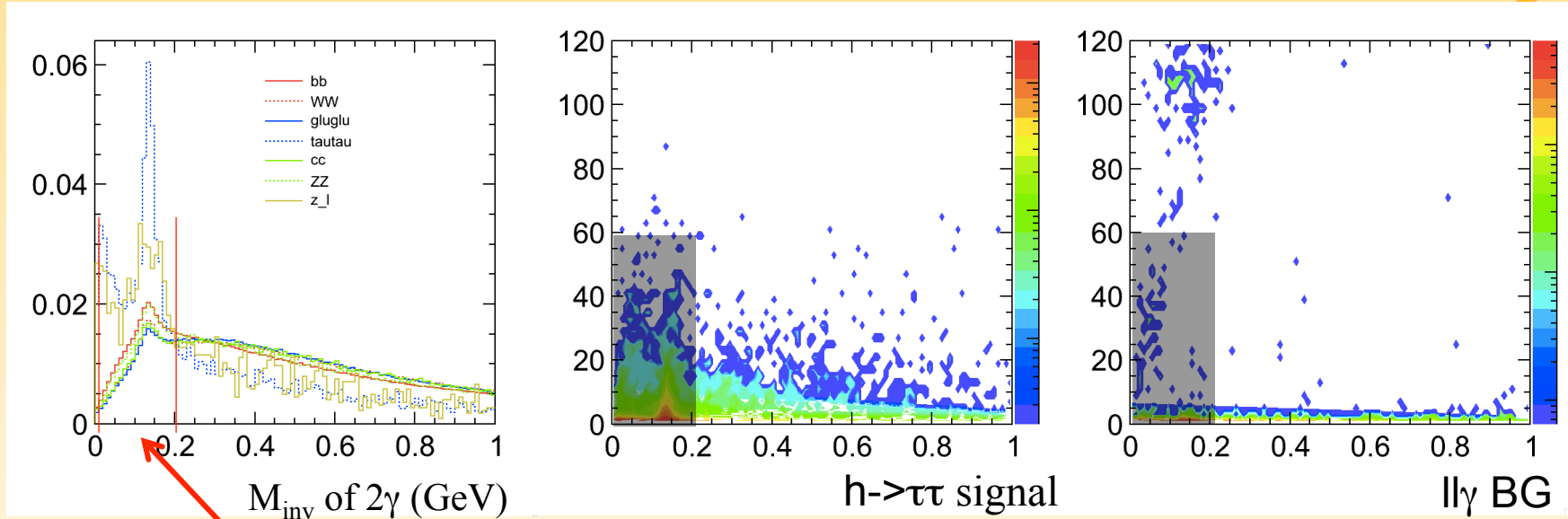
- $\delta P_{T_{\text{bal}}} = P_{T_{\text{dl}}} - P_{T_{\text{photon}}} \notin (-10, 10)$
- $h \rightarrow \tau\tau$  has long tail

- $\cos\theta$  of all PFOs  $< 0.99$
- $h \rightarrow \tau\tau$  has uniform distribution

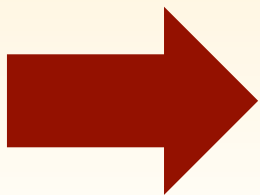


# Bias Suppression (for $\delta P_{Tbal}$ )

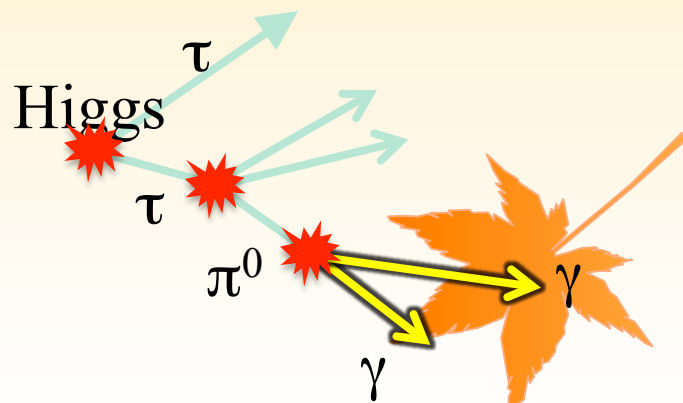
- We can suppress this bias using **Energy** of photon and **invariant mass** of each photon pair.



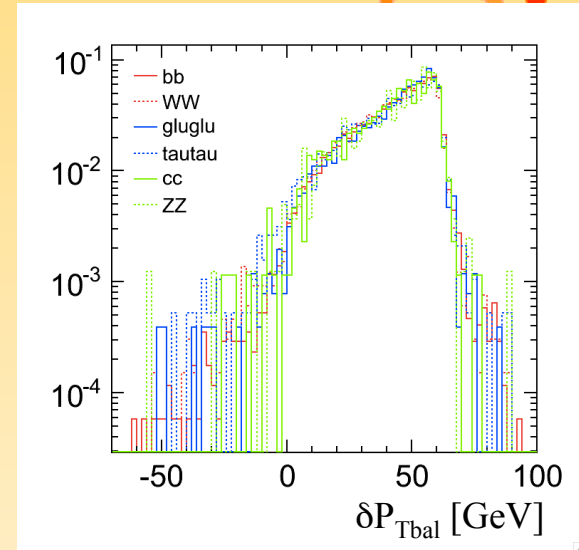
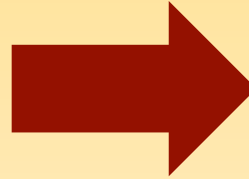
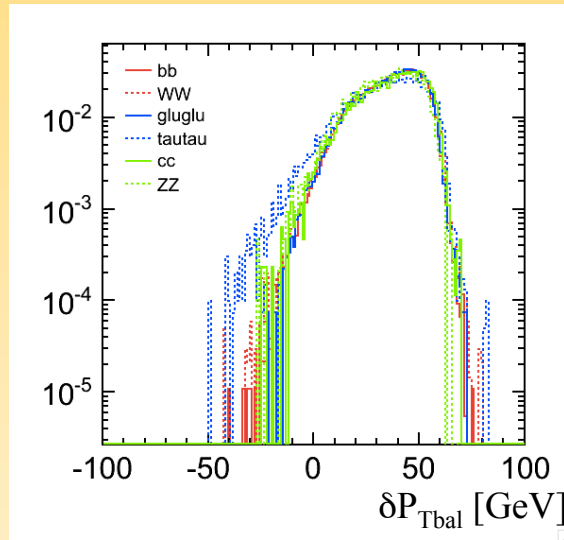
In  $h \rightarrow \tau\tau$ , there is a peak at  $m_{2\gamma} \sim m_{\pi}$



condition of used $\gamma$
$m_{2\gamma} > 0.2$ [GeV]
or $E_{\gamma} > 60$ [GeV]



# Bias Suppression (for $\delta P_{Tbal}$ )



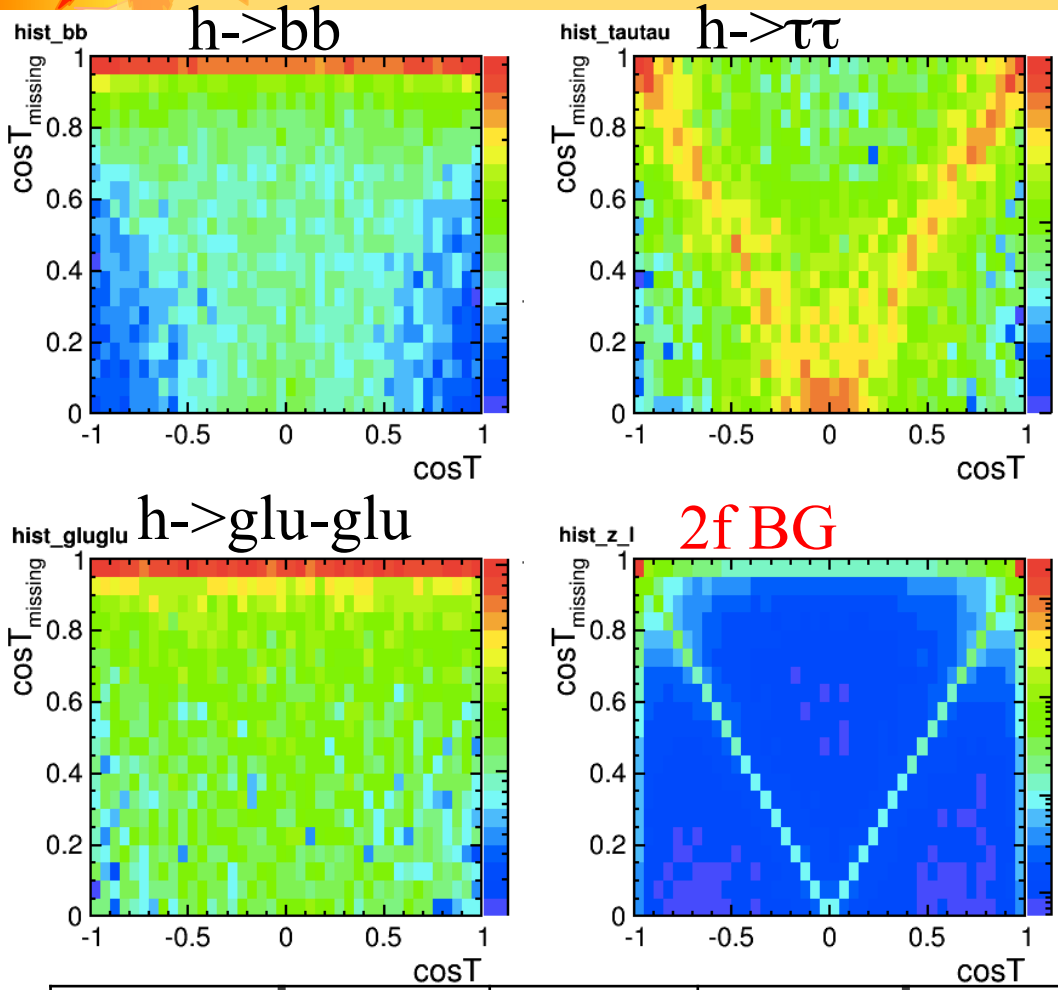
Comparison  
old & new

efficiency of  $dP_{Tbal}$  cut

	bb	$\tau\tau$	cc	z_1 (BG)
Simple calc.	99.4%	95.3%	99.0%	14.5%
My calc.	99.8%	97.8%	99.6%	22.2%

- In new calculation of  $\delta P_{Tbal}$ , bias will decrease.

# Bias Suppression (for $\cos\theta_{\text{missing}}$ )



- $\cos\theta$  of Z boson as additional variable is useful to suppress the bias.

- $|\cos\theta_{\text{missing}}| < 0.99$
- or  $|\cos\theta_{Z \text{ boson}}| < 0.8$

- Using these additional condition, efficiency of BG rejection is sacrificed, but it can avoid the bias.

	bb	glu-glu	$\tau\tau$	BG (II)
$\cos\theta_{\text{miss}} < 0.99$	95.1%	92.8%	99.2%	41.1%
$\cos\theta_{\text{miss}} < 0.99$ or $ \cos\theta  < 0.8$	99.3%	99.1%	99.8%	74.6%

← Previous  
 ← New



# Signal Efficiency

- After that, bias of signal efficiency for Higgs decay is eliminated.

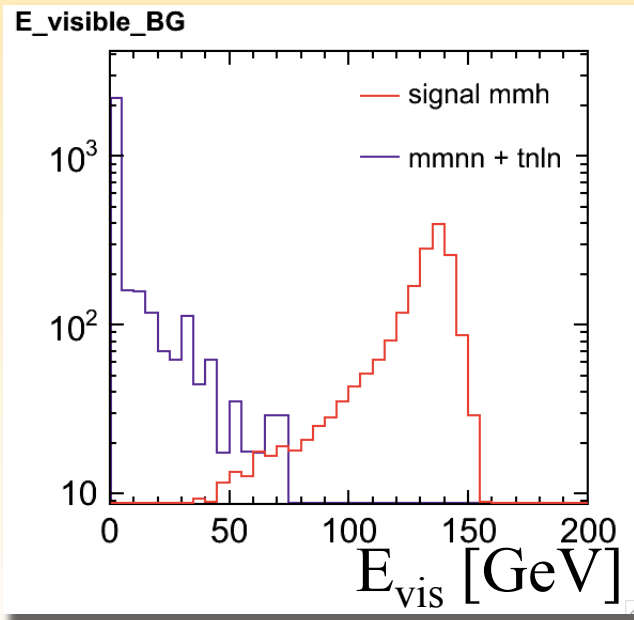
H decay mode	$\mu\mu h$ efficiency [%]	eeh efficiency [%]
bb	55.61	45.62
WW	55.39	44.95
gluglu	55.16	45.02
$\tau\tau$	55.42	44.49
cc	55.60	45.14
ZZ	54.04	45.51

- Systematic error due to efficiency in decay modes is 3%.
- (If we could use the information on measured cross section for higgs decay modes, the error should be much smaller)

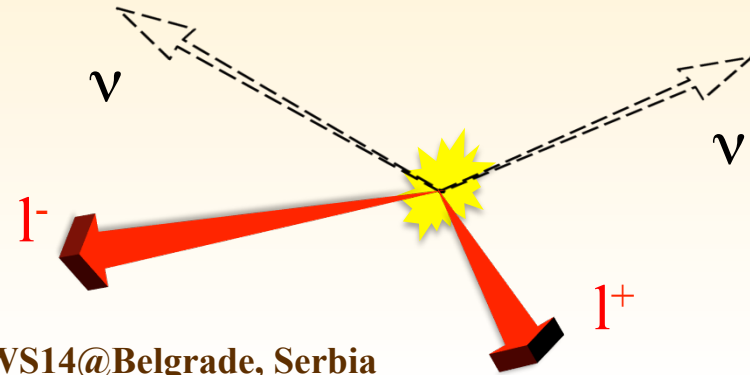
# Visible Energy Selection (Semi-MI analysis)

$\mu\mu h$	signal	$ll$	$ll\nu\nu$	$llff$	others
After Cut	1386	322	1479	1054	3
$\mu\mu$	signal	$ll$	$ll\nu\nu$	$llff$	others
		1496	2203	937	4

There seems to be large number of remaining  $ll\nu\nu$  BG.

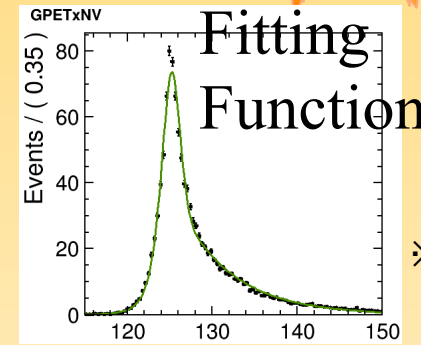
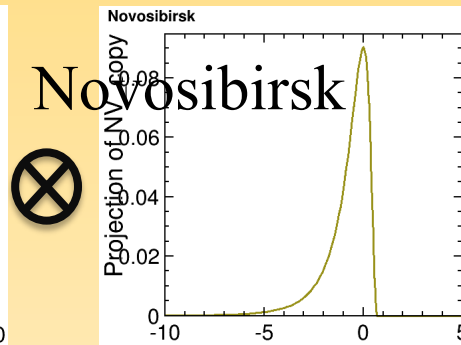
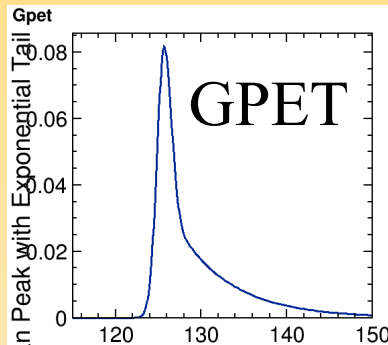


- Since contribution from Higgs invisible decays can be calibrated with data, visible energy selection is effective for reducing these BG.
- $E_{vis} := E_{PFOs} - E_{di-lepton} > 5 [GeV]$
- Loose selection is applied to avoid bias in signal selection.





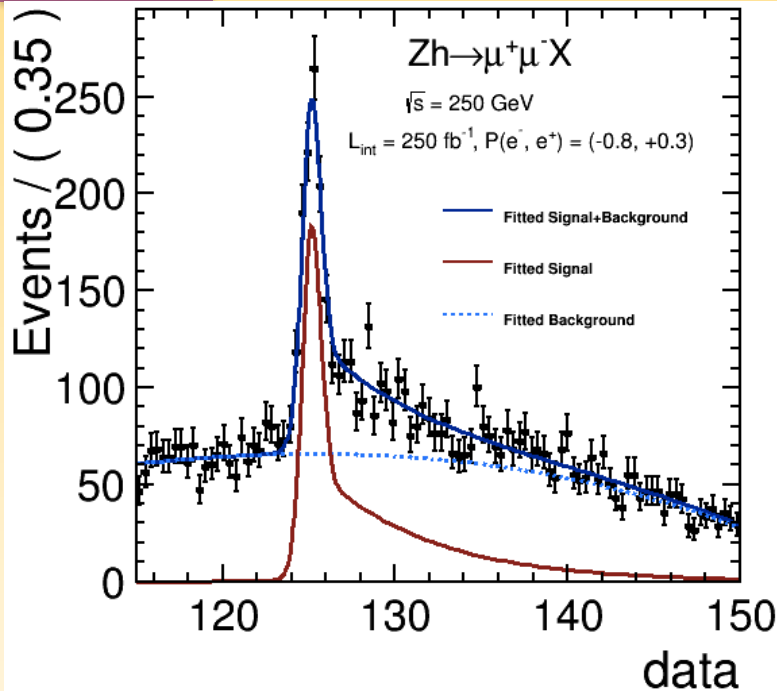
# Fitting Function



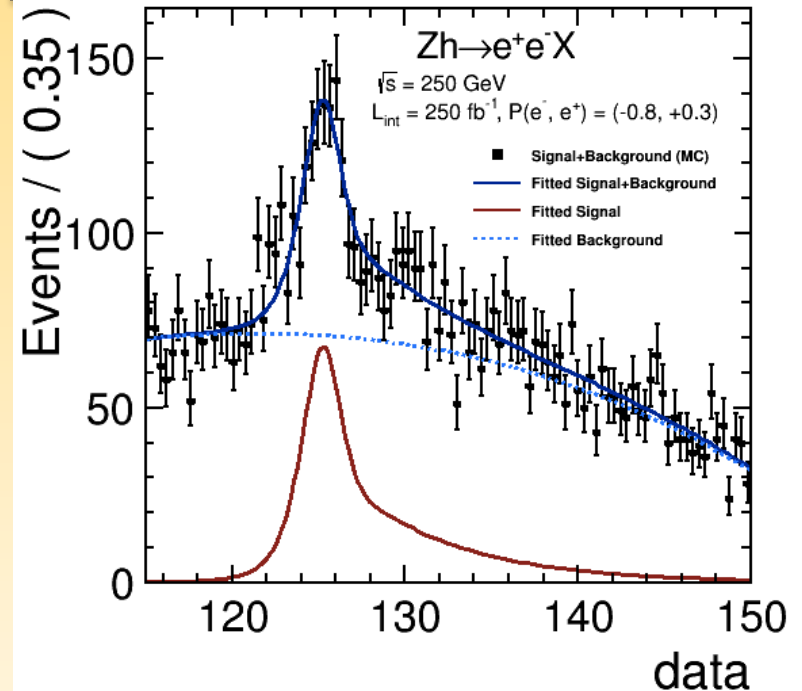
- GPET is constructed by Gaussian peak and exponential tail.
- Novosibirsk can express uncertainty of lepton detection.
  - For detail of Novosibirsk function, please check [Nuclear Instruments and Methods in Physics Research A 441 (2000) 401-426]
- For BG fitting, 3<sup>rd</sup> order polynomial is used. (BG shape is determined separately from signal shape determination)
- In pseudo-experiments, **PDF shape is fixed** and only number of signal and BG is floated.

# Fitting Results (Left Handed)

$\mu\mu h$



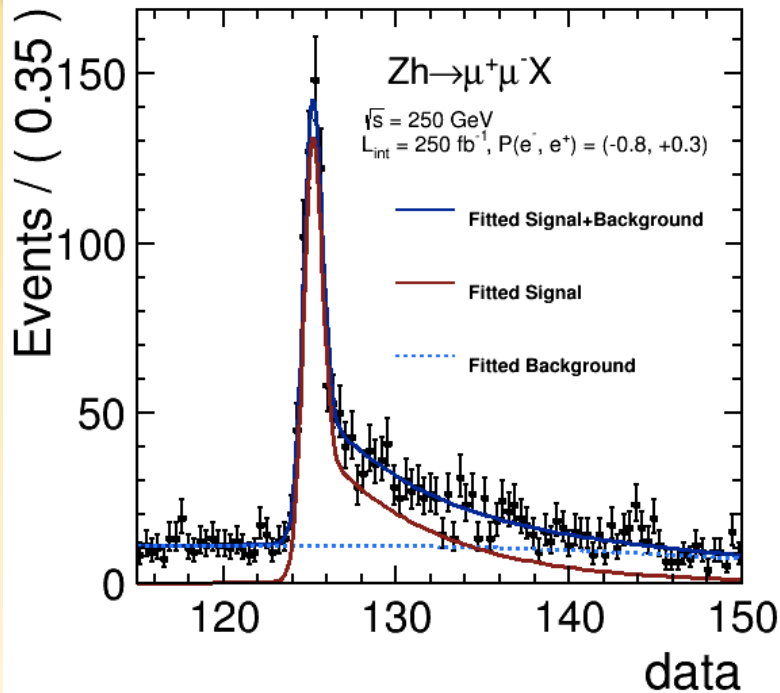
$eeh$



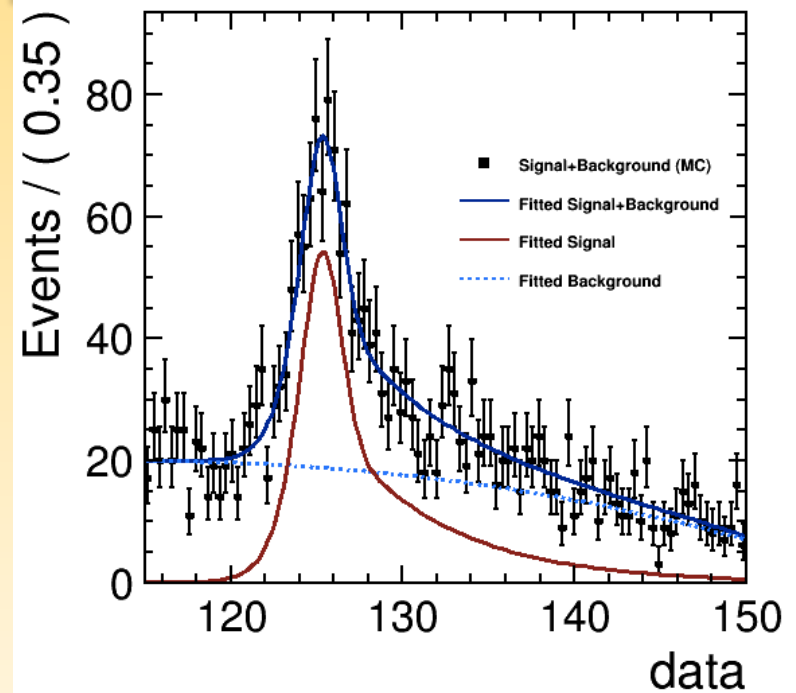
$L=250\text{fb}^{-1}$ $P(e^-, e^+) = (-0.8, +0.3)$	$\mu\mu h$		$eeh$		combined	
	MI	semi-MI	MI	semi-MI	MI	semi-MI
$\Delta\sigma/\sigma$	4.2%	3.8%	6.0%	5.6%	3.4%	3.1%
$\Delta\text{mass [MeV]}$	34	33	231	89	34	31

# Fitting Results (Right Handed)

$\mu\mu h$



$ee h$

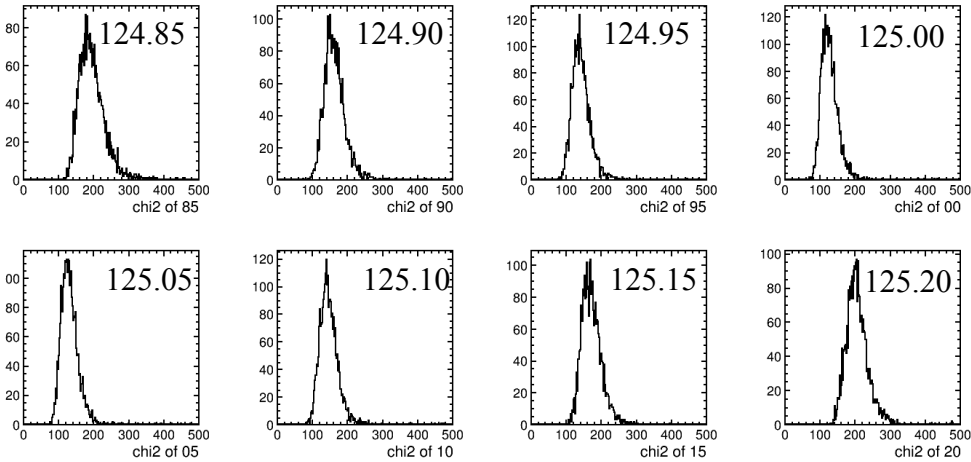
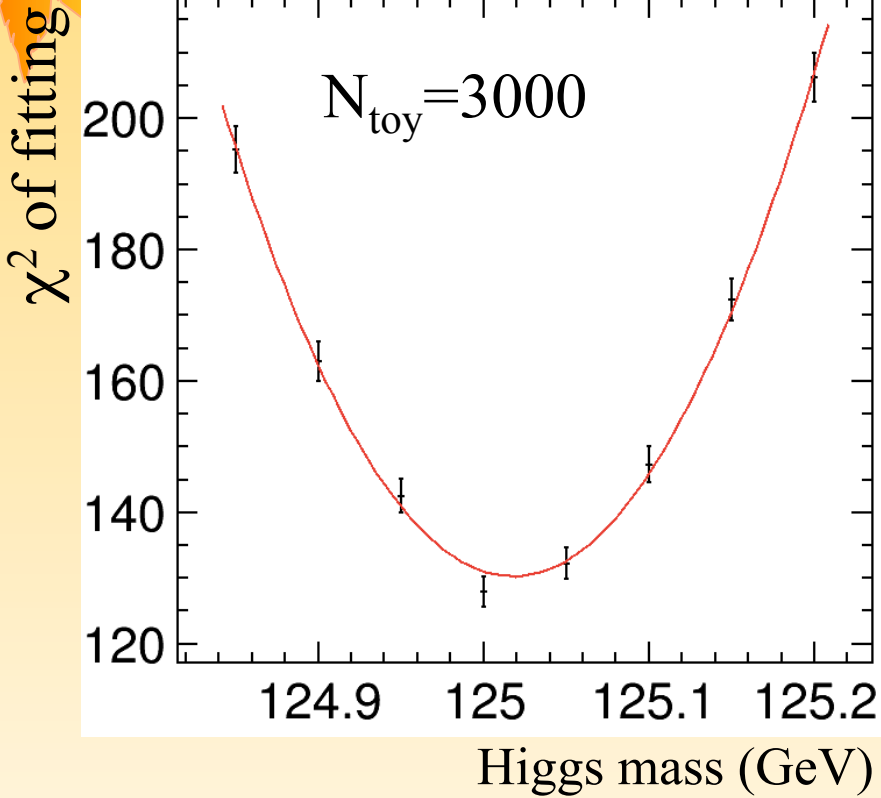


$L=250\text{fb}^{-1}$ $P(e^-, e^+) = (-0.8, +0.3)$	$\mu\mu h$	$ee h$	combined
$\Delta\sigma/\sigma$	3.8%	6.0%	3.2%
$\Delta\text{mass} [\text{MeV}]$	31	214	31

# Mass Template Method

- To avoid systematic bias of mass parameter, mass template method is tried.
- Fit dataset by PDFs from template samples with different Higgs mass.
- Template samples with  $M_{\text{Higgs}} = 124.85, 124.90, 124.95, 125.00, 125.05, 125.10, 125.15, \text{ and } 125.20$  are used (8points).
- Signal PDF is used as histograms reconstructed from template samples.
- BG PDF is used as 3<sup>rd</sup> order polynomial from DBD sample fitting.
- Toy-MC is made for data points, and mean of  $\chi^2$  values is plotted and fitted by parabola.
- Mass value at minimum  $\chi^2$  point is estimated Higgs mass.

# Fitting Result



histograms of  $\chi^2$

- Minimum position :  
 $x = 125.018 \pm 0.021$  (GeV)

# Summary and Next Plan

- The recoil mass technique is an important feature at the ILC to measure Higgs mass and cross section of ZH.

$\mu\mu h, eeh$ @250GeV		$\mu\mu h$		$eeh$		combined	
		Left	Right	Left	Right	Left	Right
MI	cross section	4.2%	3.8%	6.0%	6.0%	3.4%	3.2%
	mass [MeV]	34	31	231	214	34	31
semi-MI	cross section	3.8%		5.6%		3.1%	
	mass [MeV]	33		89		31	

- Using the mass template method, the Higgs mass can be decided within **21MeV**.
- I will estimate also the sensitivity to Higgs **CP-mixture**, which can obtain a non-zero value from anomalous coupling in 2HDM, from the Z production angle.



# BACK UP SLIDES

2014/10/07

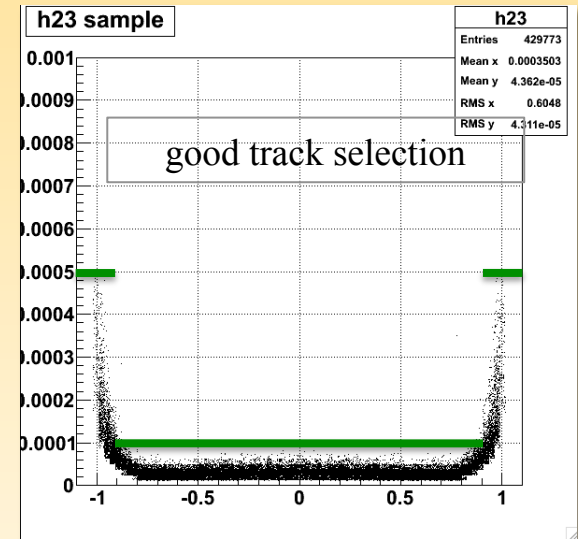
Shun Watanuki  
LCWS14@Belgrade, Serbia





# Lepton Selection

- Muon (electron) selection
  - Momentum  $p > 15$  [GeV]
  - Small (Large) energy deposited in calorimeters
    - $E_{\text{ecal}} / E_{\text{total}} < 0.5$  ( $> 0.6$ )
    - $E_{\text{total}} / p_{\text{track}} < 0.3$  ( $> 0.9$ )
- Good track selection
  - Track with small error (different selections between polar angle of tracks, barrel or end cap)
    - $dp / p^2 < 2.5 \times 10^{-5} \oplus 8 \times 10^{-4} / p$   
(for  $\cos\theta < 0.78$ )
    - $dp / p^2 < 5 \times 10^{-4}$   
(for  $\cos\theta > 0.78$ )
- Impact parameter (only for muon)
  - To suppress muons from tau decays which tend to have large impact parameters.  
 $D_0 / dD_0 < 5$



$dp / p^2$

# Efficiency of $E_{\text{visible}}$

H decay mode	$\mu\mu h$ ( $E_{\text{vis}}$ eff.)	After all cut	$ee h$ ( $E_{\text{vis}}$ eff.)	After all cut
bb	100%	66.31%	98.68%	39.14%
WW	100%	66.00%	98.31%	38.67%
gluglu	100%	65.40%	98.67%	38.82%
$\tau\tau$	99.94%	65.66%	98.43%	37.82%
cc	100%	66.32%	98.25%	39.43%
ZZ	96.64%	63.98%	94.84%	37.90%

Bias as expected from SM.

⌘ Some selections are optimized for semi-MI analysis, so that eff. is different from MI case.

